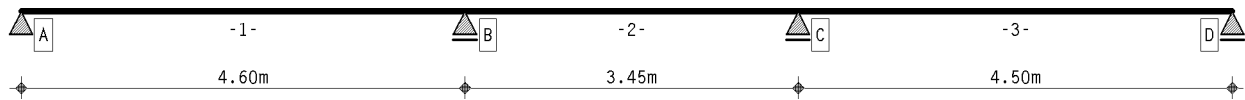


1. Options for Calculations

calculation DIN EN 1995:2010, Germany

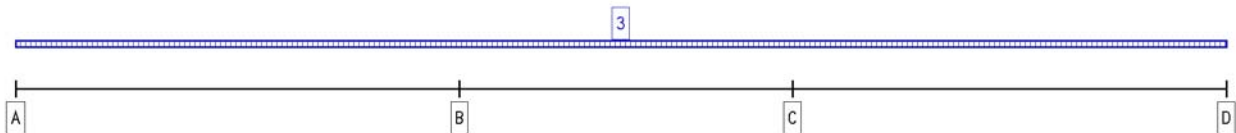
service class 1

2. Structural system

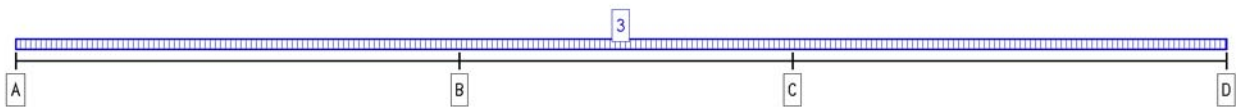


main beam

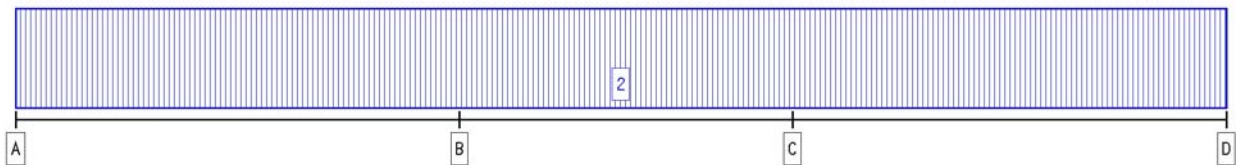
3. Loading



action effect 1: permanent loads (permanent, 2 load cases)



D

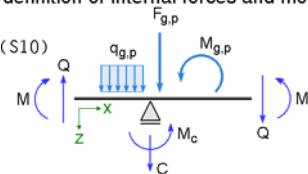


action effect 2: live loads (1) (transient, 1 load cases)

4. material parameters

beam Cross Laminated Timber Leno, 160
 structure 34.0-34.0-24.0-34.0-34.0 solid coniferous timber, C24 (S10)
 direction of fibre x-axis (strong axis)
 service class 1
 beam width/-höhe b/h = 1000 mm / 160 mm
 coeff. thermal expan. timber 0.500 *10⁻⁵ /°K
 shear coefficient κ 0.166597

definition of internal forces and moments:



5. Beam sections

beam sections

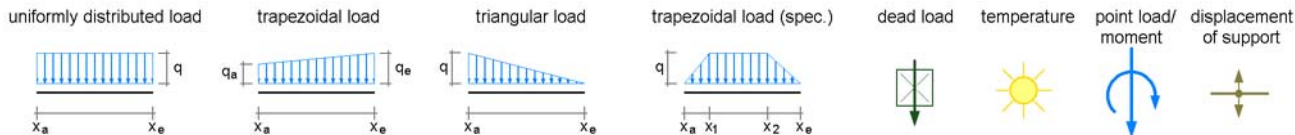
section	x _A m	x _E m	l m	l _v m	cant.11.	E _I eff Nmm ²	G _A eff N	E _A eff N	E _I eff,fire Nmm ²	G _A eff,fire N	E _A eff,fire N	z _{s,fire} mm
1	-∞	4.60	4.60	4.60	-	3053.541	11142003.00	1012000000.	831.287	7539340.500	662750016.0	46.2
2	-∞	8.05	3.45	3.45	-	3053.541	11142003.00	1012000000.	831.287	7539340.500	662750016.0	46.2
3	-∞	12.55	4.50	4.50	-	3053.541	11142003.00	1012000000.	831.287	7539340.500	662750016.0	46.2

6. Supports

coordinates of supports

supp.name	x m	width mm	depth mm	CF kN/m	CM kNm/ -	restraint (F) (M)	
A	0.00	100	1000	fix	----	X	-
B	4.60	111	1000	fix	----	X	-
C	8.05	111	1000	fix	----	X	-
D	12.55	100	1000	fix	----	X	-

7. Action effects



Permanent action effect: permanent loads

3. additive load case: EG

⇒ unif.distr.load: $q = 0.82$ kN/m from $x_a = 0.00$ m to $x_e = 12.55$ m

⇒ unif.distr.load: $q = 1.32$ kN/m from $x_a = 0.00$ m to $x_e = 12.55$ m

2. Transient action effect: live loads (1)

2. additive load case: live loads (1/1)

⇒ unif.distr.load: $q = 10.00$ kN/m from $x_a = 0.00$ m to $x_e = 12.55$ m

8. verifications

1: EC 5 load-carrying capacity

buckling analysis of compression flange acc. to DIN EN 1995, 6.3.2 will be executed
Extreme rule 1

2: EC 5 deformations

Grenzwerte für deformations vom Benutzer definiert!

