

POS. 15: 2 BOLTS (BEAM-COLUMN) (1 LK)

standardized IM-joint

moment resistant joints IM acc. to EC 3-1-8 (12.10), NA: Deutschland

dimensions of beam, bolts, end-plate and welds, material
and arrangement of bolts are taken of the following literature:

'Typisierte Anschlüsse im Stahlhochbau nach DIN EN 1993-1-8, Ergänzungsband 2018,
Stahlbau Verlags- und Service GmbH, Ausgabe 2018'

the current number and associated parameters are recorded.

the column has no reference to the literature, web stiffeners are continuously fixed.

MN-interaction follows Cерfontaine (in Jaspart/Weynand: Design of Joints in Steel Structures).

beam-column connection, steel grade S235, bolt class of bolts 10.9

10760: beam section HEA240, bolt size M24, connection with 2 bolts per row

end-plate: $t_p = 30 \text{ mm}$, $b_p = 240 \text{ mm}$, $h_p = 440 \text{ mm}$, $e_1 = 55 \text{ mm}$, $p_{1,1} = 110 \text{ mm}$, $p_{1,2} = 110 \text{ mm}$
 $p_{1,3} = 110 \text{ mm}$, $u_1 = 105 \text{ mm}$, $w = 130 \text{ mm}$

fillet welds: $a_f = 6 \text{ mm}$, $a_w = 4 \text{ mm}$

column: section HE280A

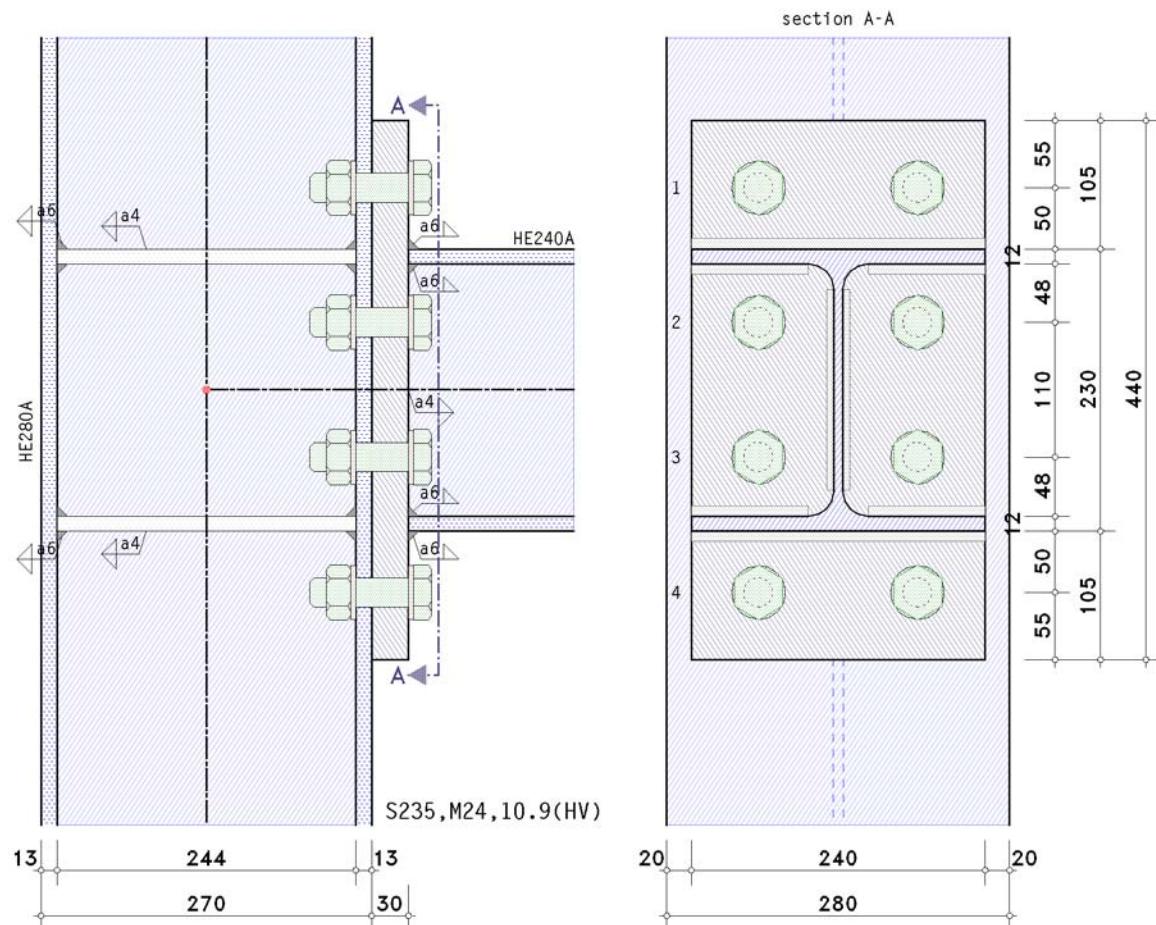
horizontal web stiffeners

internal forces and moments in the intersection point of system axes:

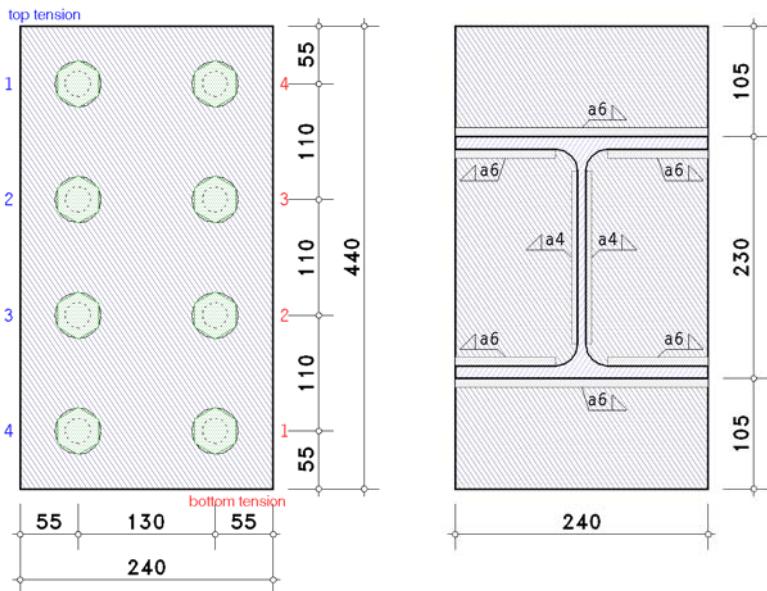
Lk 1: $M_{j,b,Ed} = -102.02 \text{ kNm}$ $V_{j,b,Ed} = 84.67 \text{ kN}$



Rigid beam connection



details



Component method

notes

connection is verified due to EC 3-1-8 regardless of preloading.
however, connections may be constructed with prestressed high strength bolts.
no verification for cross-sections.
the welds are not regarded by calculation the T-stub resistance.
simplified calculation of shear force resistance takes all bolt-rows into account.

