

1. Options for Calculations

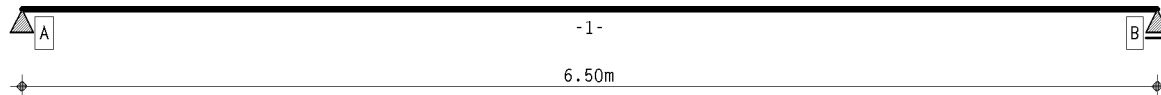
calculation DIN EN 1995:2010, Germany

service class 2

coefficient of thermal expansion for timber $\alpha_t = 0.500 \cdot 10^{-5}/^{\circ}\text{K}$

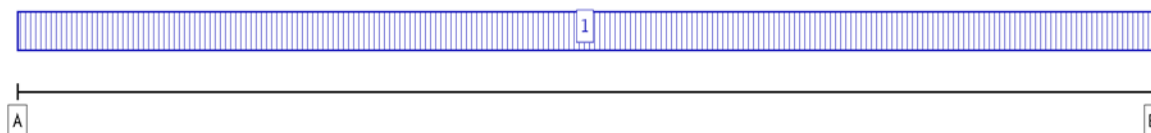
$\psi_2 = 0.60$ (factor acc. to DIN EN 1995-1-1 2.3.2.2 (2))

2. Structural system

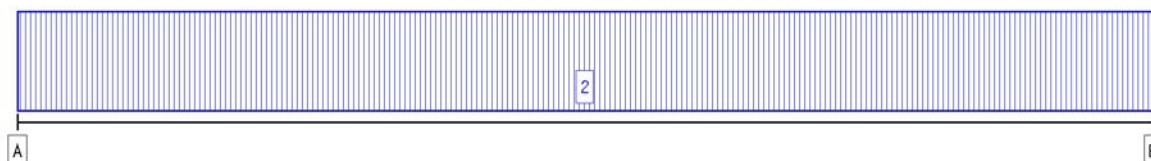


main beam

3. Loading



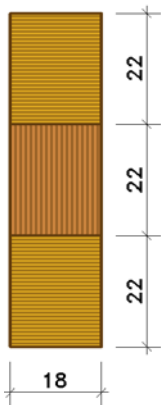
action effect 1: permanent loads (permanent, 1 load cases)



action effect 2: live loads (1) (transient, 1 load cases)

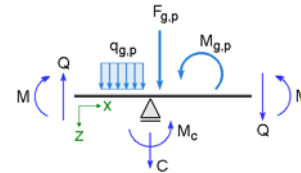
4. main beam

section scale 1:15



timber grade top flange	solid coniferous timber, C24 (S10)
char. bend. strength $f_{m,k}$	: 24.0 N/mm ²
char. shear strength $f_{v,k}$	: 4.0 N/mm ²
char. ten. strength $f_{t,k}$	: 14.5 N/mm ²
char. compr. strength $f_{c,0,k}$	: 21.0 N/mm ²
char. compr. strength $f_{c,90,k}$	: 2.5 N/mm ²
modulus of elasticity $E_{0,mean}$	: 11000 N/mm ²
Dichte ρ_k/ρ_m	: 350 / 420 kg/m ³
deformation factor k_{def}	: 0.60 -
area A_{flange}	: 396.000 cm ²
moment of inertia I_{flange}	: 15972.000 cm ⁴
timber grade web	solid coniferous timber, C24 (S10)
char. bend. strength $f_{m,k}$	: 24.0 N/mm ²
char. shear strength $f_{v,k}$	: 4.0 N/mm ²
char. ten. strength $f_{t,k}$	: 14.5 N/mm ²
char. compr. strength $f_{c,0,k}$	: 21.0 N/mm ²
char. compr. strength $f_{c,90,k}$	: 2.5 N/mm ²
k_{cr}	: 0.50 mm ² /N
modulus of elasticity $E_{0,mean}$	: 11000 N/mm ²
Dichte ρ_k/ρ_m	: 350 / 420 kg/m ³
deformation factor k_{def}	: 0.60 -
area A_{flange}	: 396.000 cm ²
moment of inertia I_{flange}	: 15972.000 cm ⁴
timber grade bottom flange	solid coniferous timber, C24 (S10)
char. bend. strength $f_{m,k}$	: 24.0 N/mm ²
char. shear strength $f_{v,k}$	: 4.0 N/mm ²
char. ten. strength $f_{t,k}$	: 14.5 N/mm ²
char. compr. strength $f_{c,0,k}$	: 21.0 N/mm ²
char. compr. strength $f_{c,90,k}$	: 2.5 N/mm ²
modulus of elasticity $E_{0,mean}$	: 11000 N/mm ²
Dichte ρ_k/ρ_m	: 350 / 420 kg/m ³
deformation factor k_{def}	: 0.60 -

