

detailed problems acc. to Eurocode 3

EC 3-1-5 (12.10), NA: Deutschland

steel grade

steel grade S 355

cross-section

beam: parameter (I-section):

$h = 3080.0 \text{ mm}$, $t_w = 15.0 \text{ mm}$, $b_f = 800.0 \text{ mm}$, $t_f = 40.0 \text{ mm}$

longitudinal stiffeners: number $n_{st} = 1$

section parameters (flat steel):

$h = 250.0 \text{ mm}$, $t = 25.0 \text{ mm}$

distance of stiffener to the top edge of beam $d_{st,0} = 2540.0 \text{ mm}$

parameters

length of buckling field $a = 300.0 \text{ cm}$

method of effective cross-sectional area

rigid support stiffener

verification at intermediate support

calculation of buckling factors acc. to EC 3-1-5

effective cross-sectional properties: A_{eff} solely from compression, W_{eff} solely from bending

verification of stability acc. to EC 3-1-1, 6.3

loading

internal forces and moments referring to the stiffened cross-section:

Lk 1: plated structures- + shear buckling (chap. 5.1.1-4)

$N_{Ed} = -4000.0 \text{ kN}$ $M_{Ed} = -33760.0 \text{ kNm}$ $V_{Ed} = 3437.5 \text{ kN}$

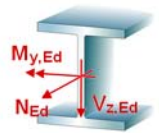
Lk 2: M-N-V-interaction (chap. 5.1.5)

$N_{Ed} = -4000.0 \text{ kN}$ $M_{Ed} = -32150.0 \text{ kNm}$ $V_{Ed} = 3288.0 \text{ kN}$

partial safety factors for material

resistance of cross-sections $\gamma_{M0} = 1.00$

resistance of members in stability failure $\gamma_{M1} = 1.10$



verifications of buckling resistance

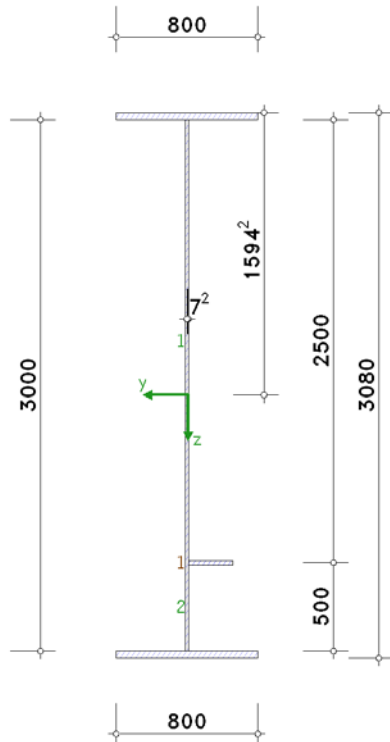
assumption: flange induced web buckling is excluded.

assumption: local buckling of stiffeners is excluded.

assumption: rotational ability of stiffeners for stress redistribution is sufficient.

assumption: plate area is supported rigidly.

the assumptions are not checked !!



method of effective cross-sectional area

EC 3-convention, compressive stresses positive

shear distortions are ignored.

cross-sectional properties: $A = 1152.50 \text{ cm}^2$, $z_s = 1594.2 \text{ mm}$, $I_y = 18753552.18 \text{ cm}^4$, $y_s = 7.2 \text{ mm}$, $I_z = 355050.53 \text{ cm}^4$

maximum/minimum stresses: $\sigma_o = -252.3 \text{ N/mm}^2$, $\sigma_u = 302.2 \text{ N/mm}^2$, $\tau = 76.4 \text{ N/mm}^2$

section class: 4 $\Rightarrow$ verification of plate buckling required !!