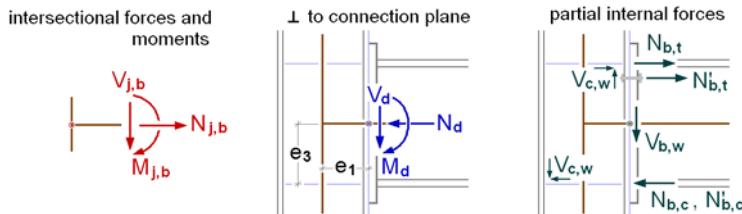
Final Result

maximum utilization: $\max U = 0.968 < 1$ **ok**
minimum rotational stiffness: $\min S_j = 13.3 \text{ MNm/rad}$, $S_{j,ini} = 27.9 \text{ MNm/rad}$
maximum rotation: $\max \varphi_{j,Ed} = 0.378^\circ$

verification succeeded

Decisive load case combination

design values



internal forces and moments in the periphery

$$\begin{aligned} N_{b,Ed} &= -N_{j,b,Ed} = 26.59 \text{ kN} \\ M_{b,Ed} &= -M_{j,b,Ed} - V_{j,b,Ed} \cdot e_1 = 90.59 \text{ kNm}, \quad e_1 = 135.0 \text{ mm} \\ V_{b,Ed} &= V_{j,b,Ed} = 84.67 \text{ kN} \end{aligned}$$

internal forces and moments perpendicular to the connection plane

$$\begin{aligned} N_d &= N_{b,Ed} = 26.59 \text{ kN} \\ M_d &= M_{b,Ed} = 90.59 \text{ kNm} \\ V_d &= V_{b,Ed} = 84.67 \text{ kN} \end{aligned}$$

partial internal forces and moments

$$\begin{aligned} \text{internal forces and moments in the periphery end-plate-beam: } M'd &= M_d - V_d \cdot t_{ep} = 88.05 \text{ kNm} \\ N_{b,t} &= -N_d \cdot z_{bu}/z_b + M'd/z_b = 390.60 \text{ kN}, \quad z_b = 218.0 \text{ mm}, \quad z_{bu} = 109.0 \text{ mm} \\ N_{b,c} &= N_d \cdot z_{bo}/z_b + M'd/z_b = 417.19 \text{ kN}, \quad z_b = 218.0 \text{ mm}, \quad z_{bo} = 109.0 \text{ mm} \end{aligned}$$

resistance of cross-section

plastic cross-sectional check for $N = -26.59 \text{ kN}$, $M_y = -88.05 \text{ kNm}$, $V_z = 84.67 \text{ kN}$

valid normal/shear stress: zul $\sigma_{Rd} = 23.50 \text{ kN/cm}^2$, zul $\tau_{Rd} = 13.57 \text{ kN/cm}^2$

top flange: resistance forces $N_{max,O} = 676.80 \text{ kN}$, $N_{min,O} = -676.80 \text{ kN}$

bottom flange: resistance forces $N_{max,U} = 676.80 \text{ kN}$, $N_{min,U} = -676.80 \text{ kN}$

web: shear force $V_s = 84.67 \text{ kN}$, shear stress $\tau_s = 5.18 \text{ kN/cm}^2 \Rightarrow U_{\tau,s} = 0.382$
resistance forces $N_{max,S} = 355.14 \text{ kN}$, $N_{min,S} = -355.14 \text{ kN}$

main bending: axial force $N = -26.59 \text{ kN}$, resistance forces $N_{max} = 1708.74 \text{ kN}$, $N_{min} = -1708.74 \text{ kN} \Rightarrow U_N = 0.016$

moment $M_y = -88.05 \text{ kNm}$, resistance moments $M_{y,max} = 166.79 \text{ kNm}$, $M_{y,min} = -166.79 \text{ kNm} \Rightarrow U_{My} = 0.528$

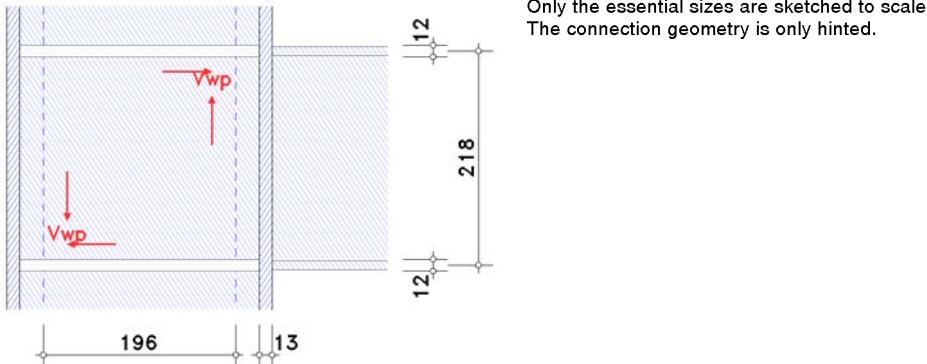
total (possibly due to load increase): max $U = 0.545 < 1 \text{ ok}$

utilizations: resistance $U_\sigma = 0.545 < 1 \text{ ok}$, c/t-ratio $U_{c/t} = 0.424 < 1 \text{ ok}$

basic components

basic component 1: Column web panel in shear

transformation parameter (EC 3-1-8, 5.3(9)) $\beta = 1.00$



slenderness of column web $d_c/t_{wc} = 24.50 < 69 \cdot \varepsilon = 69.00 \Rightarrow$ method applicable

plastic shear resistance without stiffeners $V_{wp,Rd} = (0.9 \cdot f_{y,w} \cdot A_v) / (3^{1/2} \cdot \gamma_{M0}) = 387.6 \text{ kN}$

placing of intermediate web stiffeners:

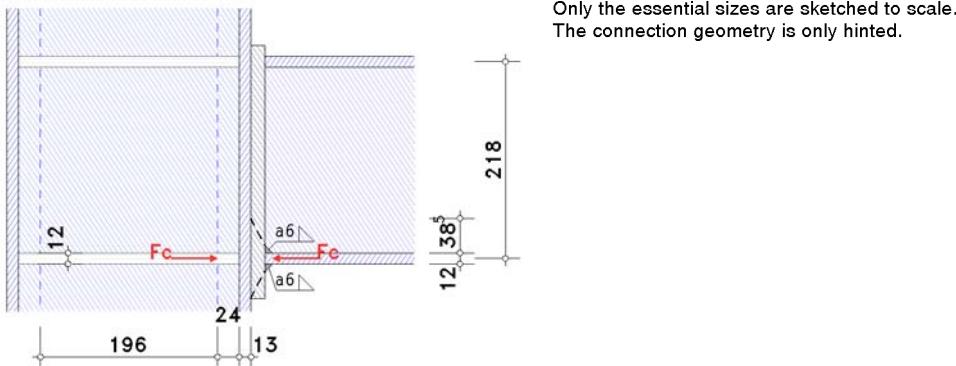
additional resistance $V_{wp,add,Rd} = 4 \cdot M_{pl,fc,Rd} / d_{st} = 51.0 \text{ kN}$

$V_{wp,add,Rd} > 2 \cdot (M_{pl,fc,Rd} + M_{pl,st,Rd}) / d_{st} = 44.8 \text{ kN} \Rightarrow V_{wp,add,Rd} = 44.8 \text{ kN}$

plastic shear resistance with transverse stiffeners $V_{wp,Rd} = 432.4 \text{ kN}$

basic component 2: column web in transverse compression

transformation parameter (EC 3-1-8, 5.3(9)) $\beta = 1.00$



reinforcement of web with transverse stiffeners:

assumption: stiffeners do not buckle: $c/t = 10.3 \cdot \varepsilon \leq 33 \cdot \varepsilon \Rightarrow$ section class $1 \leq 2 \text{ ok}$

minimum demands of the moment of inertia of stiffeners:

length of buckling field (distance of stiffeners) $a = 218.0 \text{ mm}$

web height between the flanges $h_{wc} = 244.0 \text{ mm}$

moment of inertia of stiffeners $I_{st} = 1677.72 \text{ cm}^4$

minimum moment of inertia for $a/h_{wc} = 0.89 < 2^{1/2}$: $I_{st,min} = 23.48 \text{ cm}^4 < I_{st} \text{ ok}$

requirement concerning stiffeners to avoid lateral torsional buckling:

torsional moment of inertia of stiffeners $I_T = 7.14 \text{ cm}^4$

polar moment of inertia of stiffeners $I_p = 192.45 \text{ cm}^4$

$I_T / I_p \approx 0.037 > 0.006 = 5.3 \cdot f_{y,st} / E_{st} \text{ ok}$

resistance of stiffened webs with transverse compression:

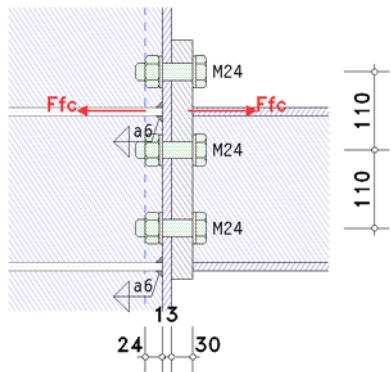
area of stiffeners incl. web $A_{st} = 30.72 \text{ cm}^2$

slenderness $\lambda = 0.035$

$\lambda \leq 0.2 \Rightarrow$ no deduction ($\chi = 1.0$)

design value of resistance of flexural buckling $F_{c,w,Rd} = 656.3 \text{ kN}$

basic component 4: column flange in bending



Only the essential sizes are sketched to scale.
The connection geometry is only hinted.

equivalent T-stub flange (each bolt-row decisive):

here: number of bolt-rows $n_b = 1$

row 1

effective length of the T-stub flange (column flange):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 262.6 \text{ mm}$, $l_{eff,cp} = 262.6 \text{ mm}$

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 298.5 \text{ mm}$

tension resistance of the T-stub flange:

in mode 1: $M_{pl,1,Rd} = (0.25 \cdot \Sigma l_{eff,1} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 2.61 \text{ kNm}$

in mode 2: $M_{pl,2,Rd} = (0.25 \cdot \Sigma l_{eff,2} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 2.96 \text{ kNm}$

in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32 \text{ kN}$

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 309.77 \text{ kN}$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 345.42 \text{ kN}$

mode 3: bolt failure

$F_{T,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 309.77 \text{ kN}$

row 2

effective length of the T-stub flange (column flange):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 262.6 \text{ mm}$, $l_{eff,cp} = 262.6 \text{ mm}$

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 302.5 \text{ mm}$

tension resistance of the T-stub flange:

in mode 1: $M_{pl,1,Rd} = (0.25 \cdot \Sigma l_{eff,1} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 2.61 \text{ kNm}$

in mode 2: $M_{pl,2,Rd} = (0.25 \cdot \Sigma l_{eff,2} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 3.00 \text{ kNm}$

in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32 \text{ kN}$

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 309.77 \text{ kN}$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 346.27 \text{ kN}$

mode 3: bolt failure

$F_{T,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 309.77 \text{ kN}$

row 3

effective length of the T-stub flange (column flange):

in mode 1: $\Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 262.6 \text{ mm}$, $l_{eff,cp} = 262.6 \text{ mm}$

in mode 2: $\Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 302.5 \text{ mm}$

tension resistance of the T-stub flange:

in mode 1: $M_{pl,1,Rd} = (0.25 \cdot \Sigma l_{eff,1} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 2.61 \text{ kNm}$

in mode 2: $M_{pl,2,Rd} = (0.25 \cdot \Sigma l_{eff,2} \cdot t_f^2 \cdot f_y) / \gamma_{M0} = 3.00 \text{ kNm}$

in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32 \text{ kN}$

mode 1: complete yielding of the T-stub flange

$F_{T,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 309.77 \text{ kN}$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$F_{T,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 346.27 \text{ kN}$

mode 3: bolt failure

$F_{T,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$

tension resistance of the T-stub flange: $F_{T,Rd} = \min(F_{T,1,Rd}, F_{T,2,Rd}, F_{T,3,Rd}) = 309.77 \text{ kN}$

resistances and effective lengths of column flange in bending (per bolt-row)

$F_{t,fc,Rd,1} = 309.77 \text{ kN}$, $l_{eff,1} = 262.6 \text{ mm}$

$F_{t,fc,Rd,2} = 309.77 \text{ kN}$, $l_{eff,1} = 262.6 \text{ mm}$

$F_{t,fc,Rd,3} = 309.77 \text{ kN}$, $l_{eff,1} = 262.6 \text{ mm}$

equivalent T-stub flange (group of bolts 1):

here: number of bolt-rows $n_b = 2$ (between stiffeners)

effective length of the T-stub flange (column flange):

in mode 1: $\Sigma l_{eff,1} = \min(\Sigma l_{eff,nc}, \Sigma l_{eff,cp}) = 454.1 \text{ mm}$, $\Sigma l_{eff,cp} = 482.6 \text{ mm}$

in mode 2: $\Sigma l_{eff,2} = \Sigma l_{eff,nc} = 454.1 \text{ mm}$

tension resistance of the T-stub flange:

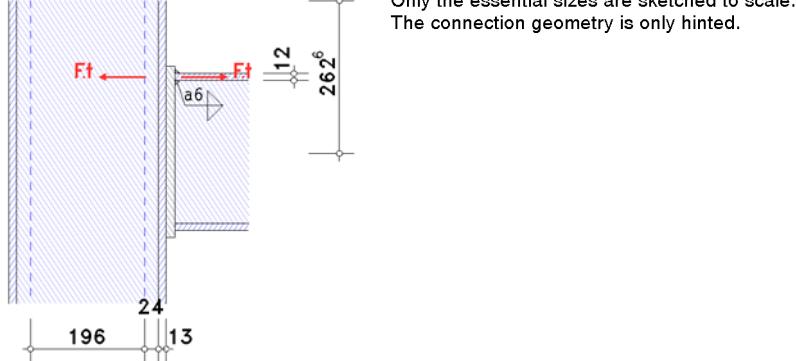
in mode 1+2: $M_{pl,Rd} = (0.25 \cdot \Sigma_{eff} \cdot t_f^2 \cdot f_y) / \gamma M_0 = 4.51 \text{ kNm}$
 in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 1016.64 \text{ kN}$
 mode 1: complete yielding of the T-stub flange
 $F_{t,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 535.58 \text{ kN}$
 mode 2: bolt failure simultaneously with yielding of the T-stub flange
 $F_{t,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 660.68 \text{ kN}$
 mode 3: bolt failure
 $F_{t,3,Rd} = \Sigma F_{t,Rd} = 1016.64 \text{ kN}$
 tension resistance of the T-stub flange: $F_{t,Rd} = \min(F_{t,1,Rd}, F_{t,2,Rd}, F_{t,3,Rd}) = 535.58 \text{ kN}$

resistances and effective lengths of end-plate in bending (per bolt group):

$$F_{ep,Rd,2-3} = 535.58 \text{ kN}, \Sigma_{eff} = 454.1 \text{ mm}, 2 \text{ rows}$$

basic component 3: column web in transverse tension

transformation parameter (EC 3-1-8, 5.3(9)) $\beta = 1.00$



each bolt-row decisive:

row 1

effective width $b_{eff,t} = 262.6 \text{ mm}$ (ℓ_{eff} from bc 4)
 reduction factor for interaction with shear stress $\beta = 1 \Rightarrow \omega = 0.798$
 resistance of a column web with transverse tension
 $F_{t,wc,Rd} = \omega \cdot (b_{eff,t} \cdot t_{wc} \cdot f_y,wc) / \gamma M_0 = 394.1 \text{ kN}$

row 2

effective width $b_{eff,t} = 262.6 \text{ mm}$ (ℓ_{eff} from bc 4)
 reduction factor for interaction with shear stress $\beta = 1 \Rightarrow \omega = 0.798$
 resistance of a column web with transverse tension
 $F_{t,wc,Rd} = \omega \cdot (b_{eff,t} \cdot t_{wc} \cdot f_y,wc) / \gamma M_0 = 394.1 \text{ kN}$

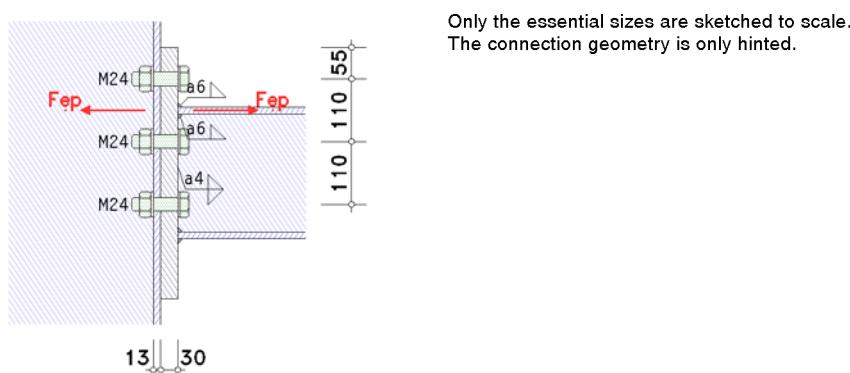
row 3

effective width $b_{eff,t} = 262.6 \text{ mm}$ (ℓ_{eff} from bc 4)
 reduction factor for interaction with shear stress $\beta = 1 \Rightarrow \omega = 0.798$
 resistance of a column web with transverse tension
 $F_{t,wc,Rd} = \omega \cdot (b_{eff,t} \cdot t_{wc} \cdot f_y,wc) / \gamma M_0 = 394.1 \text{ kN}$

group of bolt-rows, group 1:

effective width $b_{eff,t} = 454.1 \text{ mm}$ (ℓ_{eff} from bc 4)
 reduction factor for interaction with shear stress $\beta = 1 \Rightarrow \omega = 0.608$
 resistance of a column web with transverse tension
 $F_{t,wc,Rd} = \omega \cdot (b_{eff,t} \cdot t_{wc} \cdot f_y,wc) / \gamma M_0 = 519.3 \text{ kN}$

basic component 5: end-plate in bending



extended part of end-plate

in the extended part of the end-plate only one bolt-row is considered ($n_b = 1$).

effective length of the T-stub flange (end-plate):

in mode 1: $\Sigma_{eff,1} = \ell_{eff,1} = \min(\ell_{eff,nc}, \ell_{eff,cp}) = 120.0 \text{ mm}, \ell_{eff,cp} = 245.8 \text{ mm}$

in mode 2: $\Sigma_{eff,2} = \ell_{eff,2} = \ell_{eff,nc} = 120.0 \text{ mm}$

tension resistance of the T-stub flange:

in mode 1+2: $M_{pl,Rd} = (0.25 \cdot \Sigma_{eff} \cdot t_f^2 \cdot f_y) / \gamma M_0 = 6.34 \text{ kNm}$

in mode 3: $\Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32$ kN

mode 1: complete yielding of the T-stub flange

$$F_{t,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 723.10 \text{ kN}$$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$$F_{t,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 412.92 \text{ kN}$$

mode 3: bolt failure

$$F_{t,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$$

tension resistance of the T-stub flange: $F_{t,Rd} = \min(F_{t,1,Rd}, F_{t,2,Rd}, F_{t,3,Rd}) = 412.92$ kN