area A_{flange} : 396.000 cm²
moment of inertia I_{flange} : 15972.000 cm⁴
definition of internal forces and moments:



5. Beam sections

beam sections

section	x_A m	x_E m	l m	l_v m	cantil.	s_{ef} mm
1	0.00	6.50	6.50	6.50	-	100.0

stiffness values serviceability initial state

section	γ_2 -	a_2 mm	K_1 N/mm	γ_{1r} -	a_1 mm	K_3 N/mm	γ_3 -	a_3 mm	$E I_{ef,inst}$ Nmm ²	ϕ k_{def} -
1	1.0000	-0.0	7485	0.4238	-220.0	7485	0.4238	220.0	2.3141E13	0.5269

stiffness values load-carrying capacity initial state

section	γ_2 -	a_2 mm	K_1 N/mm	γ_1 -	a_1 mm	K_3 N/mm	γ_3 -	a_3 mm	$E I_{ef,inst}$ Nmm ²	$I_{ef,inst}$ mm ²	$h_{q,inst}$ mm	$A_{q,inst}$ mm
1	1.0000	0.0	4990	0.3290	-220.0	4990	0.3290	220.0	1.9144E13	1740407680.	11.00	792.00

stiffness values load-carrying capacity final state

section	γ_2 -	a_2 mm	K_1 N/mm	γ_1 -	a_1 mm	K_3 N/mm	γ_3 -	a_3 mm	$E I_{ef,inf}$ Nmm ²	$I_{ef,inf}$ mm ²	$h_{q,inf}$ mm	$A_{q,inf}$ mm
1	1.0000	0.0	2901	0.2794	-220.0	2901	0.2794	220.0	1.2538E13	1550182400.	11.00	792.00

net section properties

section	$A_{n,2}$ cm ²	$W_{n,2}$ cm ³	$I_{n,2}$ cm ⁴	$A_{n,1}$ cm ²	$W_{n,1}$ cm ³	$I_{n,1}$ cm ⁴	$A_{n,3}$ cm ²	$W_{n,3}$ cm ³	$I_{n,3}$ cm ⁴
1	308.00	1452.00	15972.00	352.00	1452.00	15972.00	352.00	1452.00	15972.00

6. Fasteners

section 1 from $x_A = 0.00$ m to $x_E = 6.50$

bolt 20 mm, FK 4.6 as fitted bolt

2-row with $a_1 = 100.0$ mm

2 - row with $a_2 = 60.0$ mm, simplified verification acc. to NA.8.2.4

$f_{uk} = 400$ N/mm², $M_{yk} = 289640$ Nmm

$K_{ser} = 7485$ N/mm, $\gamma_M = 1.10$, $R_k = 16309.7$ N, all values per shear plane

7. Supports

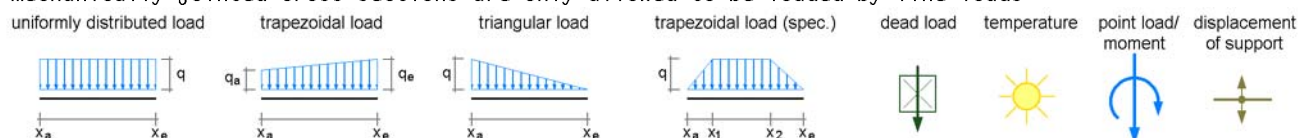
coordinates of supports

supp.name	x m	width mm	depth mm	c_F kN/m	c_M kNm/-	restraint (F) (M)
A	0.00	150	180	fix	----	X -
B	6.50	150	180	fix	----	X -