$w_{inst} \leq l_v / 300$, cantilever: $l_v / 150$

$w_{fin} \leq l_v / 200$, cantilever: $l_v / 100$

$w_{net,fin} \leq l_v / 200$, cantilever: $l_v / 100$

Extreme rule 1

3: EC 5 fire protection

fire resistance duration $t_f = 60$ min

side protected t_{ch} $t_f = t_{ch}$ t_f k_2 d_{ef}

top x 30.00 - 50.00 0.75 31.75

Extreme rule 1: standardkombination

4: EC 5 Verification of vibration

verification of vibration acc. to der Konstruktions- and Bemessungsregeln aus dem Forschungsvorhaben
Winter/Hamm/Richter: "Schwingungs- and Dämpfungsverhalten from timber- and timber-Beton-Verbunddecken"
TU München 2010 modal damping ratio $\xi = 0.00$

Decke innerhalb einer Nutzungseinheit ⇒ $f_{grenz} = 6$ Hz, $w_{grenz} = 1.0$ mm, $a_{grenz} = 0.10$ m/s²

numeric calculation with Fourier series

Attention! Gelenke bleiben unberücksichtigt

Federn werden nur in den Zwischenlagern berücksichtigt

Ohne Berücksichtigung from shear deformation

Poisson's ratio $\nu = 0.00$, torsionstiffness = 0.0 %

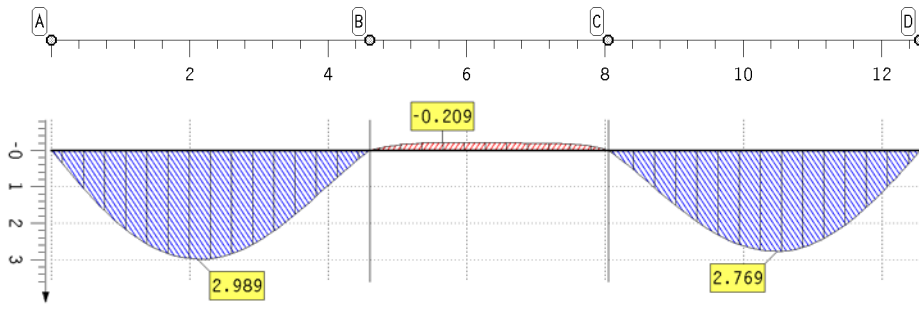
60 mm, $E = 25000$ N/mm², $g = 0.220$ kN/mm², $I_{screed} = 18$ mm⁴

in consideration of 2-dimensional effects

9. Results of load cases

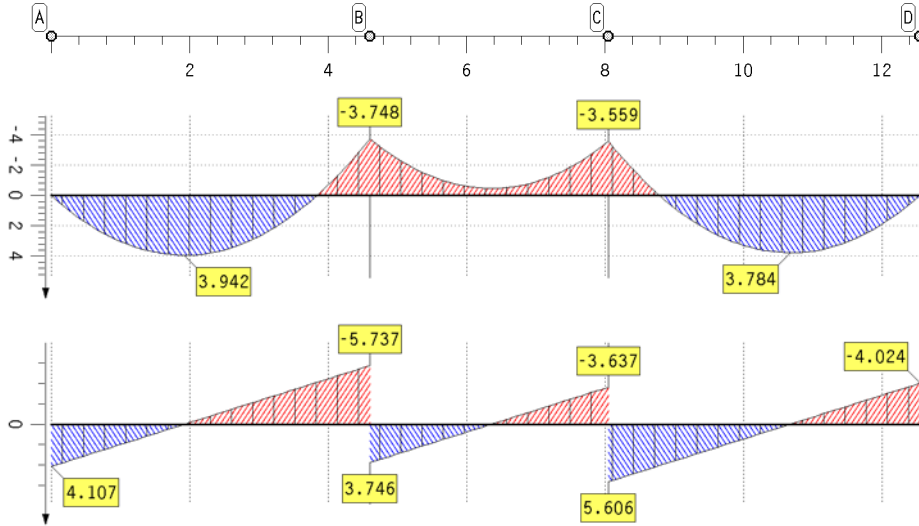
9.1. Action effect 1: load case 3: EG

deflections of main beam (characteristic)



deflection
main beam
characteristic
w in mm
Min: -0.21
Max: 2.99

internal forces and moments



flexural moment
main beam
M in kNm
Min: -3.75
Max: 3.94

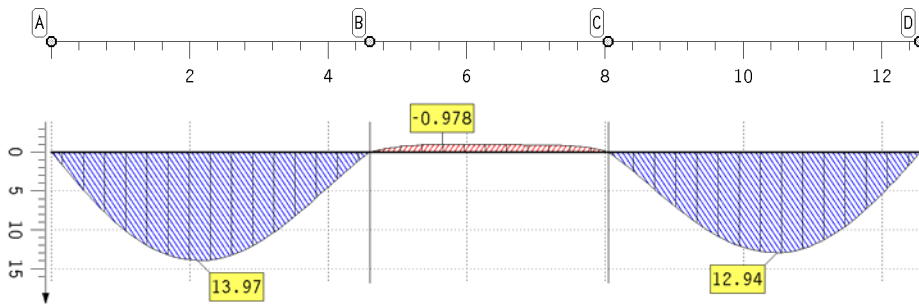
shear force
main beam
V in kN
Min: -5.74
Max: 5.61