resistance and effective length of end-plate in bending (projection)

$$F_{t,ep,Rd,1} = 412.9 \text{ kN}, \quad l_{eff,1} = 120.0 \text{ mm}$$

part of end-plate between beam flanges

equivalent T-stub flange (each bolt-row decisive):

here: number of bolt-rows $n_b = 1$

row 2

effective length of the T-stub flange (end-plate):

$$\text{in mode 1: } \Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 339.3 \text{ mm}, \quad l_{eff,cp} = 356.4 \text{ mm}$$

$$\text{in mode 2: } \Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 339.3 \text{ mm}$$

tension resistance of the T-stub flange:

$$\text{in mode 1+2: } M_{pl,Rd} = (0.25 \cdot \Sigma l_{eff} \cdot t_f^2 \cdot f_y) / \gamma_M = 17.94 \text{ kNm}$$

$$\text{in mode 3: } \Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32 \text{ kN}$$

mode 1: complete yielding of the T-stub flange

$$F_{t,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 1496.81 \text{ kN}$$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$$F_{t,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 571.43 \text{ kN}$$

mode 3: bolt failure

$$F_{t,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$$

tension resistance of the T-stub flange: $F_{t,Rd} = \min(F_{t,1,Rd}, F_{t,2,Rd}, F_{t,3,Rd}) = 508.32$ kN

row 3

effective length of the T-stub flange (end-plate):

$$\text{in mode 1: } \Sigma l_{eff,1} = l_{eff,1} = \min(l_{eff,nc}, l_{eff,cp}) = 339.3 \text{ mm}, \quad l_{eff,cp} = 356.4 \text{ mm}$$

$$\text{in mode 2: } \Sigma l_{eff,2} = l_{eff,2} = l_{eff,nc} = 339.3 \text{ mm}$$

tension resistance of the T-stub flange:

$$\text{in mode 1+2: } M_{pl,Rd} = (0.25 \cdot \Sigma l_{eff} \cdot t_f^2 \cdot f_y) / \gamma_M = 17.94 \text{ kNm}$$

$$\text{in mode 3: } \Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 508.32 \text{ kN}$$

mode 1: complete yielding of the T-stub flange

$$F_{t,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 1496.81 \text{ kN}$$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$$F_{t,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 571.43 \text{ kN}$$

mode 3: bolt failure

$$F_{t,3,Rd} = \Sigma F_{t,Rd} = 508.32 \text{ kN}$$

tension resistance of the T-stub flange: $F_{t,Rd} = \min(F_{t,1,Rd}, F_{t,2,Rd}, F_{t,3,Rd}) = 508.32$ kN

resistances and effective lengths of end-plate in bending (per bolt-row):

$$F_{ep,Rd,2} = 508.32 \text{ kN}, \quad l_{eff,1} = 339.3 \text{ mm}$$

$$F_{ep,Rd,3} = 508.32 \text{ kN}, \quad l_{eff,1} = 339.3 \text{ mm}$$

equivalent T-stub flange (group of bolts 1):

here: number of bolt-rows $n_b = 2$

effective length of the T-stub flange (end-plate):

$$\text{in mode 1: } \Sigma l_{eff,1} = \min(\Sigma l_{eff,nc}, \Sigma l_{eff,cp}) = 493.0 \text{ mm}, \quad \Sigma l_{eff,cp} = 576.4 \text{ mm}$$

$$\text{in mode 2: } \Sigma l_{eff,2} = \Sigma l_{eff,nc} = 493.0 \text{ mm}$$

tension resistance of the T-stub flange:

$$\text{in mode 1+2: } M_{pl,Rd} = (0.25 \cdot \Sigma l_{eff} \cdot t_f^2 \cdot f_y) / \gamma_M = 26.07 \text{ kNm}$$

$$\text{in mode 3: } \Sigma F_{t,Rd} = 2 \cdot n_b \cdot F_{t,Rd} = 1016.64 \text{ kN}$$

mode 1: complete yielding of the T-stub flange

$$F_{t,1,Rd} = ((8 \cdot n \cdot 2 \cdot e_w) \cdot M_{pl,1,Rd}) / (2 \cdot m \cdot n \cdot e_w \cdot (m+n)) = 2174.75 \text{ kN}$$

mode 2: bolt failure simultaneously with yielding of the T-stub flange

$$F_{t,2,Rd} = (2 \cdot M_{pl,2,Rd} + n \cdot \Sigma F_{t,Rd}) / (m+n) = 967.15 \text{ kN}$$

mode 3: bolt failure

$$F_{t,3,Rd} = \Sigma F_{t,Rd} = 1016.64 \text{ kN}$$

tension resistance of the T-stub flange: $F_{t,Rd} = \min(F_{t,1,Rd}, F_{t,2,Rd}, F_{t,3,Rd}) = 967.15$ kN

resistances and effective lengths of end-plate in bending (per bolt group):

$$F_{ep,Rd,2-3} = 967.15 \text{ kN}, \quad \Sigma l_{eff} = 493.0 \text{ mm}, \quad 2 \text{ rows}$$

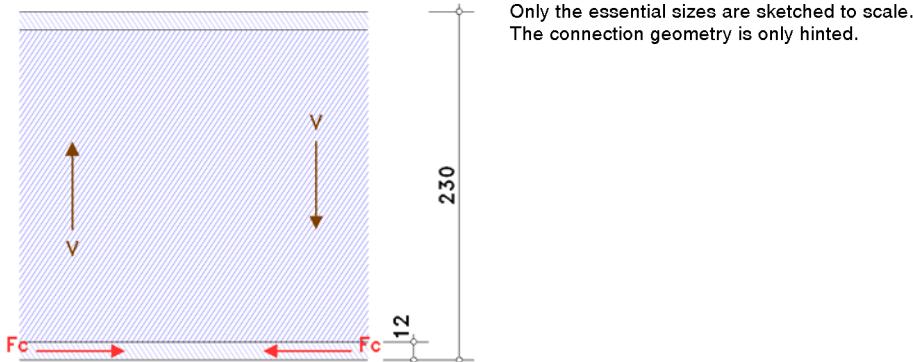
basic component 7: beam flange and web in compression

flange bottom: section class for $c/(s \cdot t) = 7.94$: 1

web: section class for $\alpha = 0.52$ and $c/(s \cdot t) = 21.87$: 1

section class of beam: 1

taking into account the moment-shear force-interaction $V_{Ed} = 84.7$ kN



stress due to bending with shear force: $V_{Ed} = 84.7$ kN ≤ 170.8 kN $= V_{pl,Rd}/2 \Rightarrow$ no effect

resistance $M_{c,Rd} = M_{pl,Rd} = (W_{pl} \cdot f_y) / \gamma M_0 = 175.07$ kNm, $W_{pl} = 745.00$ cm³

resistance of a flange (and web) with compression

$$F_{c,f,Rd} = M_{c,Rd} / (h - t_f) = 803.10$$
 kN

resistance of upper beam flange:

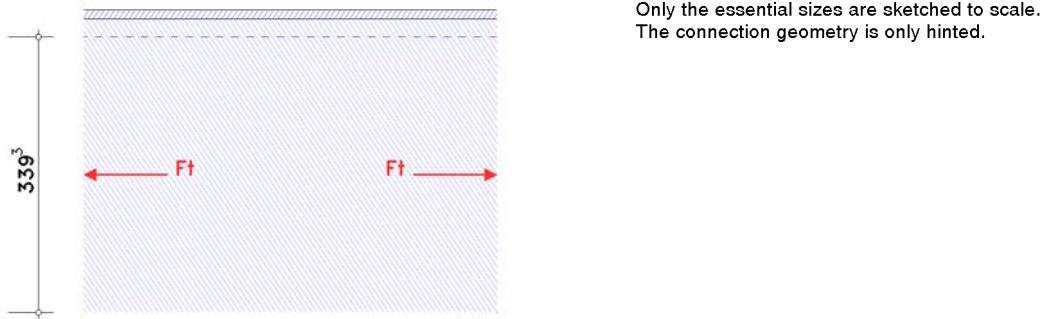
stress due to bending with shear force: $V_{Ed} = 84.7$ kN ≤ 170.8 kN $= V_{pl,Rd}/2 \Rightarrow$ no effect

resistance $M_{c,Rd} = M_{pl,Rd} = (W_{pl} \cdot f_y) / \gamma M_0 = 175.07$ kNm, $W_{pl} = 745.00$ cm³

resistance of a flange (and web) with compression

$$F_{c,f,Rd} = M_{c,Rd} / (h - t_f) = 803.10$$
 kN

basic component 8: beam web in tension



each bolt-row decisive:

row 2

effective width $b_{eff,t,wb} = 339.3$ mm (l_{eff} from bc 5)

resistance of a beam web in tension

$$F_{t,wb,Rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_y,wb / \gamma M_0 = 598.1$$
 kN

row 3

effective width $b_{eff,t,wb} = 339.3$ mm (l_{eff} from bc 5)

resistance of a beam web in tension

$$F_{t,wb,Rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_y,wb / \gamma M_0 = 598.1$$
 kN

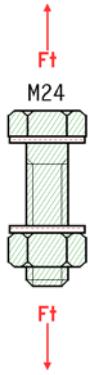
group of bolt-rows, group 1:

effective width $b_{eff,t,wb} = 493.0$ mm (l_{eff} from bc 5)

resistance of a beam web in tension

$$F_{t,wb,Rd} = b_{eff,t,wb} \cdot t_{wb} \cdot f_y,wb / \gamma M_0 = 869.0$$
 kN

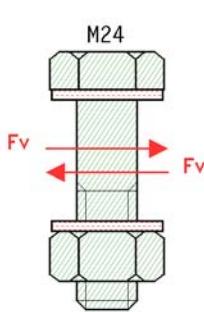
basic component 10: bolts in tension



Only the essential sizes are sketched to scale.
The connection geometry is only hinted.

tension resistance of one bolt $F_{t,Rd} = (k_2 \cdot f_{ub} \cdot A_s) / \gamma_{M2} = 254.16 \text{ kN}$, $k_2 = 0.90$
punching shear load capacity $B_{p,Rd} = (0.6 \cdot \pi \cdot d_m \cdot t_p \cdot f_u) / \gamma_{M2} = 304.17 \text{ kN}$, $t_p = 13.0 \text{ mm}$
tension-/punching shear load capacity for 2 bolts: $\Sigma F_{tp,Rd} = 2 \cdot \min(F_{t,Rd}, B_{p,Rd}) = 508.32 \text{ kN}$

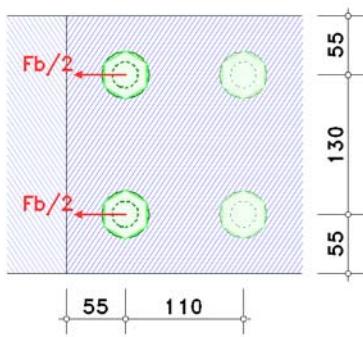
basic component 11: bolts in shear



Only the essential sizes are sketched to scale.
The connection geometry is only hinted.

shear resistance per shear plane $F_{v,Rd} = \alpha_v \cdot f_{ub} \cdot A / \gamma_{M2} = 217.15 \text{ kN}$, $\alpha_v = 0.60$
shear resistance of 2 bolts (1-shear): $\Sigma F_{v,Rd} = 2 \cdot F_{v,Rd} = 434.29 \text{ kN}$

basic component 12: plate with bearing resistance



Only the essential sizes are sketched to scale.
The connection geometry is only hinted.

row 1

end-plate:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 365.54 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 0.71$
bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 365.54 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 0.71$
bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 731.08 \text{ kN}$

column flange:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 449.28 \text{ kN}$

row 2

end-plate:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1036.80 \text{ kN}$

column flange:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$
bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 449.28 \text{ kN}$

row 3

end-plate:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40 \text{ kN}$, $k_1 = 2.50$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1036.80$ kN

column flange:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 449.28$ kN

row 4

end-plate:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 518.40$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 1036.80$ kN

column flange:

bolt 1: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bolt 2: bearing resistance $F_{b,Rd} = (k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t) / \gamma_{M2} = 224.64$ kN, $k_1 = 2.50$, $\alpha_b = 1.00$

bearing resistance of 1x2 bolts: $\Sigma F_{b,Rd} = 449.28$ kN

bearing resistance (4 rows)

$\Sigma F_{b,Rd,1} = 449.28$ kN

$\Sigma F_{b,Rd,2} = 449.28$ kN

$\Sigma F_{b,Rd,3} = 449.28$ kN

$\Sigma F_{b,Rd,4} = 449.28$ kN

connection capacity

moment resistance

distance of tension-bolt-rows from centre of compression: $h_1 = 274.0$ mm, $h_2 = 164.0$ mm, $h_3 = 54.0$ mm

resistance per bolt-row (MNV-interaction)

row 1: $F_{tr,Rd} = 309.8$ kN

row 2: $F_{tr,Rd} = 92.3$ kN

row 3: $F_{tr,Rd} = 0.0$ kN

$\Sigma F_{tr,Rd} = 402.1$ kN

resistance of flanges (MNV-interaction)