8. Action effects

Attention! Acc. to DIN EN 1995-1-1, annex B.1

mechanically jointed cross-sections are only allowed to be loaded by line loads



Permanent action effect: permanent loads

1. additive load case: dead load (1)

⇒ unif.distr.load: $q = 4.00$ kN/m from $x_a = 0.00$ m to $x_e = 6.50$ m

2. Transient action effect: live loads (1)

2. additive load case: live loads (1/1)

⇒ unif.distr.load: $q = 8.00$ kN/m from $x_a = 0.00$ m to $x_e = 6.50$ m

9. verifications

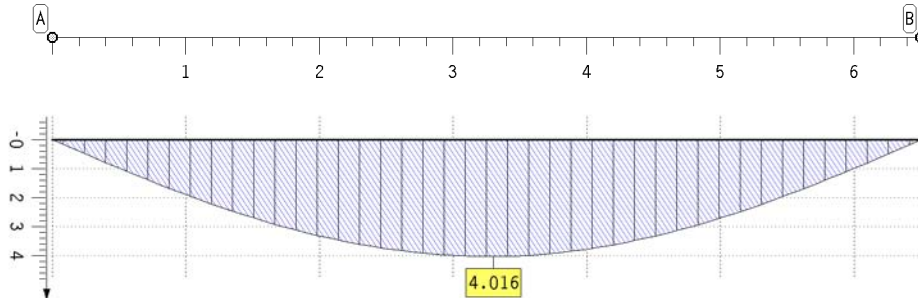
1: EC 5 load-carrying capacity

verification of bearing stress DIN EN 1995, 6.1.5 will be executed
Extreme rule 1

10. Results of action effects

10.1. Action effect 1: permanent loads

extremal deflections of main beam (characteristic)

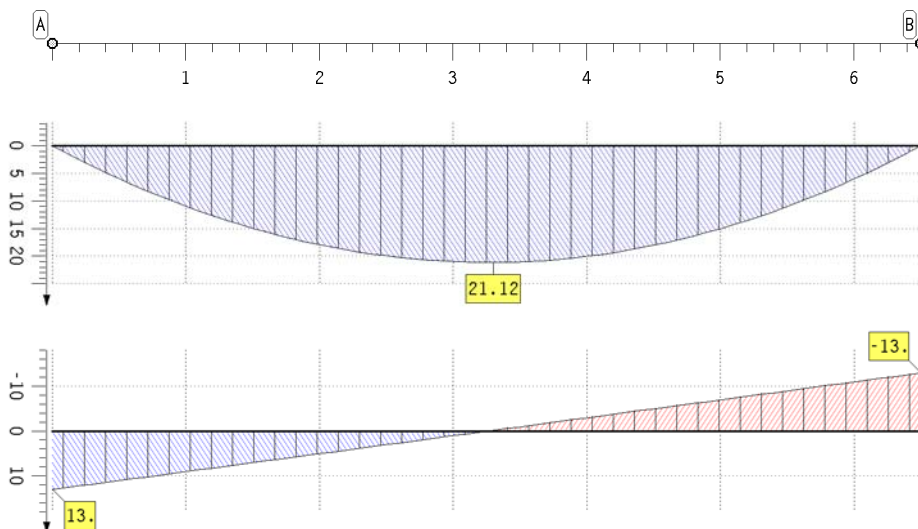


deflection
main beam
characteristic
w in mm
Min: -0.00
Max: 4.02

extremal deflections of main beam (characteristic)

point	x	min w	max w	point	x	min w	max w
-	m	mm	mm	-	m	mm	mm
A	0.000	0.00	0.00	B	6.500	-0.00	-0.00
	1.800	3.09	3.09	minimum		-0.00	-0.00
	3.200	4.02	4.02	maximum		4.02	4.02
	4.700	3.09	3.09				

