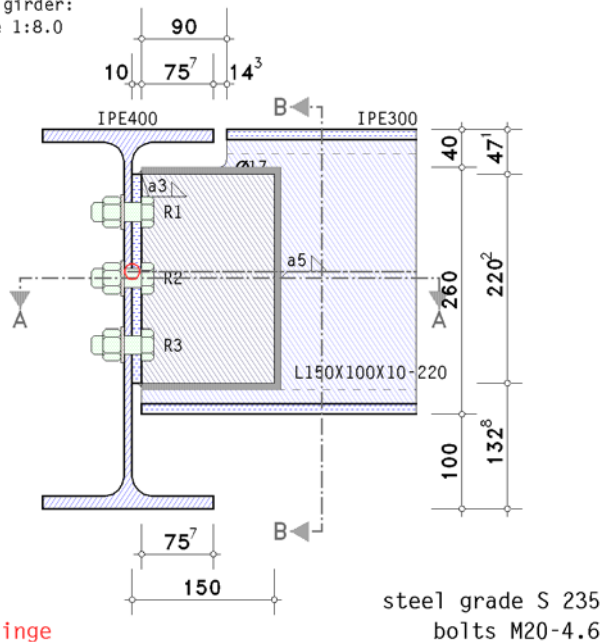


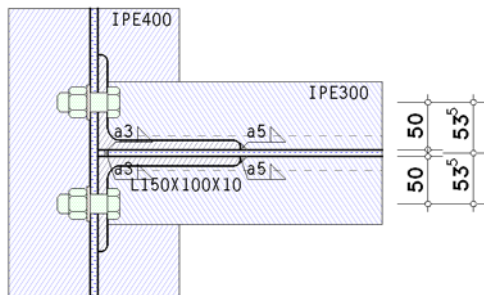
Simple Joint of Beams

EC 3-1-8 (12.10), NA: Deutschland

main girder:
scale 1:8.0



○ hinge
section A-A:



beam connection with two bolted/welded angles, connected to the web of the main girder

steel grade

steel grade S 235

bolts

bolt: bolt class 4.6, bolt size M20

shear plane passes through the unthreaded portion of the bolt

geometry

main girder

section IPE400

supported beam

section IPE300

joint configuration

2 x angle: section L150X100X10

width of angles $b_a = 220.2$ mm

plate lengths: $h_o = 0.0$ mm, $\ddot{u}_o = 47.1$ mm ($h_u = 100.0$ mm, $\ddot{u}_u = 32.8$ mm), $s = 10.0$ mm

notch: $a_o = 90.0$ mm, $e_o = 40.0$ mm

rounded notch (root radius $r_a = 8.5$ mm)

distances between bolts at main girder: $e_{z,0} = 40.0$ mm, $p_{z,1-2} = 70.0$ mm, $p_{z,2-3} = 70.0$ mm, $e_{x,0} = 50.0$ mm

thickness weld: $a_w = 5.0$ mm (at angle leg), $a_{w,s} = 3.0$ mm (end weld)

design resistance

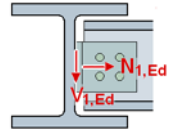
verification of welds with the simplified method

elastic cross-sectional check der supported beam

internal forces and moments

Lk 1: $V_{1,Ed} = 200.00 \text{ kN}$

Lk 2: $V_{1,Ed} = 160.00 \text{ kN}$



partial safety factors for material

resistance of cross sections $\gamma_{M0} = 1.00$

resistance of bolts, welds, plates in bearing $\gamma_{M2} = 1.25$

Simple Joint of Beams

distance of bolt rows at main girder (right)