plate buckling

effective cross-sectional area for $N_{Ed} = 4000.0 \text{ kN}$, $M_{Ed} = 0$

flange top:

section class 3 for $8.14 < c/t = 9.81 < 11.20$

effective width $b_{c,eff} = b = 392.5 \text{ mm}$

flange bottom:

section class 3 for $8.14 < c/t = 9.81 < 11.20$

effective width $b_{c,eff} = b = 392.5 \text{ mm}$

web:

single buckling field 1:

section class 4 for $34.17 < c/t = 165.83$

critical buckling stress $\sigma_{cr,p} = k_{\sigma} \cdot \sigma_E = 27.6 \text{ N/mm}^2$, $\sigma_E = 6.9 \text{ N/mm}^2$, $k_{\sigma} = 4.00$

buckling slenderness ratio $\lambda_p = (f_y / \sigma_{cr,p})^{1/2} = 3.586$

reduction factor $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.262 \leq 1$ for $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$, $\psi = 1.000$

effective width $b_{c,eff} = \rho \cdot b = 651.1 \text{ mm}$ ($b_{e1} = 325.6 \text{ mm}$, $b_{e2} = 325.6 \text{ mm}$)

single buckling field 2:

section class 3 for $30.92 < c/t = 32.50 < 34.17$

effective width $b_{c,eff} = b = 487.5 \text{ mm}$ ($b_{e1} = 243.8 \text{ mm}$, $b_{e2} = 243.8 \text{ mm}$)

overall buckling field, stiffener 1:

EC 3-1-5, appendix A.2.2 (fictitious member with elastic bedding):

critical buckling stress $\sigma_{cr,p} = \sigma_{cr,p,sl} \cdot \sigma_1 / \sigma_{sl} = 958.8 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.000$, $\sigma_{cr,p,sl} = 958.8 \text{ N/mm}^2$

buckling slenderness ratio $\lambda_p = (\beta_A \cdot f_y / \sigma_{cr,p})^{1/2} = 0.440$, $\beta_A = A_{sl,eff} / A_{sl} = 0.524$

reduction factor $\rho = 1$ for $\lambda_p < 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$, $\psi = 1.000$

critical buckling stress $\sigma_{cr,c} = \sigma_{cr,c,sl} \cdot \sigma_1 / \sigma_{sl} = 947.1 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.000$, $\sigma_{cr,c,sl} = 947.1 \text{ N/mm}^2$

buckling slenderness ratio $\lambda_c = (\beta_A \cdot f_y / \sigma_{cr,c})^{1/2} = 0.443$, $\beta_A = A_{sl,eff} / A_{sl} = 0.524$

reduction factor $\chi_c = 0.844 \leq 1$ for $\lambda_c > 0.2$

final reduction factor $\rho = (\rho - \chi_c) \cdot \xi \cdot (2 - \xi) + \chi_c = 0.848$ with $\xi = 0.012$

effective widths of adjacent buckling fields $b_{1,e2,eff} = \rho \cdot b_{1,c,eff} = 275.9 \text{ mm}$, $b_{2,e1,eff} = \rho \cdot b_{2,c,eff} = 206.6 \text{ mm}$

effective area of stiffener $A_{sl,eff} = \rho \cdot A_{st} = 52.97 \text{ cm}^2$

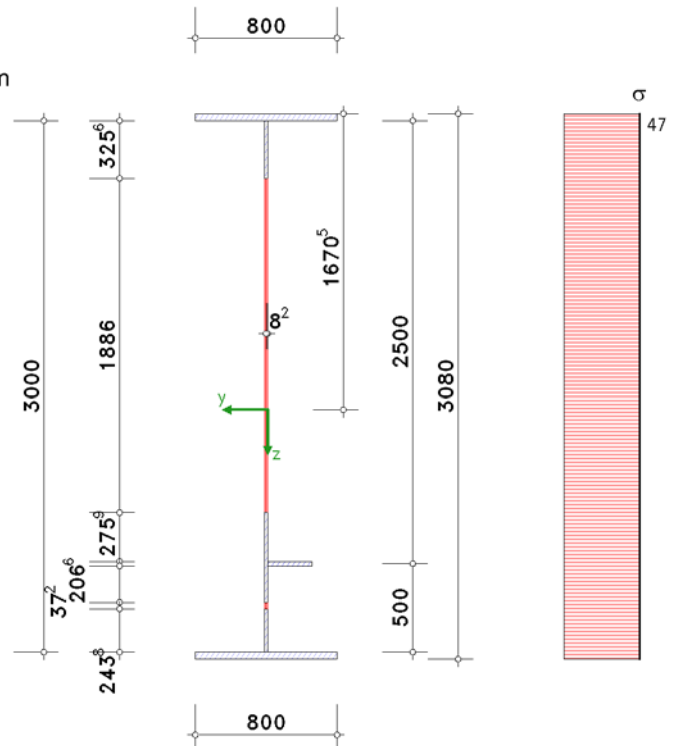
limit loads referring to the reduced cross-section:

distance of centroid from top $z_{s,eff} = 1670.5 \text{ mm}$

differential moment by $\Delta z_s = 76.3 \text{ mm}$: $\Delta M_{Ed} = 305.22 \text{ kNm}$

cross-sectional area $A_{eff} = 854.49 \text{ cm}^2$

load capacities $N_{Rd} = (f_y \cdot A_{eff}) / \gamma_{M1} = 27576.68 \text{ kN}$



effective section modulus for $M_{Ed} = 33760.0 \text{ kNm}$, $N_{Ed} = 0$

flange top:

effective width $b_{t,eff} = b = 392.5 \text{ mm}$

flange bottom:

section class 3 for $8.14 < c/t = 9.81 < 11.20$

effective width $b_{c,eff} = b = 392.5 \text{ mm}$

web:

single buckling field 1:

section class 3 for $\alpha = 0.375$ and $90.00 < c/t = 165.83 < 173.51$

effective width $b_{c,eff} = (\rho \cdot b) / (1 - \psi) = 933.3 \text{ mm}$ ($b_{e1} = 373.3 \text{ mm}$, $b_{e2} = 560.0 \text{ mm}$), $b_{t,eff} = 1554.2 \text{ mm}$, $\psi = -1.665$

single buckling field 2:

section class 3 for $30.92 < c/t = 32.50 < 38.50$

effective width $b_{c,eff} = b = 487.5 \text{ mm}$ ($b_{e1} = 224.8 \text{ mm}$, $b_{e2} = 262.7 \text{ mm}$)

overall buckling field, stiffener 1:

EC 3-1-5, appendix A.2.2 (fictitious member with elastic bedding):

critical buckling stress $\sigma_{cr,p} = \sigma_{cr,p,sl} \cdot \sigma_1 / \sigma_{sl} = 2210.9 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.529$, $\sigma_{cr,p,sl} = 1446.3 \text{ N/mm}^2$

buckling slenderness ratio $\lambda_p = (\beta_A \cdot f_y / \sigma_{cr,p})^{1/2} = 0.401$, $\beta_A = A_{sl,eff} / A_{sl} = 1.000$

reduction factor $\rho = 1$ for $\lambda_p < 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.880$, $\psi = -1.075$

critical buckling stress $\sigma_{cr,c} = \sigma_{cr,c,sl} \cdot \sigma_1 / \sigma_{sl} = 2178.6 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.529$, $\sigma_{cr,c,sl} = 1425.2 \text{ N/mm}^2$

buckling slenderness ratio $\lambda_c = (\beta_A \cdot f_y / \sigma_{cr,c})^{1/2} = 0.404$, $\beta_A = A_{sl,eff} / A_{sl} = 1.000$

reduction factor $\chi_c = 0.878 \leq 1$ for $\lambda_c > 0.2$

final reduction factor $\rho = (\rho \cdot \chi_c) \cdot \xi \cdot (2 - \xi) + \chi_c = 0.882$ with $\xi = 0.015$

effective widths of adjacent buckling fields $b_{1,e2,eff} = \rho \cdot b_{1,c,eff} = 329.2 \text{ mm}$, $b_{2,e1,eff} = \rho \cdot b_{2,c,eff} = 231.7 \text{ mm}$

effective area of stiffener $A_{sl,eff} = \rho \cdot A_{st} = 55.12 \text{ cm}^2$