extremal internal forces



flexural moment
main beam
M in kNm
Min: 0.00
Max: 21.12

shear force
main beam
V in kN
Min: -13.00
Max: 13.00

extremal internal forces

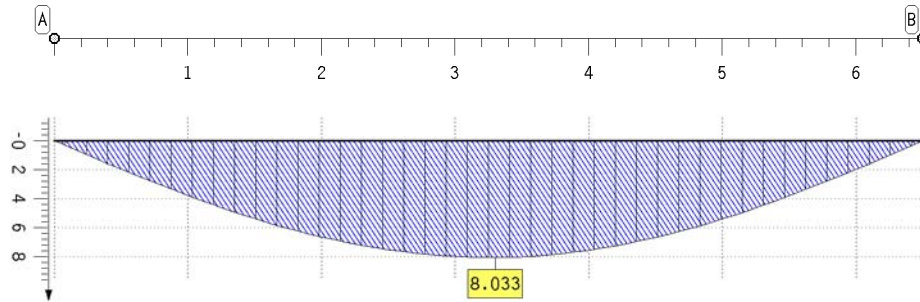
point	x	min M	max M	min V	max V	point	x	min M	max M	min V	max V
-	m	kNm	kNm	kN	kN	-	m	kNm	kNm	kN	kN
A	0.000	0.00	0.00	13.00	13.00	B	6.500	0.00	0.00	-13.00	-13.00
	1.600	15.68	15.68	6.60	6.60	minimum		0.00	0.00	-13.00	-13.00
	3.200	21.12	21.12	0.20	0.20	maximum		21.12	21.12	13.00	13.00
	4.900	15.68	15.68	-6.60	-6.60						

extremal support forces

point	x	min AP	max AP
-	m	kN	kN
A	0.000	-13.00	-13.00
B	6.500	-13.00	-13.00

10.2. Action effect 2: live loads (1)

extremal deflections of main beam (characteristic)

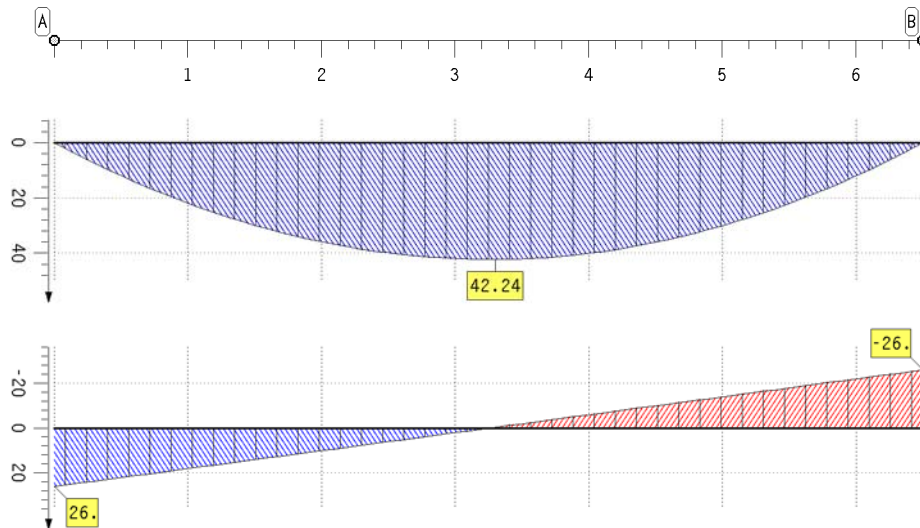


deflection
main beam
characteristic
w in mm
Min: -0.00
Max: 8.03

extremal deflections of main beam (characteristic)

point	x	min w	max w	point	x	min w	max w
-	m	mm	mm	-	m	mm	mm
A	0.000	0.00	0.00	B	6.500	-0.00	-0.00
	1.800	0.00	6.18	minimum		-0.00	0.00
	3.200	0.00	8.03	maximum		0.00	8.03
	4.700	0.00	6.18				

extremal internal forces



flexural moment
main beam
M in kNm
Min: 0.00
Max: 42.24

shear force
main beam
V in kN
Min: -26.00
Max: 26.00

extremal internal forces

point	x	min M	max M	min V	max V	point	x	min M	max M	min V	max V
-	m	kNm	kNm	kN	kN	-	m	kNm	kNm	kN	kN
A	0.000	0.00	0.00	0.00	26.00	B	6.500	0.00	0.00	-26.00	-0.00
	1.600	0.00	31.36	0.00	13.20	minimum		0.00	0.00	-26.00	-0.00
	3.200	0.00	42.24	0.00	0.40	maximum		0.00	42.24	0.00	26.00
	4.900	0.00	31.36	-13.20	-0.00						