support forces

point	x m	AP kN
A	0.000	-4.11
B	4.600	-9.48
C	8.050	-9.24
D	12.550	-4.02

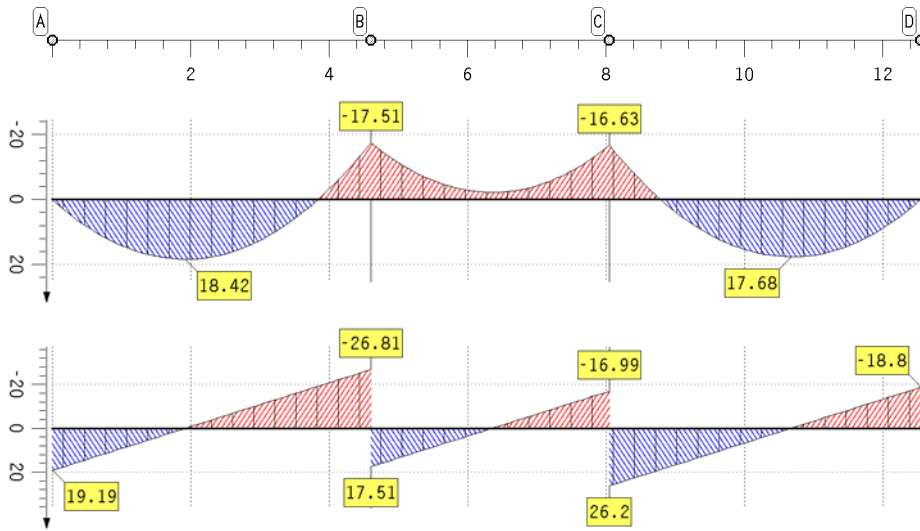
9.2. Action effect 2: load case 2: live loads (1/1)

deflections of main beam (characteristic)



deflection
main beam
characteristic
w in mm
Min: -0.98
Max: 13.97

internal forces and moments



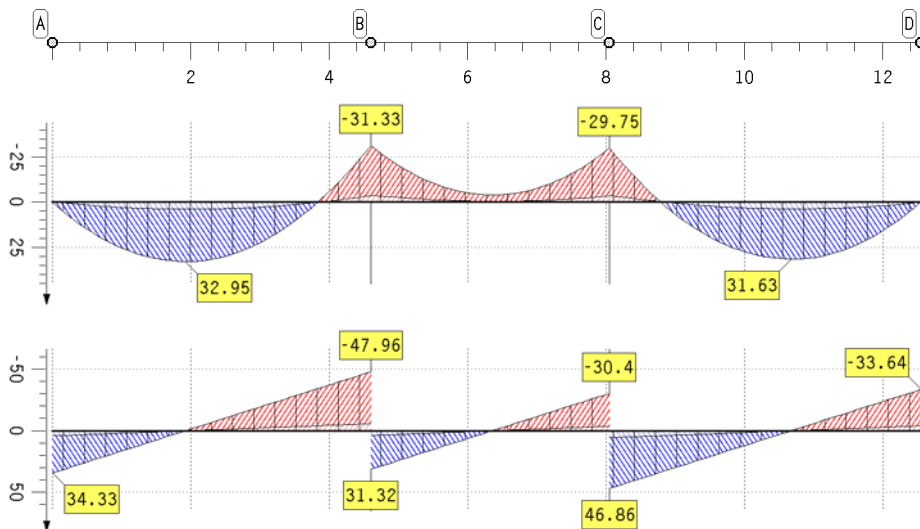
support forces

point	x m	AP kN
A	0.000	-19.19
B	4.600	-44.31
C	8.050	-43.19
D	12.550	-18.80

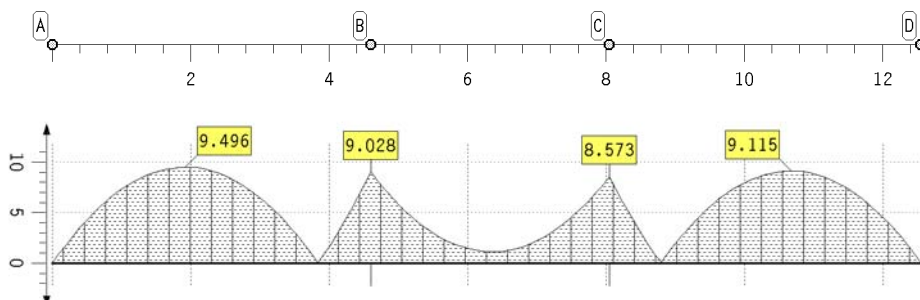
10. Results of verification of ultimate limit state

