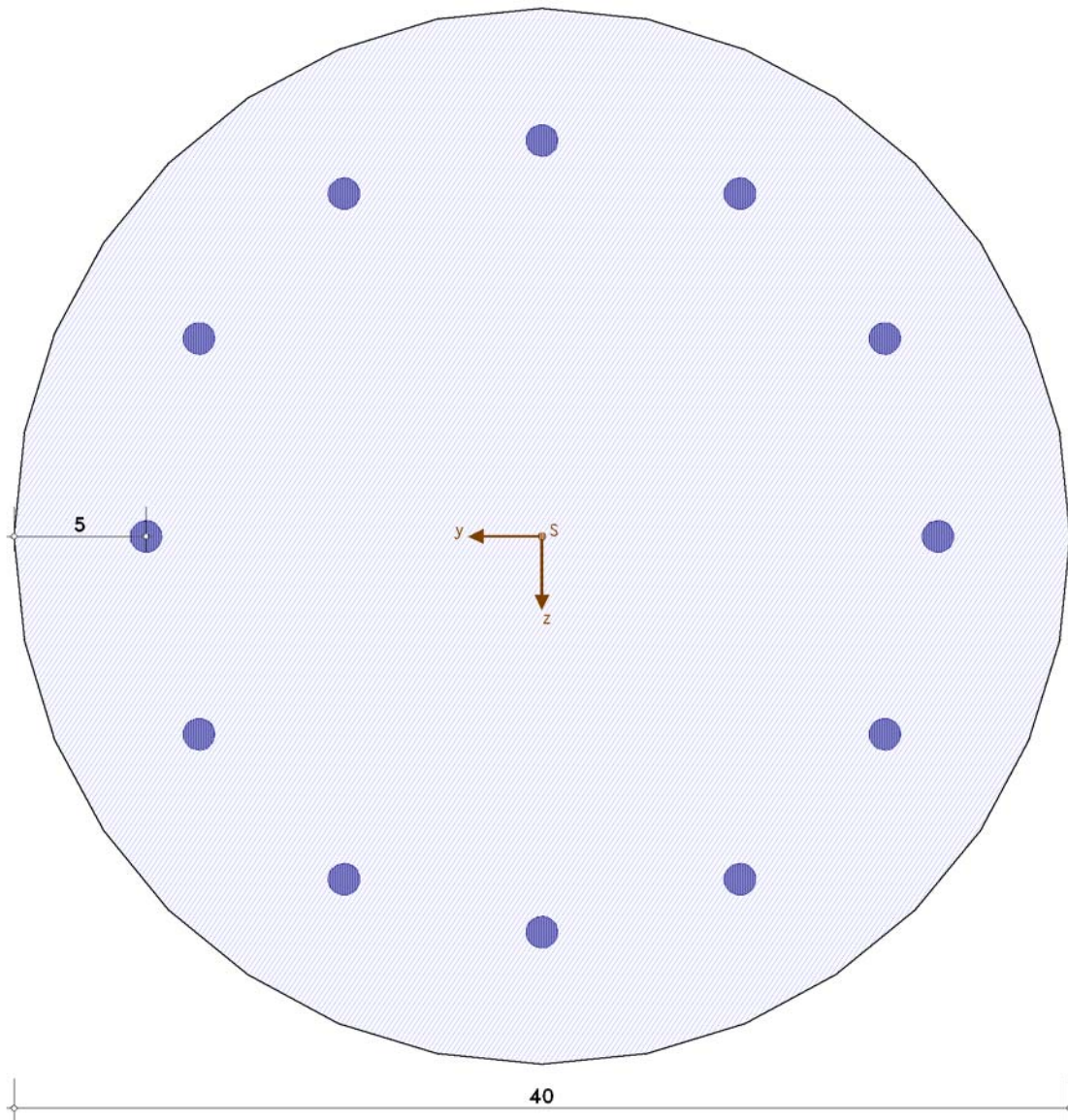


# POS. 34: KREISQUERSCHNITT

reinforced concrete design EC 2 (1.11), NA: Deutschland

4H-EC2QB Version: 10/2023-1b

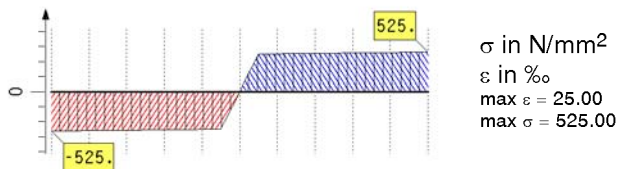
## 1. input protocol



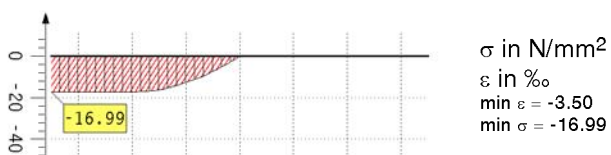
### 1.1. building material

reinforcing steel B500A, concrete C30/37

stress-strain line of reinforcing steel: EC 2-1-1, 3.2.7 (bilinear)



stress-strain line of concrete: EC 2-1-1, 3.1.7 (parabola-rectangle diagram)