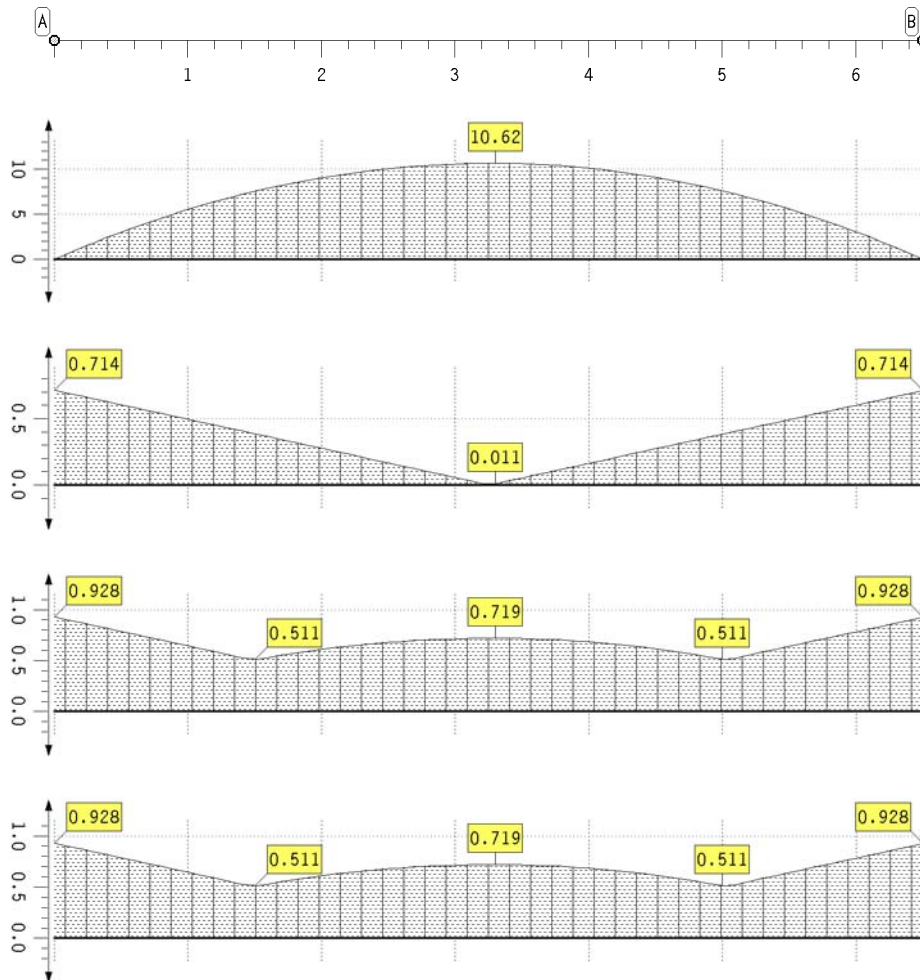
extremal support forces

point	x	min AP	max AP
-	m	kN	kN
A	0.000	-26.00	-0.00
B	6.500	-26.00	-0.00

11. Results of verification of ultimate limit state

11.1. Verification of ultimate limit state

results of verification of ultimate limit state



bending stress
main beam
 σ_h in MN/m²
Max: 10.62

shear stress
main beam
 τ_h in MN/m²
Max: 0.71

utilization
main beam
Max: 0.93

maximal
utilization
Max: 0.93

maximal utilization

point	x	U	point	x	U	point	x	U
-	m	-	-	m	-	-	m	-
A	0.000	0.928		3.200	0.719	B	6.500	0.928
	1.500	0.511		4.100	0.670	minimum		0.511
	2.400	0.670		5.000	0.511	maximum		0.928

