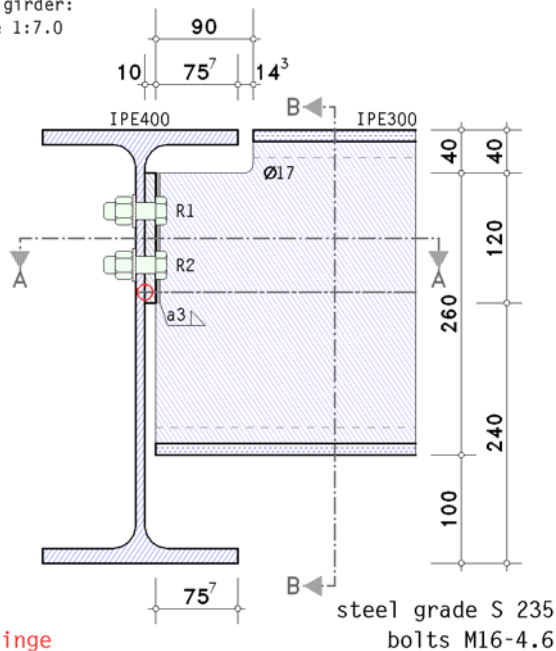


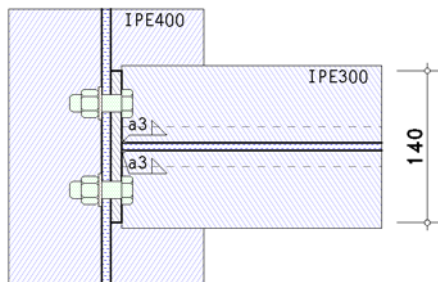
Simple Joint of Beams

EC 3-1-8 (12.10), NA: Deutschland

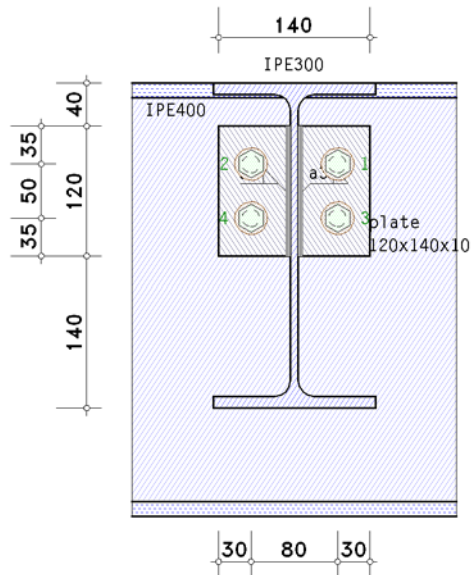
main girder:
scale 1:7.0



○ hinge
section A-A:



section B-B:



beam connection with end-plate, connected to the web of the main girder

steel grade

steel grade S 235

bolts

bolt: bolt class 4.6, bolt size M16

shear plane passes through the unthreaded portion of the bolt

geometry

main girder

section IPE400

supported beam

section IPE300

joint configuration

end-plate: thickness $t_p = 10.0$ mm, length $l_p = 120.0$ mm, width $b_p = 140.0$ mm

plate lengths: $h_o = 0.0$ mm, $ü_o = 40.0$ mm ($h_u = 100.0$ mm, $ü_u = 140.0$ mm)

notch: $a_o = 90.0$ mm, $e_o = 40.0$ mm

rounded notch (root radius $r_a = 8.5$ mm)

distances between bolts at main girder: $e_{z,0} = 35.0$ mm, $p_{z,1-2} = 50.0$ mm, $e_{x,0} = 30.0$ mm

thickness weld: $a_w = 3.0$ mm

design resistance

verification of welds with the simplified method

elastic cross-sectional check der supported beam

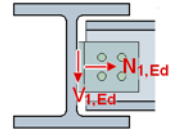
internal forces and moments

Lk 1: $V_{1,Ed} = 75.00 \text{ kN}$

partial safety factors for material

resistance of cross sections $\gamma_{M0} = 1.00$

resistance of bolts, welds, plates in bearing $\gamma_{M2} = 1.25$



Simple Joint of Beams

distance of bolt rows at main girder (right)