10.1. Verification of ultimate limit state

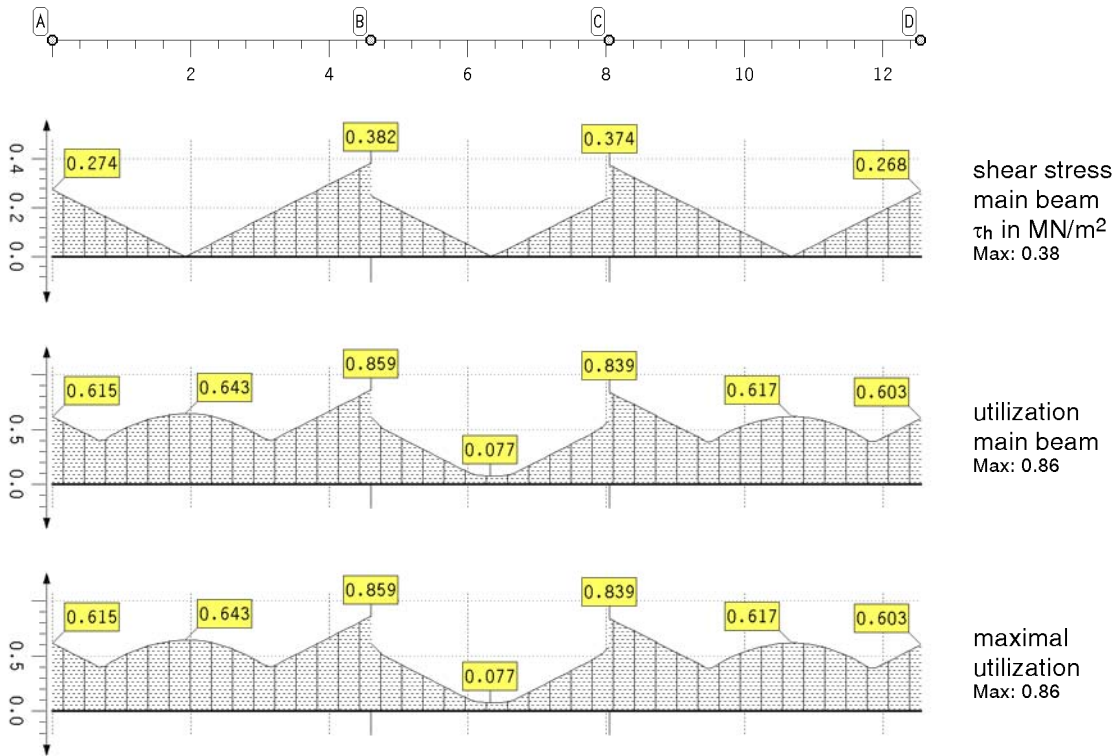
extremal internal forces



results of verification of ultimate limit state



results of verification of ultimate limit state



verification of ultimate limit state of main beam

point	x	k _{mod,h}	σ _h	τ _h	U _h	point	x	k _{mod,h}	σ _h	τ _h	U _h
-	m	-	MN/m ²	MN/m ²	-	-	m	-	MN/m ²	MN/m ²	-
A	0.000	0.000	0.00	0.27	0.615	C	8.050	0.000	8.57	0.24	0.580
	0.671	0.000	5.48	0.18	0.400	C	8.050	0.000	8.57	0.37	0.839
	1.342	0.000	8.64	0.08	0.585		8.800	0.000	0.11	0.27	0.599
	1.917	0.000	9.50	0.00	0.643		9.456	0.000	5.32	0.17	0.389
	2.492	0.000	8.65	0.08	0.586		10.113	0.000	8.32	0.08	0.563
	3.162	0.000	5.51	0.18	0.398		10.675	0.000	9.12	0.00	0.617
	3.833	0.000	0.05	0.27	0.613		11.238	0.000	8.28	0.08	0.561
B	4.600	0.000	9.03	0.38	0.859		11.894	0.000	5.25	0.17	0.392
B	4.600	0.000	9.03	0.25	0.611	D	12.550	0.000	0.00	0.27	0.603
	5.463	0.000	3.16	0.13	0.285	minimum		0.000	0.00	0.00	0.077
	6.325	0.000	1.13	0.00	0.077	maximum		0.000	9.50	0.38	0.859
	7.188	0.000	2.93	0.12	0.268						