edge dist.:	$e_2 = 50.0 \text{ mm} > 1.2 \cdot d_0 = 26.4 \text{ mm}$,	$e_2 = 50.0 \text{ mm} < 4 \cdot t_{\min} + 40 \text{ mm} = 74.4 \text{ mm}$
pitch:	$p_2 = 107.1 \text{ mm} > 2.4 \cdot d_0 = 52.8 \text{ mm}$,	$p_2 = 107.1 \text{ mm} < \min(14 \cdot t_{\min}, 200 \text{ mm}) = 120.4 \text{ mm}$
edge dist.:	$e_1 = 40.0 \text{ mm} > 1.2 \cdot d_0 = 26.4 \text{ mm}$,	$e_1 = 40.0 \text{ mm} < 4 \cdot t_1 + 40 \text{ mm} = 74.4 \text{ mm}$
pitch:	$p_1 = 70.0 \text{ mm} > 2.2 \cdot d_0 = 48.4 \text{ mm}$,	$p_1 = 70.0 \text{ mm} < \min(14 \cdot t_{\min}, 200 \text{ mm}) = 120.4 \text{ mm}$
pitch:	$p_1 = 70.0 \text{ mm} > 2.2 \cdot d_0 = 48.4 \text{ mm}$,	$p_1 = 70.0 \text{ mm} < \min(14 \cdot t_{\min}, 200 \text{ mm}) = 120.4 \text{ mm}$
edge dist.:	$e_1 = 40.2 \text{ mm} > 1.2 \cdot d_0 = 26.4 \text{ mm}$,	$e_1 = 40.2 \text{ mm} < 4 \cdot t_1 + 40 \text{ mm} = 74.4 \text{ mm}$

assumption: hinge is in the periphery to main girder web

Lk 1:

design values

transformation of member forces to the reference point (intersection point of beam axis')

$M_{1,Ed} = V_{j1,Ed} \cdot e_1 = -0.86 \text{ kNm}$, $e_1 = -4.3 \text{ mm}$

$V_{1,Ed} = V_{j1,Ed} = 200.00 \text{ kN}$

design resistance of the connection

angle leg at main girder:

compression by contact

dimensions of contact area $h_D = 20.0 \text{ mm}$, $b_D = 11.3 \text{ mm}$, compression force in contact area $D = 37.69 \text{ kN}$

check: $D / (A_D \cdot f_{yD}) = 0.712 < 1$ **ok.** $\Rightarrow$ compression by contact exists

calculation of the point section:

bolt 1 $T_{y,1} = 3.77 \text{ kN}$, $T_{z,1} = 33.33 \text{ kN}$, $T_1 = 33.55 \text{ kN}$

bolt 2 $T_{y,2} = 12.56 \text{ kN}$, $T_{z,2} = 33.33 \text{ kN}$, $T_2 = 35.62 \text{ kN}$

bolt 3 $T_{y,3} = 21.36 \text{ kN}$, $T_{z,3} = 33.33 \text{ kN}$, $T_3 = 39.59 \text{ kN}$

shear force resistance

bolts in shear:

$U_i = T_i / F_{v,Rd}$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

design shear resistance per shear plane: $F_{v,Rd} = \alpha_v \cdot f_{ub} \cdot A / \gamma_{M2} = 60.32 \text{ kN}$, $\alpha_v = 0.60$

bolt 1: $U_1 = 0.556$ $V_{Rd,1} = 359.6 \text{ kN}$

bolt 2: $U_2 = 0.591$ $V_{Rd,2} = 338.7 \text{ kN}$

bolt 3: $U_3 = 0.656$ $V_{Rd,3} = 304.7 \text{ kN}$

design shear resistance total: $V_{Rd,1} = 304.7 \text{ kN}$

angle leg 2 with bearing resistance:

$U_{z,i} = T_{z,i} / F_{b,z,Rd}$, $U_{y,i} = T_{y,i} / F_{b,y,Rd}$, $U_i = \max(U_{z,i}, U_{y,i})$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

bolt 1: $F_{b,z,1} = 87.27 \text{ kN}$ $F_{b,y,1} = 109.09 \text{ kN}$ $U_1 = 0.382$ $V_{Rd,1} = 523.6 \text{ kN}$

bolt 2: $F_{b,z,2} = 116.73 \text{ kN}$ $F_{b,y,2} = 123.84 \text{ kN}$ $U_2 = 0.286$ $V_{Rd,2} = 700.4 \text{ kN}$

bolt 3: $F_{b,z,3} = 87.62 \text{ kN}$ $F_{b,y,3} = 109.09 \text{ kN}$ $U_3 = 0.380$ $V_{Rd,3} = 525.7 \text{ kN}$

design bearing resistance total: $V_{Rd,2} = 523.6 \text{ kN}$

beam web with bearing resistance:

$U_{z,i} = T_{z,i} / F_{b,z,Rd}$, $U_{y,i} = T_{y,i} / F_{b,y,Rd}$, $U_i = \max(U_{z,i}, U_{y,i})$, $V_{Rd,i} = V_{1,Ed} / U_i$, $V_{Rd} = \min V_{Rd,i}$

bolt 1: $F_{b,z,1} = 100.39 \text{ kN}$ $F_{b,y,1} = 123.84 \text{ kN}$ $U_1 = 0.332$ $V_{Rd,1} = 602.3 \text{ kN}$

bolt 2: $F_{b,z,2} = 100.39 \text{ kN}$ $F_{b,y,2} = 123.84 \text{ kN}$ $U_2 = 0.332$ $V_{Rd,2} = 602.3 \text{ kN}$

bolt 3: $F_{b,z,3} = 100.39 \text{ kN}$ $F_{b,y,3} = 123.84 \text{ kN}$ $U_3 = 0.332$ $V_{Rd,3} = 602.3 \text{ kN}$

design bearing resistance total: $V_{Rd,3} = 602.3 \text{ kN}$

shear resistance: $\min V_{Rd,a2} = V_{Rd,1} = 304.7 \text{ kN}$

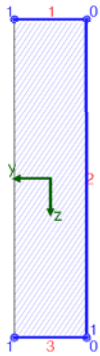
angle leg at supported beam:

s. weld verification

verification of the connection

$V_{Ed} = 200.0 \text{ kN}$: $V_{Ed} / \min V_{Rd} = 0.656 < 1$ **ok.**

weld verification



weld 1: $a_w = 5.0 \text{ mm}$ $l_w = 50.0 \text{ mm}$
weld 2: $a_w = 5.0 \text{ mm}$ $l_w = 220.2 \text{ mm}$
weld 3: $a_w = 5.0 \text{ mm}$ $l_w = 50.0 \text{ mm}$

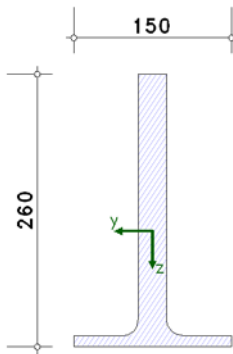
$F_{w,Ed} = 6.81 \text{ kN/cm} < F_{w,Rd} = 10.39 \text{ kN/cm} \Rightarrow U_w = 0.656 < 1$ **ok.**

end weld:

$F_{w,Ed} = 2.00 \text{ kN/cm} < F_{w,Rd} = 6.24 \text{ kN/cm} \Rightarrow U_w = 0.321 < 1$ **ok.**

cross-sectional check of supported beam

verification at $\Delta x = 95.8 \text{ mm}$ with notch

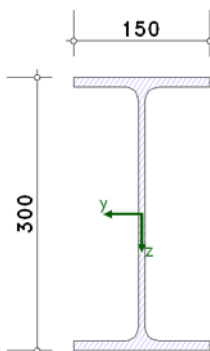


elastic cross-sectional check for $M_{Ed} = 18.30 \text{ kNm}$, $V_{Ed} = 200.00 \text{ kN}$

elastic stresses: $\max \sigma_x = 3.55 \text{ kN/cm}^2$, $\min \sigma_x = -4.81 \text{ kN/cm}^2$, $\max \tau = 3.92 \text{ kN/cm}^2$, $\max \sigma_v = 6.79 \text{ kN/cm}^2$

utilizations: design resistance $U_\sigma = 0.289 < 1$ **ok.**

verification at $\Delta x = 104.3 \text{ mm}$



elastic cross-sectional check for $M_{Ed} = 20.00 \text{ kNm}$, $V_{Ed} = 200.00 \text{ kN}$

elastic stresses: $\max \sigma_x = 3.59 \text{ kN/cm}^2$, $\min \sigma_x = -3.59 \text{ kN/cm}^2$, $\max \tau = 10.59 \text{ kN/cm}^2$, $\max \sigma_v = 18.35 \text{ kN/cm}^2$

utilizations: design resistance $U_\sigma = 0.781 < 1$ **ok.**, c/t-ratio $U_{c/t} = 0.147 < 1$ **ok.**

verification result

maximum utilization: $\max U = 0.781 < 1$ **ok.**

design values

transformation of member forces to the reference point (intersection point of beam axis')

$$M_{1,Ed} = V_{j1,Ed} \cdot e_1 = -0.69 \text{ kNm}, \quad e_1 = -4.3 \text{ mm}$$