edge dist.:	$e_2 = 30.0 \text{ mm} > 1.2 \cdot d_0 = 21.6 \text{ mm}$,	$e_2 = 30.0 \text{ mm} < 4 \cdot t_{\min} + 40 \text{ mm} = 74.4 \text{ mm}$
pitch:	$p_2 = 80.0 \text{ mm} > 2.4 \cdot d_0 = 43.2 \text{ mm}$,	$p_2 = 80.0 \text{ mm} < \min(14 \cdot t_{\min}, 200 \text{ mm}) = 120.4 \text{ mm}$
edge dist.:	$e_1 = 35.0 \text{ mm} > 1.2 \cdot d_0 = 21.6 \text{ mm}$,	$e_1 = 35.0 \text{ mm} < 4 \cdot t_1 + 40 \text{ mm} = 74.4 \text{ mm}$
pitch:	$p_1 = 50.0 \text{ mm} > 2.2 \cdot d_0 = 39.6 \text{ mm}$,	$p_1 = 50.0 \text{ mm} < \min(14 \cdot t_{\min}, 200 \text{ mm}) = 120.4 \text{ mm}$
edge dist.:	$e_1 = 35.0 \text{ mm} > 1.2 \cdot d_0 = 21.6 \text{ mm}$,	$e_1 = 35.0 \text{ mm} < 4 \cdot t_1 + 40 \text{ mm} = 74.4 \text{ mm}$

assumption: hinge is in the periphery to main girder web

Lk 1:

design values

transformation of member forces to the reference point (intersection point of beam axis')

$M_{1,Ed} = V_{j1,Ed} \cdot e_1 = -0.32 \text{ kNm}$, $e_1 = -4.3 \text{ mm}$

$V_{1,Ed} = V_{j1,Ed} = 75.00 \text{ kN}$

design resistance of the connection

calculation of the point section:

bolt 1 $T_1 = T_{z,1} = 18.75 \text{ kN}$

bolt 2 $T_2 = T_{z,2} = 18.75 \text{ kN}$

bolt 3 $T_3 = T_{z,3} = 18.75 \text{ kN}$

bolt 4 $T_4 = T_{z,4} = 18.75 \text{ kN}$

shear force resistance

bolts in shear:

$U_i = T_i / F_{v,Rd}$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

design shear resistance per shear plane: $F_{v,Rd} = \alpha_v \cdot f_{ub} \cdot A / \gamma_{M2} = 38.60 \text{ kN}$, $\alpha_v = 0.60$

bolt 1: $U_1 = 0.486$ $V_{Rd,1} = 154.4 \text{ kN}$

bolt 2: $U_2 = 0.486$ $V_{Rd,2} = 154.4 \text{ kN}$

bolt 3: $U_3 = 0.486$ $V_{Rd,3} = 154.4 \text{ kN}$

bolt 4: $U_4 = 0.486$ $V_{Rd,4} = 154.4 \text{ kN}$

design shear resistance total: $V_{Rd,1} = 154.4 \text{ kN}$

end-plate with bearing resistance:

$U_{z,i} = T_{z,i} / F_{b,z,Rd}$, $U_{y,i} = T_{y,i} / F_{b,y,Rd}$, $U_i = \max(U_{z,i}, U_{y,i})$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

bolt 1: $F_{b,z,1} = 74.67 \text{ kN}$ $U_1 = 0.251$ $V_{Rd,1} = 298.7 \text{ kN}$

bolt 2: $F_{b,z,2} = 74.67 \text{ kN}$ $U_2 = 0.251$ $V_{Rd,2} = 298.7 \text{ kN}$

bolt 3: $F_{b,z,3} = 74.67 \text{ kN}$ $U_3 = 0.251$ $V_{Rd,3} = 298.7 \text{ kN}$

bolt 4: $F_{b,z,4} = 74.67 \text{ kN}$ $U_4 = 0.251$ $V_{Rd,4} = 298.7 \text{ kN}$

design bearing resistance total: $V_{Rd,2} = 298.7 \text{ kN}$

beam web with bearing resistance:

$U_{z,i} = T_{z,i} / F_{b,z,Rd}$, $U_{y,i} = T_{y,i} / F_{b,y,Rd}$, $U_i = \max(U_{z,i}, U_{y,i})$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

bolt 1: $F_{b,z,1} = 66.97 \text{ kN}$ $U_1 = 0.280$ $V_{Rd,1} = 267.9 \text{ kN}$

bolt 2: $F_{b,z,2} = 66.97 \text{ kN}$ $U_2 = 0.280$ $V_{Rd,2} = 267.9 \text{ kN}$

bolt 3: $F_{b,z,3} = 66.97 \text{ kN}$ $U_3 = 0.280$ $V_{Rd,3} = 267.9 \text{ kN}$

bolt 4: $F_{b,z,4} = 66.97 \text{ kN}$ $U_4 = 0.280$ $V_{Rd,4} = 267.9 \text{ kN}$

design bearing resistance total: $V_{Rd,3} = 267.9 \text{ kN}$

end-plate in tension and shear (shear block):

shear resistance $V_{eff,Rd} = (A_{nt} \cdot f_u) / \gamma_{M2} + (A_{nv} \cdot f_y / 3^{1/3}) / \gamma_{M0} = 257.25 \text{ kN}$

shear resistance total: $V_{Rd,4} = 257.3 \text{ kN}$

end-plate in bending and shear:

shear resistance $V_{Rd} = f_y / \gamma_{M0} \cdot ((b' / W_{el})^2 + 3 \cdot (1/A)^2)^{1/2} = 88.86 \text{ kN}$

shear resistance total: $V_{Rd,5} = 2 \cdot 88.86 = 177.7 \text{ kN}$

beam web with shear (next to the weld):

shear resistance $V_{Rd} = (A_v \cdot f_y) / (3^{1/2} \cdot \gamma_{M0}) = 115.60 \text{ kN}$
shear resistance total: $V_{Rd,6} = 115.6 \text{ kN}$

shear resistance: $\min V_{Rd,p} = V_{Rd,6} = 115.6 \text{ kN}$

verification of the connection

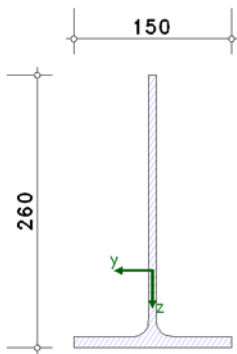
$V_{Ed} = 75.0 \text{ kN}$: $V_{Ed} / \min V_{Rd} = 0.649 < 1$ **ok.**

weld verification

$F_{w,Ed} = 3.49 \text{ kN/cm} < F_{w,Rd} = 6.24 \text{ kN/cm} \Rightarrow U_w = 0.560 < 1$ **ok.**

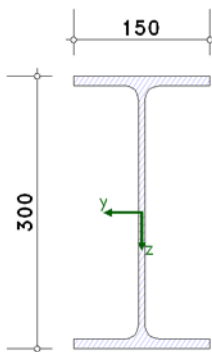
cross-sectional check of supported beam

verification at $\Delta x = 95.8 \text{ mm}$ with notch



elastic cross-sectional check for $M_{Ed} = 6.86 \text{ kNm}$, $V_{Ed} = 75.00 \text{ kN}$
elastic stresses: $\max \sigma_x = 2.16 \text{ kN/cm}^2$, $\min \sigma_x = -5.47 \text{ kN/cm}^2$, $\max \tau = 5.57 \text{ kN/cm}^2$, $\max \sigma_v = 9.64 \text{ kN/cm}^2$
utilizations: design resistance $U_\sigma = 0.410 < 1$ **ok.**

verification at $\Delta x = 104.3 \text{ mm}$



elastic cross-sectional check for $M_{Ed} = 7.50 \text{ kNm}$, $V_{Ed} = 75.00 \text{ kN}$
elastic stresses: $\max \sigma_x = 1.35 \text{ kN/cm}^2$, $\min \sigma_x = -1.35 \text{ kN/cm}^2$, $\max \tau = 3.97 \text{ kN/cm}^2$, $\max \sigma_v = 6.88 \text{ kN/cm}^2$
utilizations: design resistance $U_\sigma = 0.293 < 1$ **ok.**, c/t-ratio $U_{c/t} = 0.090 < 1$ **ok.**

verification result

maximum utilization: $\max U = 0.649 < 1$ **ok.**

Final Result

maximum utilization: design resistance $\max U = 0.649 < 1$ **ok.**
c/t-ratio $\max U = 0.090 < 1$ **ok.**

verification succeeded

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-8: Bemessung von Anschlüssen;

Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-8/NA, Nationaler Anhang zur DIN EN 1993-1-8, Ausgabe Dezember 2010

ECCS Document No. 126: European Recommendations for the Design of Simple Joints in Steel Structures.

ECCS TC10 - Structural Connections, 2009. J.P. Jaspart, J.F. Demonceau, S. Renkin, M.L. Guillaume