$F_{c,Rd} = 432.4$ kN

moment resistance

$M_{j,Rd} = \Sigma (F_{tr,Rd} \cdot h_r) = 100.0$ kNm

tension resistance

$N_{j,t,Rd} = \Sigma F_{tr,Rd} = 402.1$ kN

compression resistance

$N_{j,c,Rd} = F_{c,Rd} = 432.4$ kN

shear/bearing resistance

$V_{j,Rd} = 96.6$ kN (MNV-interaction)

shear resistance

shear resistance of end plate

plate: $V_{ep,Rd} = 667.53$ kN

resistance of a weld (req.1): $f_{1w,d} = f_u / (\beta_w \cdot \gamma_{M2}) = 360.0$ N/mm²

welds: $F_{w,Rd} = 272.69$ kN

shear resistance of end plate: $V_{ep,Rd} = F_{w,Rd} = 272.69$ kN

shear resistance of column web

$V_{wp,Rd}/\beta = 432.4$ kN

plastic shear resistance

$V_{pl,Rd} = 0.5 \cdot A_v \cdot (f_y / 3^{1/2}) / \gamma_{M0} = 170.8$ kN (requirement, s. 'Typisierte Anschlüsse')

total

$M_{j,Rd} = 100.0$ kNm $N_{j,t,Rd} = 402.1$ kN $N_{j,c,Rd} = 432.4$ kN $V_{j,Rd} = 96.6$ kN $V_{wp,Rd}/\beta = 432.4$ kN $V_{pl,Rd} = 170.8$ kN

$V_{ep,Rd} = 272.7$ kN

verifications

verification of the connection capacity by means of the component method

$U_{MN} = 0.877 < 1$ **ok**

$V_{wp,Ed}/(V_{wp,Rd}/\beta) = 0.968 < 1$ **ok**

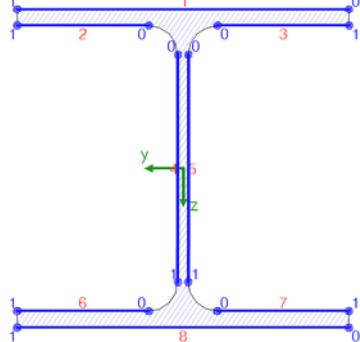
$V_{Ed}/V_{pl,Rd} = 0.496 < 1$ **ok**

$V_{Ed}/V_{ep,Rd} = 0.310 < 1$ **ok**

verification of welds at beam section

- weld 1: beam flange in tension outer welds 2,3: beam flange in tension inner
weld 8: beam flange in compression outer welds 4,5: beam web double-sided
weld 4: NA-DE: plate thickness $t_{max} \geq 30$ mm: weld thickness $a = 4.0$ mm < $a_{min} = 5$ mm !!
weld 4: weld thickness $a = 4.0$ mm > $a_{max} = 0.7 \cdot t_{min} = 3.7$ mm !!
weld 5: NA-DE: plate thickness $t_{max} \geq 30$ mm: weld thickness $a = 4.0$ mm < $a_{min} = 5$ mm !!
weld 5: weld thickness $a = 4.0$ mm > $a_{max} = 0.7 \cdot t_{min} = 3.7$ mm !!

calculation section:



weld 1:	$a_w = 6.0$ mm	$l_w = 240.0$ mm
weld 2:	$a_w = 6.0$ mm	$l_w = 95.3$ mm
weld 3:	siehe weld 2	
weld 4:	$a_w = 4.0$ mm	$l_w = 164.0$ mm
weld 5:	siehe weld 4	
weld 6:	$a_w = 6.0$ mm	$l_w = 95.3$ mm
weld 7:	siehe weld 6	
weld 8:	$a_w = 6.0$ mm	$l_w = 240.0$ mm

design values referring to centroid of the section:

$$N_{Ed} = -26.59 \text{ kN}, M_{y,Ed} = -90.59 \text{ kNm}, V_{z,Ed} = 84.67 \text{ kN}$$

cross-sectional properties referring to centroid of the line cross-section:

$$\Sigma A_w = 64.78 \text{ cm}^2, A_{w,z} = 13.12 \text{ cm}^2, \Sigma l_w = 118.9 \text{ cm}$$

$$I_{w,y} = 6528.08 \text{ cm}^4, I_{w,z} = 2754.52 \text{ cm}^4, W_{w,t} = 61.47 \text{ cm}^3, \Delta z_w = 0.0 \text{ mm}$$

verifications in the edge points of the individual welds:

weld 1, pt. 0: $\sigma_{w,x} = 155.48 \text{ N/mm}^2$	$\Rightarrow U_w = 0.611 < 1 \text{ ok}$
weld 2, pt. 0: $\sigma_{w,x} = 138.83 \text{ N/mm}^2$	$\Rightarrow U_w = 0.545 < 1 \text{ ok}$
weld 4, pt. 0: $\sigma_{w,x} = 109.69 \text{ N/mm}^2$	$\Rightarrow U_w = 0.531 < 1 \text{ ok}$
pt. 1: $\sigma_{w,x} = -117.89 \text{ N/mm}^2$	$\tau_{w,z} = 64.53 \text{ N/mm}^2 \Rightarrow U_w = 0.558 < 1 \text{ ok}$
weld 6, pt. 0: $\sigma_{w,x} = -147.04 \text{ N/mm}^2$	$\Rightarrow U_w = 0.578 < 1 \text{ ok}$
weld 8, pt. 0: $\sigma_{w,x} = -163.69 \text{ N/mm}^2$	$\Rightarrow U_w = 0.643 < 1 \text{ ok}$

Result:

$$\text{weld 8, pt. 1: } \sigma_{w,x} = -163.69 \text{ N/mm}^2 \\ \text{Max: } \sigma_{1,w,Ed} = 23.15 \text{ kN/cm}^2 < f_{1w,d} = 36.00 \text{ kN/cm}^2, \\ \sigma_{2,w,Ed} = 11.57 \text{ kN/cm}^2 < f_{2w,d} = 25.92 \text{ kN/cm}^2 \Rightarrow U_w = 0.643 < 1 \text{ ok}$$

verification of web stiffeners

compression stiffener

$$F_{c,Ed} = 427.00 \text{ kN}$$

forces per rib

$$F = 0.5 \cdot F_{c,Ed} \cdot (bf \cdot 2 \cdot r \cdot tw) / bf = 170.8 \text{ kN}, H = F \cdot e_F / e_H = 56.0 \text{ kN}$$

assumption: stiffeners do not buckle: $c/t = 10.3 \cdot \epsilon \leq 33 \cdot \epsilon \Rightarrow$ section class $1 \leq 2 \text{ ok}$