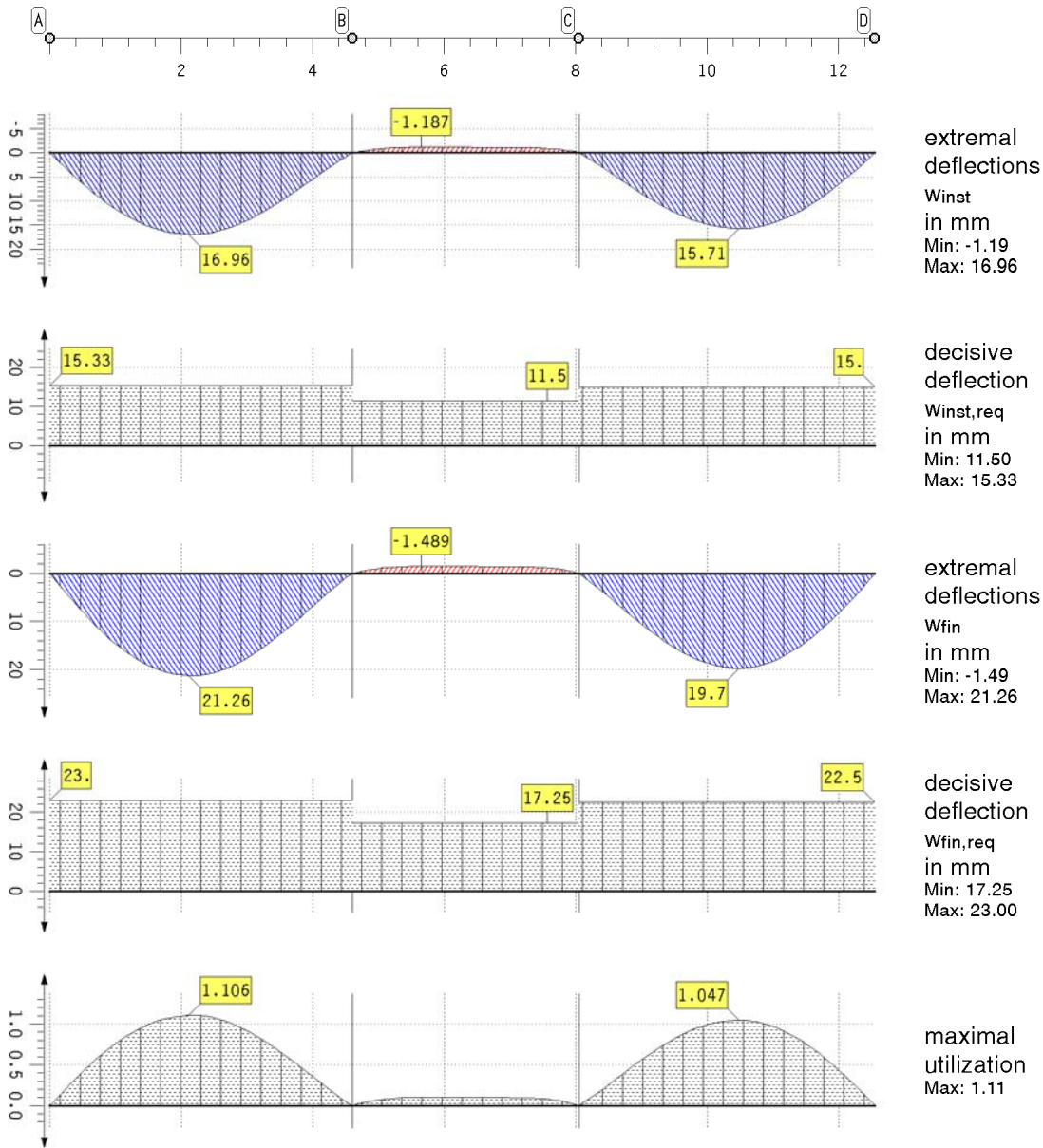
maximal utilization

point	x	U	point	x	U	point	x	U	point	x	U
-	m	-	-	m	-	-	m	-	-	m	-
A	0.000	0.615	B	4.600	0.859	C	8.050	0.839	D	12.550	0.603
	0.671	0.400	B	4.600	0.611		9.456	0.389	minimum		0.077
	1.342	0.585		6.037	0.100		10.113	0.563	maximum		0.859
	1.917	0.643		6.325	0.077		10.675	0.617			
	2.492	0.586		6.708	0.115		11.238	0.561			
	3.162	0.398	C	8.050	0.580		11.894	0.392			

11. Results of verification of deflections

11.1. Verification of deflections

results of verification of deflections



verification of deflections

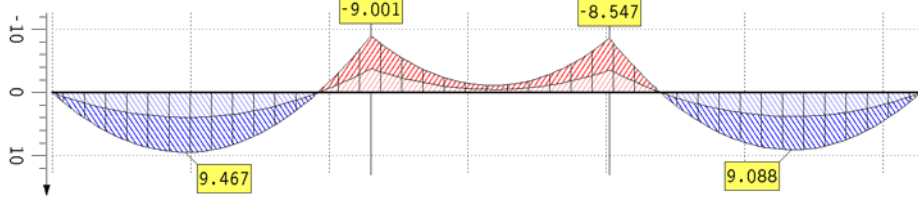
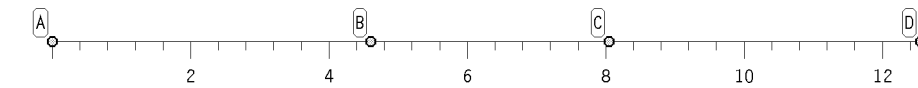
point	x m	min/max/req w_{inst}			min/max/req w_{fin}			min/max/req $w_{net,fin}$			U
		mm	mm	mm	mm	mm	mm	mm	mm	mm	
A	0.000	0.00	0.00	15.33	0.00	0.00	23.00	----	----	----	0.000
	1.150	0.00	12.92	15.33	0.00	16.20	23.00	----	----	----	0.842
	2.108	0.00	16.96	15.33	0.00	21.26	23.00	----	----	----	1.106
	3.067	0.00	13.61	15.33	0.00	17.07	23.00	----	----	----	0.888
B	4.600	0.00	0.00	15.33	0.00	0.00	23.00	----	----	----	0.000
	4.600	0.00	0.00	11.50	0.00	0.00	17.25	----	----	----	0.000
	4.792	-0.50	0.00	11.50	-0.63	0.00	17.25	----	----	----	0.043
	5.079	-0.94	0.00	11.50	-1.18	0.00	17.25	----	----	----	0.082
	5.654	-1.19	0.00	11.50	-1.49	0.00	17.25	----	----	----	0.103
	7.379	-1.03	0.00	11.50	-1.29	0.00	17.25	----	----	----	0.089
	7.762	-0.64	0.00	11.50	-0.80	0.00	17.25	----	----	----	0.056
	8.050	0.00	0.00	11.50	0.00	0.00	17.25	----	----	----	0.000
C	8.050	0.00	0.00	15.00	0.00	0.00	22.50	----	----	----	0.000
	9.550	0.00	12.64	15.00	0.00	15.85	22.50	----	----	----	0.842
	10.488	0.00	15.71	15.00	0.00	19.70	22.50	----	----	----	1.047
	11.425	0.00	11.96	15.00	0.00	15.00	22.50	----	----	----	0.797
D	12.550	0.00	0.00	15.00	0.00	0.00	22.50	----	----	----	0.000
minimum		-1.19	0.00	11.50	-1.49	0.00	17.25	0.00	0.00	0.00	0.000
maximum		0.00	16.96	15.33	0.00	21.26	23.00	0.00	0.00	0.00	1.106



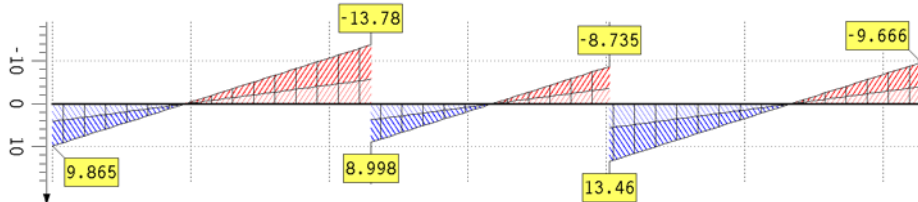
12. Results of verification of fire protection

12.1. Verification of fire protection

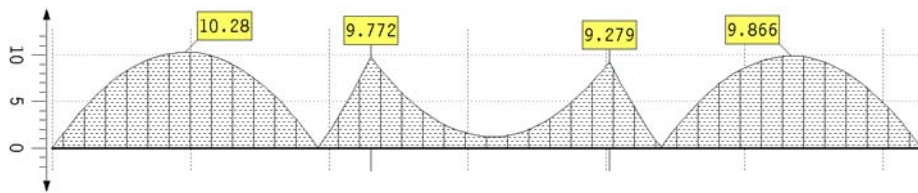
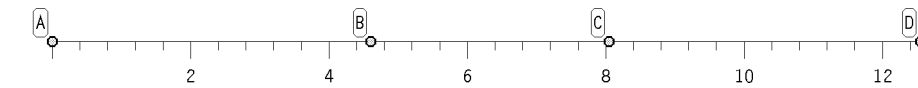
extremal internal forces