## 1.2. material safety factors

design situation: basic combination

design resistance: concrete  $\gamma_c = 1.50$ , reinforcement  $\gamma_s = 1.15$

## 1.3. cross section

circle:  $r = 20.0$  cm, center distance:  $d_a = 5.0$  cm

base reinforcement:  $A_{sa0} = 12 \text{ } \varnothing 12 = 13.57 \text{ cm}^2$

max. reinforcement ratio  $\rho_s = 8.00\%$

## 1.4. durability and concrete cover

internal: minimum strength class, concrete cover for  $\varnothing_s = 8$  mm

due to reinforcement corrosion X0  $\Rightarrow$  C12/15,  $c_{min} = 10$  mm,  $\Delta c = 10$  mm,  $c_{nom} = c_{min} + \Delta c = 20$  mm

minimum concrete quality C12/15 with  $f_{ck} = 12.0 \text{ N/mm}^2 < 30.0 \text{ N/mm}^2$  ok

minimum axial spacing  $\min d = c_{nom} + \varnothing_s/2 = 24$  mm  $<$  clc  $d = 30$  mm ok

external: minimum strength class, concrete cover for  $\varnothing_s = 12$  mm

due to reinforcement corrosion X0  $\Rightarrow$  C12/15,  $c_{min} = \varnothing_s = 12$  mm,  $\Delta c = 10$  mm,  $c_{nom} = c_{min} + \Delta c = 22$  mm

minimum concrete quality C12/15 with  $f_{ck} = 12.0 \text{ N/mm}^2 < 30.0 \text{ N/mm}^2$  ok

minimum axial spacing  $\min d = c_{nom} + \varnothing_s/2 = 28$  mm  $<$  clc  $d = 50$  mm ok

## 1.5. design parameters

### 1.5.1. bending/shear design

#### 1.5.1.1. bending design

minimum reinforcement for columns

tension reinforcement only, do not consider base reinforcement statically

minimum center of compression normal force

#### 1.5.1.2. shear design

reinforcing steel like flexural reinforcement

shear force

angle of the shear force reinforcement  $\alpha = 90^\circ$

simplified approach of the compression strut angle

with minimum reinforcement (beam)

inner lever arm from bending design  $z \leq d - 2 \cdot c_{v,l} \leq d - c_{v,l} - 3$  cm

with concrete cover to longitudinal reinforcement in the compress. zone  $c_{v,l} = 3.0$  cm

limit the design value of the shear force resistance without shear force reinforcement  $V_{Rd,c}$

effectiveness factor for circle design  $\alpha_k = 0.800$

#### 1.5.1.3. design calculation values

| lc | $N_{Ed}$<br>kN | $M_{y,Ed}$<br>kNm | $V_{z,Ed}$<br>kN | $M_{z,Ed}$<br>kNm | $V_{y,Ed}$<br>kN |             |
|----|----------------|-------------------|------------------|-------------------|------------------|-------------|
| 1  | -742.03        | 39.43             | -9.86            | -174.55           | -38.24           | Import lc 1 |
| 2  | -96.56         | -270.04           | 52.51            | 24.01             | 6.00             | Import lc 2 |
| 3  | -691.63        | 34.01             | -8.50            | -266.32           | -57.58           | Import lc 3 |
| 4  | -655.63        | 39.43             | -9.86            | -29.08            | -7.27            | Import lc 4 |
| 5  | -240.56        | -270.04           | 52.51            | -218.45           | -45.61           | Import lc 5 |
| 6  | -218.99        | 15.83             | -3.96            | -8.68             | -2.17            | Import lc 6 |
| 7  | -668.58        | -132.09           | 24.02            | -154.94           | -33.33           | Import lc 7 |
| 8  | -534.56        | -255.29           | 48.82            | -232.62           | -49.16           | Import lc 8 |
| 9  | -253.63        | 19.26             | -4.81            | -9.69             | -2.42            | Import lc 9 |

### 1.5.2. fire design

fire design with Gl.(5.7), EC 2-1-2

fire resistance class R 90

replacement length of the column in case of fire  $l_{0,fi} = 4.2$  m

conversion factor of internal forces from th.l.o. to th.ll.o.  $f^{I-II} = 0.70$

#### 1.5.2.1. design calculation values

| lc | $N_{Ed}$<br>kN | $M_{y,Ed}$<br>kNm | $M_{z,Ed}$<br>kNm |             | lc | $N_{Ed}$<br>kN | $M_{y,Ed}$<br>kNm | $M_{z,Ed}$<br>kNm |             |
|----|----------------|-------------------|-------------------|-------------|----|----------------|-------------------|-------------------|-------------|
| 1  | -317.69        | 11.29             | 43.73             | Import lc 1 | 4  | -200.57        | -32.84            | 21.54             | Import lc 4 |
| 2  | -181.37        | -32.84            | 53.87             | Import lc 2 | 5  | -197.69        | 5.27              | 49.51             | Import lc 5 |
| 3  | -288.89        | 8.89              | 13.71             | Import lc 3 | 6  | -272.57        | -29.23            | 18.07             | Import lc 6 |