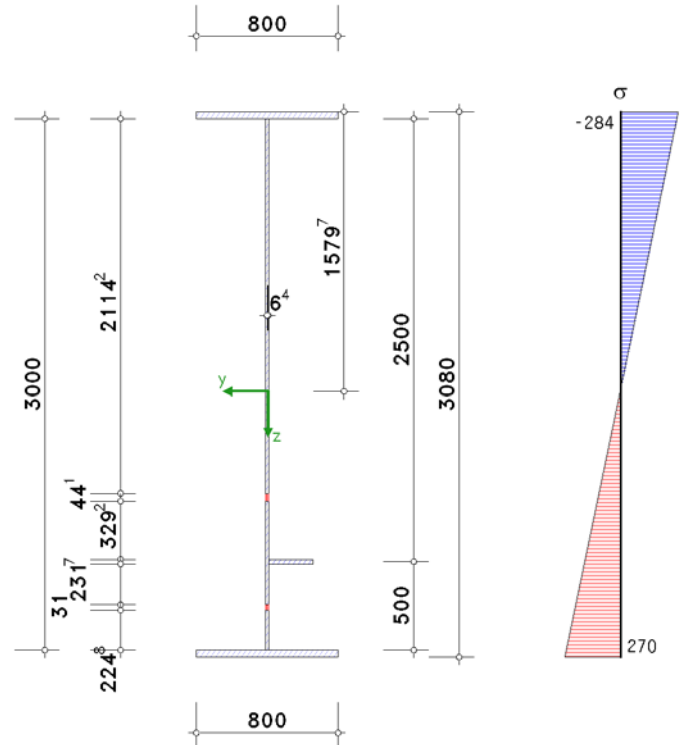
limit loads referring to the reduced cross-section:

distance of centroid from top $z_{s,eff} = 1579.7 \text{ mm}$

second moment of area $I_{y,eff} = 18595061.34 \text{ cm}^4$

section modulus $W_{y,eff} = 125619.21 \text{ cm}^3$

load capacities $M_{Rd} = (f_y \cdot W_{eff}) / \gamma_{M1} = 40540.74 \text{ kNm}$



verification (M-N-interaction)

acting moment $M_{Ed}' = M_{Ed} - \Delta M_{Ed} = 33454.78 \text{ kNm}$

$I N_{Ed} / N_{Rd} + I M_{Ed}' / M_{Rd,u} = 0.145 + 0.825 = 0.970 < 1$ ok.

shear buckling

single buckling field 1:

shear buckling: $h_w / t_w = 166.67 > 72 \cdot \epsilon / \eta = 48.82 \Rightarrow$ particular verification is required !!

buckling factor of shear for $a / h_w = 1.20 > 1$: $k_\tau = 5.34 + 4 / (a / h_w)^2 = 8.12$

critical buckling stress of shear $\tau_{cr,p} = k_\tau \cdot \sigma_E = 55.5 \text{ N/mm}^2$, $\sigma_E = 6.8 \text{ N/mm}^2$

modified slenderness $\lambda_w = 0.76 \cdot (f_y / \tau_{cr,p}) = 1.923$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.522$ for $\lambda_w \geq 1.08$

resistance $V_{bw,Rd} = (\chi_w \cdot f_y \cdot h_w \cdot t_w) / (3^{1/2} \cdot \gamma_{M1}) = 4379.87 \text{ kN}$

design value of resistance $V_{b,Rd} = V_{bw,Rd} = 4379.9 \text{ kN}$

single buckling field 2:

shear buckling: $h_w / t_w = 33.33 \leq 72 \cdot \epsilon / \eta = 48.82$ ok.

overall buckling field:

shear buckling: $h_w / t_w = 200.00 > 31 \cdot \epsilon \cdot k_\tau^{1/2} / \eta = 85.14$, $k_\tau = 16.41 \Rightarrow$ particular verification is required !!

contribution of the flanges:

resisting moment $M_{f,Rd} = f_{N,f} \cdot M_{f,k} / \gamma_{M0} = 28454.4 \text{ kNm}$, $M_{f,k} = 34534.4 \text{ kNm}$, $f_{N,f} = 0.82$