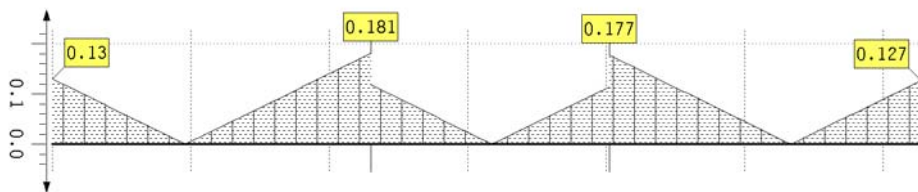
flexural moment
main beam
M in kNm
Min: -9.00
Max: 9.47



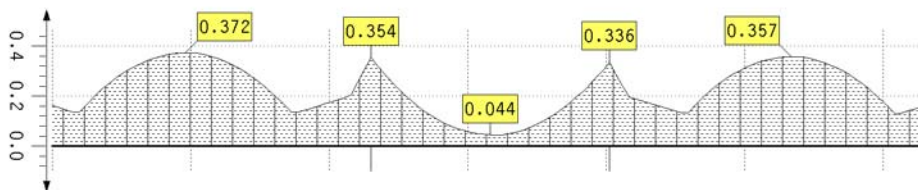
shear force
main beam
V in kN
Min: -13.78
Max: 13.46



bending stress
main beam
 σ_h in MN/m²
Max: 10.28



shear stress
main beam
 τ_h in MN/m²
Max: 0.18



utilization
main beam
Max: 0.37

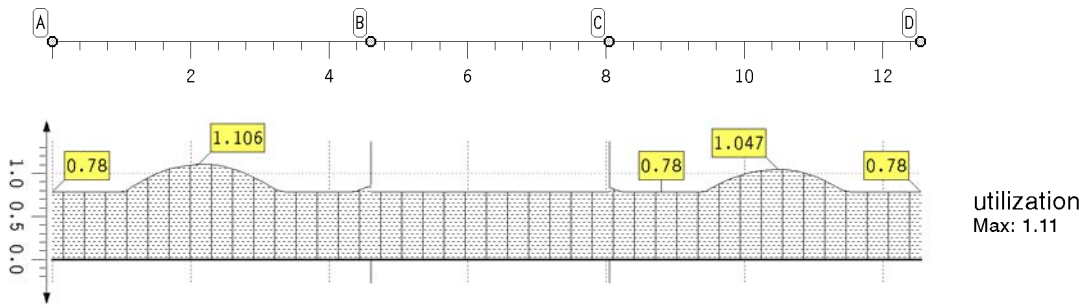
verification of ultimate limit state of main beam

point	x m	$k_{mod,h}$	σ_h MN/m ²	τ_h MN/m ²	U_h	point	x m	$k_{mod,h}$	σ_h MN/m ²	τ_h MN/m ²	U_h
A	0.000	0.000	0.00	0.13	0.161	C	8.050	0.000	9.28	0.11	0.336
	0.383	0.000	3.70	0.10	0.134		8.050	0.000	9.28	0.18	0.336
	1.150	0.000	8.63	0.05	0.313		8.331	0.000	5.39	0.16	0.196
	1.917	0.000	10.28	0.00	0.372		8.800	0.000	0.11	0.13	0.157
	2.683	0.000	8.65	0.05	0.313		9.175	0.000	3.63	0.10	0.132
	3.450	0.000	3.74	0.10	0.136		9.925	0.000	8.32	0.05	0.301
	3.833	0.000	0.06	0.13	0.161		10.675	0.000	9.87	0.00	0.357
	4.312	0.000	5.70	0.16	0.207		11.425	0.000	8.27	0.05	0.300
B	4.600	0.000	9.77	0.18	0.354	12.175	0.000	3.54	0.10	0.128	
	4.600	0.000	9.77	0.12	0.354	D	12.550	0.000	0.00	0.13	0.158
B	5.463	0.000	3.42	0.06	0.124	minimum	0.000	0.00	0.00	0.044	
	6.325	0.000	1.22	0.00	0.044	maximum	0.000	10.28	0.18	0.372	
B	7.188	0.000	3.18	0.06	0.115						

13. Summary

13.1. Summary of all verifications

maximal utilization



13.2. Eigenfrequenz

$EI_{\text{längs}} = 3.503541 \text{ MNm}^2/\text{m}$, $EI_{\text{quer}} = 1.151125 \text{ MNm}^2/\text{m}$

$f_e = 11.036 \text{ Hz} \geq f_e = 6 \text{ Hz} \Rightarrow \text{Kriterium successful!}$

13.3. Steifigkeitskriterium

Raumbreite $b = 1.000 \text{ m}$, $b_{\text{ef}} = 1.000 \text{ m}$, $x_{\text{max F}} = 2.119 \text{ m}$, $x_{\text{max w}} = 2.119 \text{ m} \Rightarrow w_{\text{max}} = 0.390 \text{ mm}$

$w(2\text{kN}) = 0.78 \text{ mm} \leq w_{\text{grenz}} = 1.0 \text{ mm} \Rightarrow \text{Kriterium successful!}$

13.4. Konstruktive Anforderungen

Schwimmende supportung des screeds ist unbedingt erforderlich!

Nach [Winter/Hamm/Richter], TU München 2010 gilt:

Nassestriche sind aufgrund ihrer höheren Masse and höheren Steifigkeit gegenüber Trockenestrichen günstiger zu bewerten, was das Schwingungsverhalten der Decken betrifft.

Eine (möglichst schwere) Schüttung verbessert das Schwingungsverhalten.

