

detailed problems acc. to Eurocode 3

EC 3-1-5 (12.10), NA: Deutschland

steel grade

steel grade S 355

cross-section

beam: parameter (I-section):

$h = 3080.0 \text{ mm}$, $t_w = 15.0 \text{ mm}$, $b_f = 800.0 \text{ mm}$, $t_f = 40.0 \text{ mm}$

longitudinal stiffeners: number $n_{st} = 1$

section parameters (flat steel):

$h = 250.0 \text{ mm}$, $t = 25.0 \text{ mm}$

distance of stiffener to the top edge of beam $d_{st,0} = 2540.0 \text{ mm}$

parameters

length of buckling field $a = 300.0 \text{ cm}$

method of reduced stresses

rigid support stiffener

verification at intermediate support

calculation of buckling factors with 4H-tool

loading

internal forces and moments referring to the stiffened cross-section:

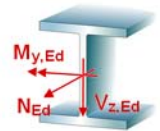
LK 1: method of reduced stresses (chap. 10)

$N_{Ed} = -4000.0 \text{ kN}$ $M_{Ed} = -32750.0 \text{ kNm}$ $V_{Ed} = 3288.0 \text{ kN}$

partial safety factors for material

resistance of cross-sections $\gamma_{M0} = 1.00$

resistance of members in stability failure $\gamma_{M1} = 1.10$



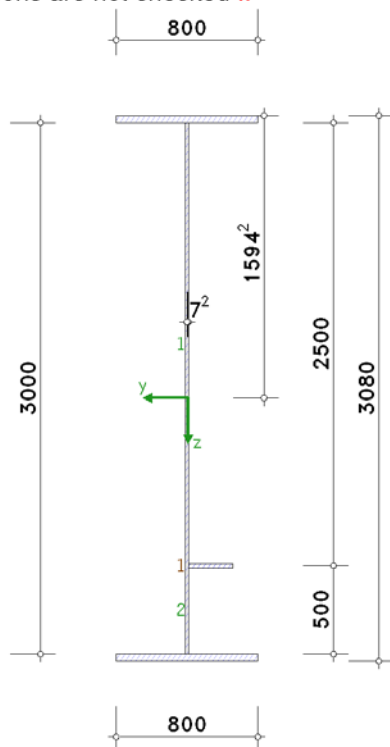
verifications of buckling resistance

assumption: flange induced web buckling is excluded.

assumption: local buckling of stiffeners is excluded.

assumption: plate area is supported rigidly.

the assumptions are not checked !!



method of reduced stresses

EC 3-convention, compressive stresses positive

shear distortions are ignored.

cross-sectional properties: $A = 1152.50 \text{ cm}^2$, $z_s = 1594.2 \text{ mm}$, $I_y = 18753552.18 \text{ cm}^4$, $y_s = 7.2 \text{ mm}$, $I_z = 355050.53 \text{ cm}^4$

maximum/minimum stresses: $\sigma_o = -243.7 \text{ N/mm}^2$, $\sigma_u = 294.2 \text{ N/mm}^2$, $\tau = 73.1 \text{ N/mm}^2$

section class: 4 $\Rightarrow$ verification of buckling resistance required !!

buckling factors (4H-tool)

web: $\alpha_{cr} = 0.838$, $\alpha_{cr,1} = 0.621$, $\alpha_{cr,2} = 2.688$

reduced stresses

flange top:

buckling stresses $\sigma_{Ed} = -240.2 \text{ N/mm}^2 \leq 0 \Rightarrow$ verification not required

flange bottom:

$\sigma_{Ed} = 290.7 \text{ N/mm}^2$

non-dimensional slenderness ratio $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.646$, $\alpha_{ult} = 1.221$, $\alpha_{cr} = 2.925$

reduction factor $\rho = 1$ for $\lambda_p < 0.748$, $\psi = 1.000$

ultimate buckling stress $\sigma_{Rd} = \rho \cdot f_y / \gamma_{M1} = 322.7 \text{ N/mm}^2$

verification: $\sigma_{Ed}/\sigma_{Rd} = 0.901 < 1$ **ok.**

web:

single buckling field 1:

$\sigma_{Ed} = 236.7 \text{ N/mm}^2$, $\tau_{Ed} = 73.1 \text{ N/mm}^2$

non-dimensional slenderness ratio $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 1.459$, $\alpha_{ult} = 1.323$, $\alpha_{cr} = 0.621$ (4H-tool)

reduction factor $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.638 \leq 1$ for $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.887$, $\psi = -1.184$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.635$ for $\lambda_w \geq 1.08$

ultimate buckling stresses $\sigma_{Rd} = \rho \cdot f_y / \gamma_{M1} = 206.1 \text{ N/mm}^2$, $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma_{M1}) = 118.2 \text{ N/mm}^2$

verification: $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 1.304 > 1$ **not ok. !!**

single buckling field 2:

$\sigma_{Ed} = 287.2 \text{ N/mm}^2$, $\tau_{Ed} = 73.1 \text{ N/mm}^2$

non-dimensional slenderness ratio $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 0.649$, $\alpha_{ult} = 1.131$, $\alpha_{cr} = 2.688$ (4H-tool)

reduction factor $\rho = 1$ for $\lambda_p < 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.716$, $\psi = 0.696$

reduction factor $\chi_w = 1.200 = \eta$ for $\lambda_w < 0.83/\eta = 0.692$

ultimate buckling stresses $\sigma_{Rd} = \rho \cdot f_y / \gamma_{M1} = 322.7 \text{ N/mm}^2$, $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma_{M1}) = 223.6 \text{ N/mm}^2$

verification: $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 0.948 < 1$ **ok.**

overall buckling field:

$\sigma_{Ed} = 287.2 \text{ N/mm}^2$, $\tau_{Ed} = 73.1 \text{ N/mm}^2$

non-dimensional slenderness ratio $\lambda_p = \lambda_c = \lambda_w = (\alpha_{ult}/\alpha_{cr})^{1/2} = 1.162$, $\alpha_{ult} = 1.131$, $\alpha_{cr} = 0.838$ (4H-tool)

reduction factor $\rho = (\lambda_p - 0.055 \cdot (3 + \psi)) / \lambda_p^2 = 0.772 \leq 1$ for $\lambda_p > 0.5 + (0.085 - 0.055 \cdot \psi)^{1/2} = 0.861$, $\psi = -0.824$

critical buckling stress $\sigma_{cr,p} = \alpha_{cr} \cdot \sigma_{Ed} = 240.8 \text{ N/mm}^2$, $\sigma_{Ed} = 287.2 \text{ N/mm}^2$

critical buckling stress $\sigma_{cr,c} = \sigma_{cr,c,sl} \cdot \sigma_1 / \sigma_{sl} = 1978.8 \text{ N/mm}^2$, $\sigma_1 / \sigma_{sl} = 1.437$, $\sigma_{cr,c,sl} = 1377.2 \text{ N/mm}^2$

reduction factor $\chi_c = 0.428 \leq 1$ for $\lambda_c > 0.2$

final reduction factor $\rho = (\rho - \chi_c) \cdot \xi \cdot (2 - \xi) + \chi_c = 0.428$ with $\xi = 0.000$

reduction factor $\chi_w = 1.37 / (0.7 + \lambda_w) = 0.736$ for $\lambda_w \geq 1.08$

ultimate buckling stresses $\sigma_{Rd} = \rho \cdot f_y / \gamma_{M1} = 138.1 \text{ N/mm}^2$, $\tau_{Rd} = \chi_w \cdot f_y / (3^{1/2} \cdot \gamma_{M1}) = 137.1 \text{ N/mm}^2$

verification: $((\sigma_{Ed}/\sigma_{Rd})^2 + (\tau_{Ed}/\tau_{Rd})^2)^{1/2} = 2.147 > 1$ **not ok. !!**

total utilization: $U = 2.147 > 1$ **not ok. !!**

Final Result

maximum utilization: $\max U = 2.147 > 1$ **not ok. !!**

design resistance not ensured !!

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-5, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-5: Plattenförmige Bauteile;