$M_{Ed} \geq M_{f,Rd}$: flanges fully exploited, resistance $V_{bf,Rd} = 0$

contribution of the web:

buckling factor of shear for $a / h_w = 1.00 < 3$: $k_\tau = 4.1 + (6.3 + 0.18 \cdot |s| / (h_w \cdot t_w^3)) / (a / h_w)^2 + 2.2 \cdot (|s| / (h_w \cdot t_w^3))^{1/3} = 16.41$

critical buckling stress of shear $\tau_{cr,p} = k_\tau \cdot \sigma_E = 77.9 \text{ N/mm}^2$, $\sigma_E = 4.7 \text{ N/mm}^2$

modified slenderness $\lambda_w = 0.76 \cdot (f_y / \tau_{cr,p}) = 1.623$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.590$ for $\lambda_w \geq 1.08$

resistance $V_{bw,Rd} = (\gamma_w \cdot f_y \cdot h_w \cdot t_w) / (3^{1/2} \cdot \gamma_{M1}) = 4945.45 \text{ kN}$
 design value of resistance $V_{b,Rd} = V_{bw,Rd} = 4945.4 \text{ kN}$
 load capacities $V_{b,Rd,min} = 4379.9 \text{ kN}$, $V_{bw,Rd,min} = 4379.9 \text{ kN}$
 verification: $V_{Ed}/V_{b,Rd,min} = 0.785 < 1$ **ok.**

interaction between shear, internal moment and axial force

utilization due to shear buckling of the web $\eta_3 = V_{Ed}/V_{bw,Rd,min} = 0.785 > 0.5$
 utilization due to plate buckling $\eta_1 = M_{Ed}/M_{pl,Rd} = 0.696 > \eta_{1,lim} = M_{f,Rd}/M_{pl,Rd} = 0.587$
 with $M_{pl,Rd} = 48493.1 \text{ kNm}$, $M_{f,Rd} = 28454.4 \text{ kNm}$
 verification: $\eta_1 + (1 - \eta_{1,lim}) \cdot (2 \cdot \eta_3 - 1)^2 = 0.830 < 1$ **ok.**

total utilization: $U = 0.970 < 1$ **ok.**

Lk 2: M-N-V-interaction (chap. 5.1.5)

method of effective cross-sectional area

EC 3-convention, compressive stresses positive

shear distortions are ignored.

cross-sectional properties: $A = 1152.50 \text{ cm}^2$, $z_s = 1594.2 \text{ mm}$, $I_y = 18753552.18 \text{ cm}^4$, $y_s = 7.2 \text{ mm}$, $I_z = 355050.53 \text{ cm}^4$
 maximum/minimum stresses: $\sigma_o = -238.6 \text{ N/mm}^2$, $\sigma_u = 289.4 \text{ N/mm}^2$, $\tau = 73.1 \text{ N/mm}^2$
 section class: 4 $\Rightarrow$ verification of plate buckling required **!!**

plate buckling

effective cross-sectional area for $N_{Ed} = 4000.0 \text{ kN}$, $M_{Ed} = 0$

flange top:

section class 3 for $8.14 < c/t = 9.81 < 11.20$
 effective width $b_{c,eff} = b = 392.5 \text{ mm}$

flange bottom:

section class 3 for $8.14 < c/t = 9.81 < 11.20$
 effective width $b_{c,eff} = b = 392.5 \text{ mm}$

web:

single buckling field 1:

section class 4 for $34.17 < c/t = 165.83$
 critical buckling stress $\sigma_{cr,p} = k_\sigma \cdot \sigma_E = 27.6 \text{ N/mm}^2$, $\sigma_E = 6.9 \text{ N/mm}^2$, $k_\sigma = 4.00$
 buckling slenderness ratio $\lambda_p = (f_y / \sigma_{cr,p})^{1/2} = 3.586$
 reduction factor $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.262 \leq 1$ for $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$, $\psi = 1.000$
 effective width $b_{c,eff} = \rho \cdot b = 651.1 \text{ mm}$ ($b_{e1} = 325.6 \text{ mm}$, $b_{e2} = 325.6 \text{ mm}$)

single buckling field 2:

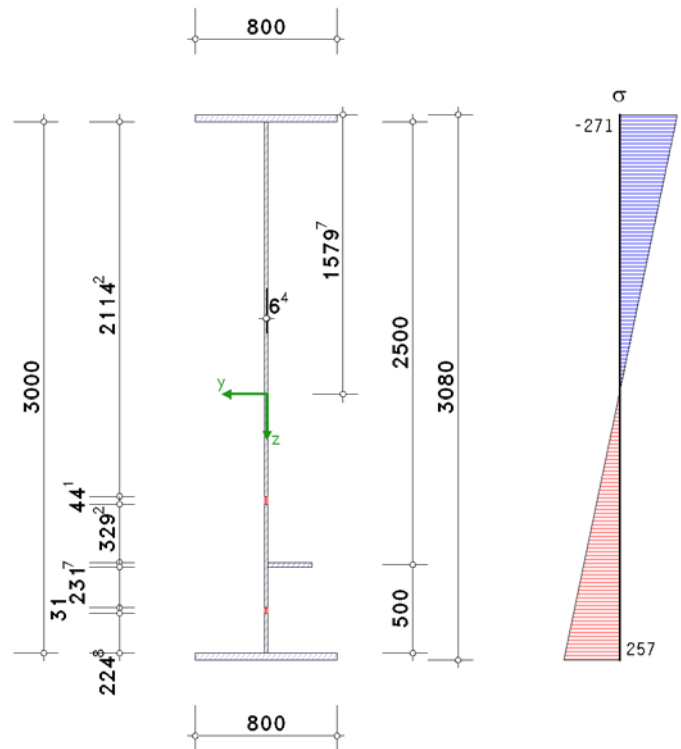
section class 3 for $30.92 < c/t = 32.50 < 34.17$
 effective width $b_{c,eff} = b = 487.5 \text{ mm}$ ($b_{e1} = 243.8 \text{ mm}$, $b_{e2} = 243.8 \text{ mm}$)

overall buckling field, stiffener 1:

EC 3-1-5, appendix A.2.2 (fictitious member with elastic bedding):
 critical buckling stress $\sigma_{cr,p} = \sigma_{cr,p,sl} \cdot \sigma_1 / \sigma_{sl} = 958.8 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.000$, $\sigma_{cr,p,sl} = 958.8 \text{ N/mm}^2$
 buckling slenderness ratio $\lambda_p = (\beta_A \cdot f_y / \sigma_{cr,p})^{1/2} = 0.440$, $\beta_A = A_{sl,eff} / A_{sl} = 0.524$
 reduction factor $\rho = 1$ for $\lambda_p < 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.673$, $\psi = 1.000$
 critical buckling stress $\sigma_{cr,c} = \sigma_{cr,c,sl} \cdot \sigma_1 / \sigma_{sl} = 947.1 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.000$, $\sigma_{cr,c,sl} = 947.1 \text{ N/mm}^2$
 buckling slenderness ratio $\lambda_c = (\beta_A \cdot f_y / \sigma_{cr,c})^{1/2} = 0.443$, $\beta_A = A_{sl,eff} / A_{sl} = 0.524$
 reduction factor $\chi_c = 0.844 \leq 1$ for $\lambda_c > 0.2$
 final reduction factor $\rho = (\rho \cdot \chi_c) \cdot \xi \cdot (2 - \xi) + \chi_c = 0.848$ with $\xi = 0.012$
 effective widths of adjacent buckling fields $b_{1,e2,eff} = \rho \cdot b_{1,c,eff} = 275.9 \text{ mm}$, $b_{2,e1,eff} = \rho \cdot b_{2,c,eff} = 206.6 \text{ mm}$
 effective area of stiffener $A_{sl,eff} = \rho \cdot A_{st} = 52.97 \text{ cm}^2$

limit loads referring to the reduced cross-section:

distance of centroid from top $z_{s,eff} = 1670.5 \text{ mm}$
 differential moment by $\Delta z_s = 76.3 \text{ mm}$: $\Delta M_{Ed} = 305.22 \text{ kNm}$
 cross-sectional area $A_{eff} = 854.49 \text{ cm}^2$
 load capacities $N_{Rd} = (f_y \cdot A_{eff}) / \gamma_{M1} = 27576.68 \text{ kN}$



verification (M-N-interaction)

acting moment $M_{Ed}' = M_{Ed} - \Delta M_{Ed} = 31844.78 \text{ kNm}$

$IN_{Ed}/N_{Rd} + IM_{Ed}'/M_{Rd,u} = 0.145 + 0.786 = 0.931 < 1$ **ok.**

shear buckling

single buckling field 1:

shear buckling: $h_w/t_w = 166.67 > 72 \cdot \epsilon / \eta = 48.82 \Rightarrow$ particular verification is required !!