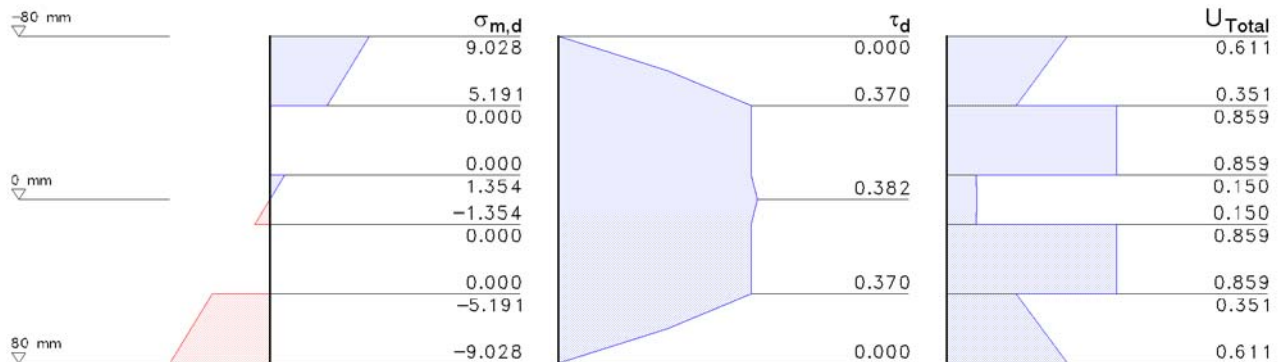
Je schwerer die Schüttung, desto größer die Verbesserung der subjektiven Bewertung. Als schwere Schüttung werden Schüttungen with einem areangewicht from mindestens 60 kg/m^2 bezeichnet.

14. Utilizations of all verifications

verification der deformations ($u = 1.106$) does not meet the requirements!

15. Detailed verification piont

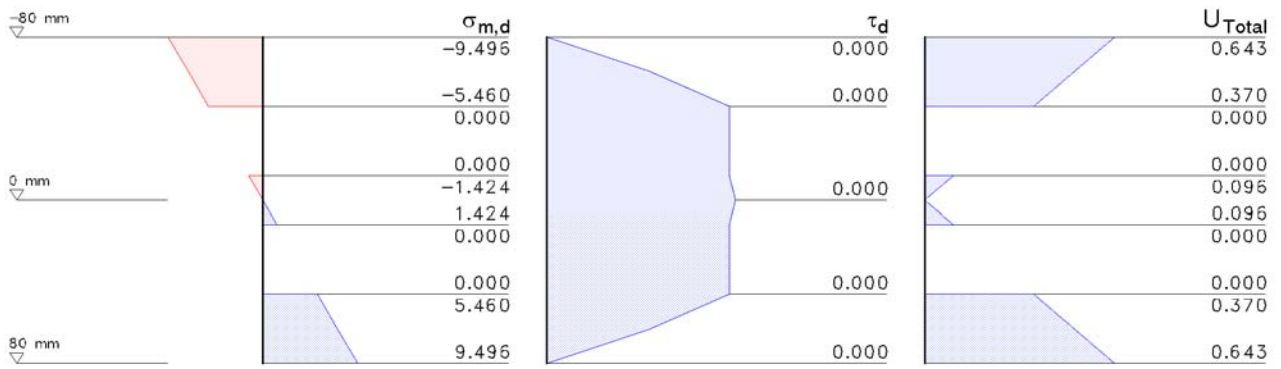
15.1. Verification of load-carrying capacity at $x = 4.60 \text{ m}$, $\max V_d = -5.74 \text{ kN}$, $\min M_d = -31.33 \text{ kNm}$, $\max M_d = -3.75 \text{ kNm}$



mechanical resistance and static terms: stiffness $B_x = 3053.541 \text{ Nmm}$

z [mm]	ES_x [Nmm]	$\sigma_{m,d}$ [N/mm ²]	$f_{m,d}$ [N/mm ²]	$\tau_{v,d}$ [N/mm ²]	$f_{v,d}$ [N/mm ²]	z [mm]	ES_x [Nmm]	$\sigma_{m,d}$ [N/mm ²]	$f_{m,d}$ [N/mm ²]	$\tau_{v,d}$ [N/mm ²]	$f_{v,d}$ [N/mm ²]
80.0	0.000	-9.028	14.77	0.000	2.46	-12.0	-23.562	0.000	14.77	0.370	0.43
63.0	-13.370	-7.110	14.77	0.210	2.46	-29.0	-23.562	0.000	14.77	0.370	0.43
46.0	-23.562	0.000	14.77	0.370	0.43	-46.0	-23.562	5.191	14.77	0.370	2.46
29.0	-23.562	0.000	14.77	0.370	0.43	-63.0	-13.370	7.110	14.77	0.210	2.46
12.0	-23.562	-1.354	14.77	0.370	2.46	-80.0	0.000	9.028	14.77	0.000	2.46
0.0	-24.354	-0.000	14.77	0.382	2.46						