extremal support forces

point	x	min AP	max AP
-	m	kN	kN
A	0.000	-56.55	-13.00
B	6.500	-56.55	-13.00

verification of bearing stress

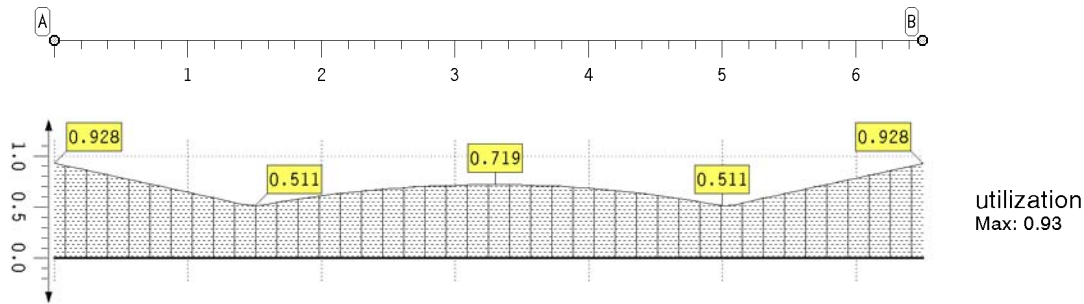
support	l_{ef}	A_{ef}	A_P	k_{c90}	k_{mod}	f_{c90d}	σ_{c90d}	u
	mm	mm ²	N			N/mm ²	N/mm ²	-
A	180	32400	56550	1.00	0.80	1.54	1.75	1.13
B	180	32400	56550	1.00	0.80	1.54	1.75	1.13

verification of bearing stresses für den main beam(u = 1.134) does not meet the requirements!

12. Summary

12.1. Summary of all verifications

maximal utilization



maximal utilization

point	x	U	point	x	U	point	x	U
-	m	-	-	m	-	-	m	-
A	0.000	0.928		3.200	0.719	B	6.500	0.928
	1.500	0.511		4.100	0.670	minimum		0.511
	2.400	0.670		5.000	0.511	maximum		0.928

verification of bearing stress

support	l_{ef}	A_{ef}	A_p	k_{c90}	k_{mod}	f_{c90d}	σ_{c90d}	u
	mm	mm ²	N	-	-	N/mm ²	N/mm ²	-
A	180	32400	56550	1.00	0.80	1.54	1.75	1.13
B	180	32400	56550	1.00	0.80	1.54	1.75	1.13

verification of bearing stresses für den main beam(u = 1.134) does not meet the requirements!

13. Utilizations of all verifications

verification of load-carrying capacity (u = 1.134) does not meet the requirements!

14. Detailed verification piont

14.1. Verification of load-carrying capacity at x = 0.00 m

internal forces and moments

state	M	V	M ₁	N ₁	M ₂	N ₂	M ₃	N ₃
	kNm	kN	Nmm	N	Nmm	N	Nmm	N
start,min	0.00	13.00	0	-0	0	-0	0	0
start,max	0.00	56.55	0	-0	0	-0	0	0
end,min	0.00	13.00	0	-0	0	-0	0	0
end,max	0.00	56.55	0	-0	0	-0	0	0

stresses and utilization web

state	$k_{mod,2}$	$\sigma_{m,2}$	$\sigma_{c,2}$	$u_{\sigma,2}$	τ_2	u_{τ}	u_2
	-	N/mm ²	N/mm ²	-	N/mm ²	-	-
start	0.8	0.00	0.00	0.00	0.71	0.29	0.29
end	0.8	0.00	0.00	0.00	0.71	0.29	0.29

stresses and utilization flanges

state	$k_{mod,1}$	$\sigma_{m,1}$	$\sigma_{c,1}$	u_1	$k_{mod,3}$	$\sigma_{m,3}$	$\sigma_{c,3}$	u_3
	-	N/mm ²	N/mm ²	-	-	N/mm ²	N/mm ²	-
start	0.8	0.00	-0.00	0.00	0.8	0.00	0.00	0.00
end	0.8	0.00	-0.00	0.00	0.8	0.00	0.00	0.00

fastener

state	$F_{1,d}$	$u_{1,d}$
	N	-
start	-9314	0.93
end	-8880	0.88

resulting utilization at verification point $u_{res} = 0.928$