$$V_{1,Ed} = V_{j1,Ed} = 160.00 \text{ kN}$$

design resistance of the connection

angle leg at main girder:

compression by contact

dimensions of contact area $h_D = 20.0 \text{ mm}$, $b_D = 11.3 \text{ mm}$, compression force in contact area $D = 30.15 \text{ kN}$

check: $D / (A_D \cdot f_{yD}) = 0.569 < 1$ **ok.** $\Rightarrow$ compression by contact exists

calculation of the point section:

$$\text{bolt 1 } T_{y,1} = 3.02 \text{ kN}, \quad T_{z,1} = 26.67 \text{ kN}, \quad T_1 = 26.84 \text{ kN}$$

$$\text{bolt 2 } T_{y,2} = 10.05 \text{ kN}, \quad T_{z,2} = 26.67 \text{ kN}, \quad T_2 = 28.50 \text{ kN}$$

$$\text{bolt 3 } T_{y,3} = 17.09 \text{ kN}, \quad T_{z,3} = 26.67 \text{ kN}, \quad T_3 = 31.67 \text{ kN}$$

shear force resistance

bolts in shear:

$$U_i = T_j / F_{v,Rd}, \quad V_{Rd,i} = V_{1,Ed} / U_i, \quad V_{Rd} = \min V_{Rd,i}$$

design shear resistance per shear plane: $F_{v,Rd} = \alpha_v \cdot f_{ub} \cdot A / \gamma_{M2} = 60.32 \text{ kN}$, $\alpha_v = 0.60$

$$\text{bolt 1: } U_1 = 0.445 \quad V_{Rd,1} = 359.6 \text{ kN}$$

$$\text{bolt 2: } U_2 = 0.472 \quad V_{Rd,2} = 338.7 \text{ kN}$$

$$\text{bolt 3: } U_3 = 0.525 \quad V_{Rd,3} = 304.7 \text{ kN}$$

design shear resistance total: $V_{Rd,1} = 304.7 \text{ kN}$

angle leg 2 with bearing resistance:

$$U_{z,i} = T_{z,i} / F_{b,z,Rd}, \quad U_{y,i} = T_{y,i} / F_{b,y,Rd}, \quad U_i = \max(U_{z,i}, U_{y,i}), \quad V_{Rd,i} = V_{1,Ed} / U_i, \quad V_{Rd} = \min V_{Rd,i}$$

$$\text{bolt 1: } F_{b,z,1} = 87.27 \text{ kN} \quad F_{b,y,1} = 109.09 \text{ kN} \quad U_1 = 0.306 \quad V_{Rd,1} = 523.6 \text{ kN}$$

$$\text{bolt 2: } F_{b,z,2} = 116.73 \text{ kN} \quad F_{b,y,2} = 109.09 \text{ kN} \quad U_2 = 0.228 \quad V_{Rd,2} = 700.4 \text{ kN}$$

$$\text{bolt 3: } F_{b,z,3} = 87.62 \text{ kN} \quad F_{b,y,3} = 109.09 \text{ kN} \quad U_3 = 0.304 \quad V_{Rd,3} = 525.7 \text{ kN}$$

design bearing resistance total: $V_{Rd,2} = 523.6 \text{ kN}$

beam web with bearing resistance:

$$U_{z,i} = T_{z,i} / F_{b,z,Rd}, \quad U_{y,i} = T_{y,i} / F_{b,y,Rd}, \quad U_i = \max(U_{z,i}, U_{y,i}), \quad V_{Rd,i} = V_{1,Ed} / U_i, \quad V_{Rd} = \min V_{Rd,i}$$

$$\text{bolt 1: } F_{b,z,1} = 100.39 \text{ kN} \quad F_{b,y,1} = 123.84 \text{ kN} \quad U_1 = 0.266 \quad V_{Rd,1} = 602.3 \text{ kN}$$

$$\text{bolt 2: } F_{b,z,2} = 100.39 \text{ kN} \quad F_{b,y,2} = 123.84 \text{ kN} \quad U_2 = 0.266 \quad V_{Rd,2} = 602.3 \text{ kN}$$

$$\text{bolt 3: } F_{b,z,3} = 100.39 \text{ kN} \quad F_{b,y,3} = 123.84 \text{ kN} \quad U_3 = 0.266 \quad V_{Rd,3} = 602.3 \text{ kN}$$