cross-section at flange

$$\text{compression resistance } N_{c,Rd} = (A \cdot f_y) / \gamma_m = 248.16 \text{ kN}$$

$$\text{design value: } F_{Ed} = (F^2 + 3 \cdot H^2)^{1/2} = 196.4 \text{ kN}$$

$$F_{Ed} = 196.4 \text{ kN} < F_{Rd} = 248.2 \text{ kN} \Rightarrow U = 0.792 < 1 \text{ ok}$$

cross-section at web

$$\text{shear resistance } V_{Rd} = 397.26 \text{ kN}$$

$$\text{design value: } F_{Ed} = F = 170.8 \text{ kN}$$

$$F_{Ed} = 170.8 \text{ kN} < F_{Rd} = 397.3 \text{ kN} \Rightarrow U = 0.430 < 1 \text{ ok}$$

flange welds

$$\text{design values: } F_{Ed}(\sigma_s) = F / (2 \cdot b_1) = 9.70 \text{ kN/cm}, F_{Ed}(\tau_p) = H / (2 \cdot b_1) = 3.18 \text{ kN/cm}, b_1 = 88.0 \text{ mm}$$

$$\sigma_{1,w,Ed} = 18.60 \text{ kN/cm}^2 < f_{1w,d} = 36.00 \text{ kN/cm}^2 \Rightarrow U = 0.517 < 1 \text{ ok}$$

$$\sigma_{2,w,Ed} = 16.17 \text{ kN/cm}^2 < f_{2w,d} = 25.92 \text{ kN/cm}^2 \Rightarrow U = 0.624 < 1 \text{ ok}$$

web welds

$$\text{design value: } F_{Ed}(\tau_p) = F / (2 \cdot l_1) = 4.97 \text{ kN/cm}, l_1 = 172.0 \text{ mm}$$

$$\sigma_{1,w,Ed} = 21.50 \text{ kN/cm}^2 < f_{1w,d} = 36.00 \text{ kN/cm}^2 \Rightarrow U = 0.597 < 1 \text{ ok}$$

stiffener in tension

$$F_{t,Ed} = 400.42 \text{ kN}$$

forces per rib

$$F = 0.5 \cdot F_{t,Ed} \cdot (bf \cdot 2 \cdot r \cdot tw) / bf = 160.2 \text{ kN}, H = F \cdot e_F / e_H = 52.5 \text{ kN}$$

cross-section at flange

$$\text{tension resistance } N_{t,Rd} = 248.16 \text{ kN}$$

$$\text{design value: } F_{Ed} = (F^2 + 3 \cdot H^2)^{1/2} = 184.2 \text{ kN}$$

$$F_{Ed} = 184.2 \text{ kN} < F_{Rd} = 248.2 \text{ kN} \Rightarrow U = 0.742 < 1 \text{ ok}$$

cross-section at web

$$\text{shear resistance } V_{Rd} = 397.26 \text{ kN}$$

$$\text{design value: } F_{Ed} = F = 160.2 \text{ kN}$$

$$F_{Ed} = 160.2 \text{ kN} < F_{Rd} = 397.3 \text{ kN} \Rightarrow U = 0.403 < 1 \text{ ok}$$

flange welds

design values: $F_{Ed}(\sigma_s) = F / (2 \cdot b_1) = 9.10 \text{ kN/cm}$, $F_{Ed}(\tau_p) = H / (2 \cdot b_1) = 2.98 \text{ kN/cm}$, $b_1 = 88.0 \text{ mm}$

$\sigma_{1,w,Ed} = 17.44 \text{ kN/cm}^2 < f_{1w,d} = 36.00 \text{ kN/cm}^2 \Rightarrow U = 0.485 < 1 \text{ ok}$

$\sigma_{2,w,Ed} = 15.17 \text{ kN/cm}^2 < f_{2w,d} = 25.92 \text{ kN/cm}^2 \Rightarrow U = 0.585 < 1 \text{ ok}$

web welds

design value: $F_{Ed}(\tau_p) = F / (2 \cdot l_1) = 4.66 \text{ kN/cm}$, $l_1 = 172.0 \text{ mm}$

$\sigma_{1,w,Ed} = 20.16 \text{ kN/cm}^2 < f_{1w,d} = 36.00 \text{ kN/cm}^2 \Rightarrow U = 0.560 < 1 \text{ ok}$

verification result

maximum utilization: max $U = 0.968 < 1 \text{ ok}$

rotational stiffness

stiffness coefficients

$$k_1 = 0.38 \cdot A_{vc} / (\beta \cdot z) = 5.51 \text{ mm}$$

$k_2 = \infty$ (stiffened)

equivalent stiffness coefficient for 2 tension-bolt-rows:

$$1: k_3 = 7.50 \text{ mm}, k_4 = 7.11 \text{ mm}, k_5 = 36.14 \text{ mm}, k_{10} = 8.25 \text{ mm} \Rightarrow k_{eff,1} = 1 / \sum(1/k_i,1) = 2.365 \text{ mm}$$

$$2: k_3 = 6.49 \text{ mm}, k_4 = 6.15 \text{ mm}, k_5 = 32.82 \text{ mm}, k_{10} = 8.25 \text{ mm} \Rightarrow k_{eff,2} = 1 / \sum(1/k_i,2) = 2.134 \text{ mm}$$

$$k_{eq} = \sum(k_{eff,r} \cdot h_r) / z_{eq} = 4.239 \text{ mm}, z_{eq} = \sum(k_{eff,r} \cdot h_r^2) / \sum(k_{eff,r} \cdot h_r) = 235.4 \text{ mm}$$

rotational stiffness

initial rotational stiffness: $S_{j,ini} = (E \cdot z^2) / \sum(1/k_i) = 27881.2 \text{ kNm/rad}$, $z = z_{eq} = 235.4 \text{ mm}$, $\sum(1/k_i) = 0.417 \text{ mm}^{-1}$

$$N_{b,Ed} = N_d = 26.59 \text{ kN}$$

$$|N_{b,Ed}| = 26.59 \text{ kN} < 5\% \cdot N_{pl,Rd} = 90.28 \text{ kN} \text{ ok}$$

$$|M_{j,Ed}| = 87.69 \text{ kNm} > 2/3 \cdot M_{j,Rd} = 66.7 \text{ kNm} \Rightarrow \mu = ((1.5 \cdot M_{j,Ed}) / M_{j,Rd})^\Psi = 2.095, \Psi = 2.7$$

rotational stiffness: $S_{j,Rd} = S_{j,ini} / \mu = 13305.4 \text{ kNm/rad}$

rotation: $\varphi_{j,Ed} = M_{j,Ed} / S_{j,Rd} = 0.378^\circ$