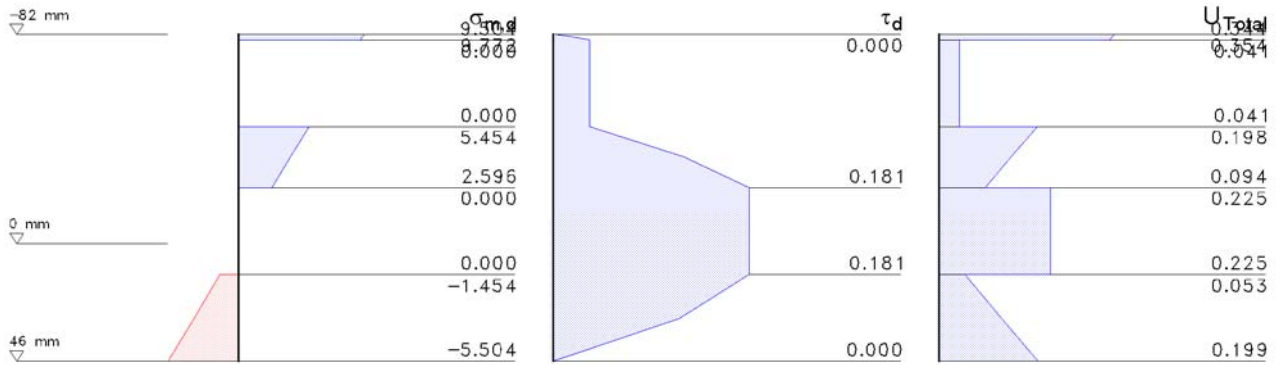
15.2. Verification of load-carrying capacity at $x = 1.92 \text{ m}$, $\max V_d = 0.05 \text{ kN}$, $\min M_d = 3.94 \text{ kNm}$, $\max M_d = 32.95 \text{ kNm}$



mechanical resistance and static terms: stiffness $B_x = 3053.541 \text{ Nmm}$

Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²	Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²
80.0	0.000	9.496	14.77	0.000	2.46	-12.0	-23.562	0.000	14.77	0.000	0.43
63.0	-13.370	7.478	14.77	0.000	2.46	-29.0	-23.562	0.000	14.77	0.000	0.43
46.0	-23.562	0.000	14.77	0.000	0.43	-46.0	-23.562	-5.460	14.77	0.000	2.46
29.0	-23.562	0.000	14.77	0.000	0.43	-63.0	-13.370	-7.478	14.77	0.000	2.46
12.0	-23.562	1.424	14.77	0.000	2.46	-80.0	0.000	-9.496	14.77	0.000	2.46
0.0	-24.354	0.000	14.77	0.000	2.46						

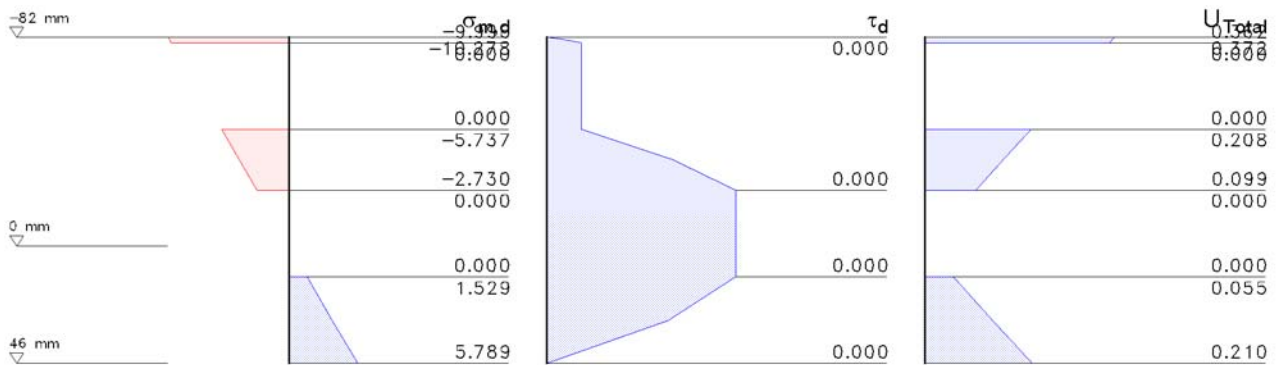
15.3. Resistance to fire at $x = 4.60 \text{ m}$, $\max V_d = -5.74 \text{ kN}$, $\min M_d = -9.00 \text{ kNm}$, $\max M_d = -3.75 \text{ kNm}$



mechanical resistance and static terms: stiffness $B_x = 831.287 \text{ Nmm}$

Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²	Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²
46.2	0.000	-5.504	27.60	0.000	4.60	-45.8	-2.003	0.000	27.60	0.033	0.81
29.2	-7.051	-3.479	27.60	0.117	4.60	-62.8	-2.003	0.000	27.60	0.033	0.81
12.2	-10.924	0.000	27.60	0.181	0.81	-79.8	-2.003	9.504	27.60	0.033	4.60
-4.8	-10.924	0.000	27.60	0.181	0.81	-80.9	-1.008	9.638	27.60	0.017	4.60
-21.8	-10.924	2.596	27.60	0.181	4.60	-82.0	0.000	9.772	27.60	0.000	4.60
-33.8	-7.255	4.025	27.60	0.120	4.60						

15.4. Resistance to fire at $x = 1.92 \text{ m}$, $\max V_d = 0.01 \text{ kN}$, $\min M_d = 3.94 \text{ kNm}$, $\max M_d = 9.47 \text{ kNm}$



mechanical resistance and static terms: stiffness $B_x = 831.287 \text{ Nmm}$

Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²	Z mm	ES _x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²
46.2	0.000	5.789	27.60	0.000	4.60	-21.8	-10.924	-2.730	27.60	0.000	4.60
29.2	-7.051	3.659	27.60	0.000	4.60	-33.8	-7.255	-4.233	27.60	0.000	4.60
12.2	-10.924	0.000	27.60	0.000	0.81	-45.8	-2.003	0.000	27.60	0.000	0.81
-4.8	-10.924	0.000	27.60	0.000	0.81	-62.8	-2.003	0.000	27.60	0.000	0.81

mechanical resistance and static terms: stiffness $B_x = 831.287 \text{ Nmm}$

z mm	ES_x Nmm	$\sigma_{m,d}$ N/mm ²	$f_{m,d}$ N/mm ²	$\tau_{v,d}$ N/mm ²	$f_{v,d}$ N/mm ²
-79.8	-2.003	-9.996	27.60	0.000	4.60
-80.9	-1.008	-10.137	27.60	0.000	4.60
-82.0	0.000	-10.278	27.60	0.000	4.60