buckling factor of shear for $a/h_w = 1.20 > 1$: $k_\tau = 5.34 + 4/(a/h_w)^2 = 8.12$

critical buckling stress of shear $\tau_{cr,p} = k_\tau \cdot \sigma_E = 55.5 \text{ N/mm}^2$, $\sigma_E = 6.8 \text{ N/mm}^2$

modified slenderness $\lambda_w = 0.76 \cdot (f_y / \tau_{cr,p}) = 1.923$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.522$ for $\lambda_w \geq 1.08$

resistance $V_{bw,Rd} = (\chi_w \cdot f_y \cdot h_w \cdot t_w) / (3^{1/2} \cdot \gamma_{M1}) = 4379.87 \text{ kN}$

design value of resistance $V_{b,Rd} = V_{bw,Rd} = 4379.9 \text{ kN}$

single buckling field 2:

shear buckling: $h_w/t_w = 33.33 \leq 72 \cdot \epsilon / \eta = 48.82$ **ok.**

overall buckling field:

shear buckling: $h_w/t_w = 200.00 > 31 \cdot \epsilon \cdot k_\tau^{1/2} / \eta = 85.14$, $k_\tau = 16.41 \Rightarrow$ particular verification is required !!

contribution of the flanges:

resisting moment $M_{f,Rd} = f_{N,f} \cdot M_{f,k} / \gamma_{M0} = 28454.4 \text{ kNm}$, $M_{f,k} = 34534.4 \text{ kNm}$, $f_{N,f} = 0.82$

$M_{Ed} \geq M_{f,Rd}$: flanges fully exploited, resistance $V_{bf,Rd} = 0$

contribution of the web:

buckling factor of shear for $a/h_w = 1.00 < 3$: $k_\tau = 4.1 + (6.3 + 0.18 \cdot |s| / (h_w \cdot t_w^3)) / (a/h_w)^2 + 2.2 \cdot (|s| / (h_w \cdot t_w^3))^{1/3} = 16.41$

critical buckling stress of shear $\tau_{cr,p} = k_\tau \cdot \sigma_E = 77.9 \text{ N/mm}^2$, $\sigma_E = 4.7 \text{ N/mm}^2$

modified slenderness $\lambda_w = 0.76 \cdot (f_y / \tau_{cr,p}) = 1.623$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.590$ for $\lambda_w \geq 1.08$

resistance $V_{bw,Rd} = (\chi_w \cdot f_y \cdot h_w \cdot t_w) / (3^{1/2} \cdot \gamma_{M1}) = 4945.45 \text{ kN}$

design value of resistance $V_{b,Rd} = V_{bw,Rd} = 4945.4 \text{ kN}$

load capacities $V_{b,Rd,min} = 4379.9 \text{ kN}$, $V_{bw,Rd,min} = 4379.9 \text{ kN}$

verification: $V_{Ed}/V_{b,Rd,min} = 0.751 < 1$ **ok.**

interaction between shear, internal moment and axial force

utilization due to shear buckling of the web $\eta_3 = V_{Ed}/V_{bw,Rd,min} = 0.751 > 0.5$

utilization due to plate buckling $\eta_1 = M_{Ed}/M_{pl,Rd} = 0.663 > \eta_{1,lim} = M_{f,Rd}/M_{pl,Rd} = 0.587$

with $M_{pl,Rd} = 48493.1 \text{ kNm}$, $M_{f,Rd} = 28454.4 \text{ kNm}$

verification: $\eta_1 + (1 - \eta_{1,lim}) \cdot (2 \cdot \eta_3 - 1)^2 = 0.767 < 1$ **ok.**

total utilization: $U = 0.931 < 1$ **ok.**

Final Result

maximum utilization [Lk 1]: $\max U = 0.970 < 1$ **ok.**

verifications succeeded

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;
Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010
DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -
Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;
Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010
DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-5, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -
Teil 1-5: Plattenförmige Bauteile;
Deutsche Fassung EN 1993-1-5:2006 + AC:2009, Ausgabe Dezember 2010
DIN EN 1993-1-5/NA, Nationaler Anhang zur DIN EN 1993-1-5, Ausgabe Dezember 2010