design bearing resistance total: $V_{Rd,3} = 602.3 \text{ kN}$

shear resistance: $\min V_{Rd,a2} = V_{Rd,1} = 304.7 \text{ kN}$

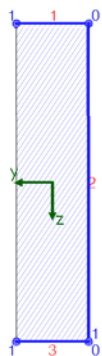
angle leg at supported beam:

s. weld verification

verification of the connection

$$V_{Ed} = 160.0 \text{ kN: } V_{Ed} / \min V_{Rd} = 0.525 < 1 \quad \text{ok.}$$

weld verification



weld 1:	$a_w = 5.0 \text{ mm}$	$l_w = 50.0 \text{ mm}$
weld 2:	$a_w = 5.0 \text{ mm}$	$l_w = 220.2 \text{ mm}$
weld 3:	$a_w = 5.0 \text{ mm}$	$l_w = 50.0 \text{ mm}$

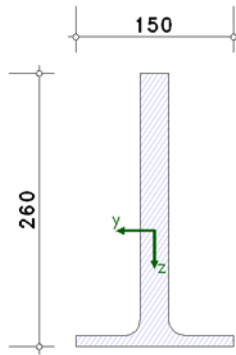
$$F_{w,Ed} = 5.45 \text{ kN/cm} < F_{w,Rd} = 10.39 \text{ kN/cm} \Rightarrow U_w = 0.524 < 1 \quad \text{ok.}$$

end weld:

$$F_{w,Ed} = 1.60 \text{ kN/cm} < F_{w,Rd} = 6.24 \text{ kN/cm} \Rightarrow U_w = 0.257 < 1 \text{ ok.}$$

cross-sectional check of supported beam

verification at $\Delta x = 95.8 \text{ mm}$ with notch

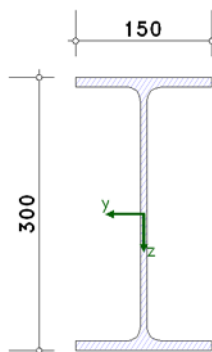


elastic cross-sectional check for $M_{Ed} = 14.64 \text{ kNm}$, $V_{Ed} = 160.00 \text{ kN}$

elastic stresses: $\max \sigma_x = 2.84 \text{ kN/cm}^2$, $\min \sigma_x = -3.85 \text{ kN/cm}^2$, $\max \tau = 3.14 \text{ kN/cm}^2$, $\max \sigma_v = 5.43 \text{ kN/cm}^2$

utilizations: design resistance $U_\sigma = 0.231 < 1 \text{ ok.}$

verification at $\Delta x = 104.3 \text{ mm}$



elastic cross-sectional check for $M_{Ed} = 16.00 \text{ kNm}$, $V_{Ed} = 160.00 \text{ kN}$

elastic stresses: $\max \sigma_x = 2.87 \text{ kN/cm}^2$, $\min \sigma_x = -2.87 \text{ kN/cm}^2$, $\max \tau = 8.47 \text{ kN/cm}^2$, $\max \sigma_v = 14.68 \text{ kN/cm}^2$

utilizations: design resistance $U_\sigma = 0.625 < 1 \text{ ok.}$, c/t-ratio $U_{c/t} = 0.131 < 1 \text{ ok.}$

verification result

maximum utilization: $\max U = 0.625 < 1 \text{ ok.}$

Final Result

maximum utilization [Lk 1]: design resistance $\max U = 0.781 < 1 \text{ ok.}$
c/t-ratio $\max U = 0.147 < 1 \text{ ok.}$

verification succeeded

Regulations

DIN EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

DIN EN 1990/NA, Nationaler Anhang zur DIN EN 1990, Ausgabe Dezember 2010

DIN EN 1993-1-1, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1993-1-1:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-1/NA, Nationaler Anhang zur DIN EN 1993-1-1, Ausgabe Dezember 2010

DIN EN 1993-1-8, Eurocode 3: Bemessung und Konstruktion von Stahlbauten -

Teil 1-8: Bemessung von Anschlüssen;

Deutsche Fassung EN 1993-1-8:2005 + AC:2009, Ausgabe Dezember 2010

DIN EN 1993-1-8/NA, Nationaler Anhang zur DIN EN 1993-1-8, Ausgabe Dezember 2010