## 2. bending/shear design

### material properties

bending design:

concrete acc. to EC 2, 3.1.7(1): C30/37,  $\varepsilon_{c2} = -2.00\%$ ,  $\varepsilon_{cu2} = -3.50\%$ ,  $f_{cd} = 17.00 \text{ N/mm}^2$

reinf. external acc. to EC 2, 3.2.7(2a): B500A,  $\varepsilon_{ud} = 25.0\%$ ,  $f_{yd} = 434.78 \text{ N/mm}^2$ ,  $f_{td} = 456.52 \text{ N/mm}^2$ ,  $E_s = 200000.0 \text{ N/mm}^2$

minimum reinforcement:



$\sigma$ - $\varepsilon$  line acc. to EC 2, 3.2.7(2b): B500A,  $f_{yk} = 500.0 \text{ N/mm}^2$ ,  $E_s = 200000.0 \text{ N/mm}^2$

shear design:

$\sigma$ - $\varepsilon$  line acc. to EC 2, 3.2.7(2a): B500A,  $\varepsilon_{ud} = 25.00\%$ ,  $f_{yd} = 434.78 \text{ N/mm}^2$ ,  $f_{td} = 456.52 \text{ N/mm}^2$ ,  $E_s = 200000.0 \text{ N/mm}^2$

## 2.1. results table

| lc | $N_{Ed}$<br>kN | $M_{Ed}$<br>kNm | $V_{Ed}$<br>kN | $A_{sa}$<br>cm <sup>2</sup> | $a_{sbv}$<br>cm <sup>2</sup> /m |            |
|----|----------------|-----------------|----------------|-----------------------------|---------------------------------|------------|
| 1  | -742.03        | 178.95          | 39.49          | 26.52                       | 3.71                            |            |
| 2  | -96.56         | 271.11          | 52.85          | 55.14                       | 3.71                            |            |
| 3  | -691.63        | 268.48          | 58.20          | 51.09                       | 3.71                            |            |
| 4  | -655.63        | 48.99           | 12.25          | 2.26                        | 3.71                            | min reinf. |
| 5  | -240.56        | 347.34          | 69.55          | 73.74                       | 3.71                            |            |
| 6  | -218.99        | 18.05           | 4.52           | 0.76                        | 3.71                            | min reinf. |
| 7  | -668.58        | 203.60          | 41.08          | 33.40                       | 3.71                            |            |
| 8  | -534.56        | 345.38          | 69.28          | 72.18                       | 3.71                            |            |
| 9  | -253.63        | 21.56           | 5.38           | 0.88                        | 3.71                            | min reinf. |

N,M,V: design calculation values;  $A_{sa}$ : flexural reinforcement;  $a_{sbv}$ : shear reinforcement

## 2.2. lc 5 (decisive)

### 2.2.1. bending design (EC 2, 6.1)

bending/normal force

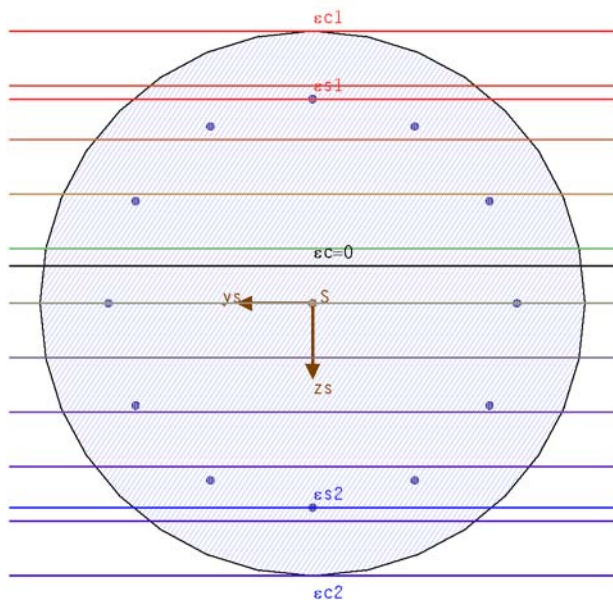
design calculation values:  $N_{Ed} = -240.56 \text{ kN}$ ,  $M_{Ed} = 347.34 \text{ kNm}$

design aid values:  $d = 30.4 \text{ cm}$ ,  $z = 24.4 \text{ cm}$ ,  $x = 17.25 \text{ cm}$

reinforcement

$A_{sa} = 73.74 \text{ cm}^2$

limit strains



limit strains:  $\varepsilon_{c1} = -3.500\%$ ,  $\varepsilon_{s1} = -2.485\%$ ,  $\varepsilon_{s2} = 3.600\%$ ,  $\varepsilon_{c2} = 4.615\%$ ,  $\alpha_k = 90.00^\circ$

### 2.2.2. shear design (EC 2, 6.2)

shear force (EC 2, 6.2)

design shear force  $V_{Ed} = 69.55 \text{ kN}$

design aid values:  $\rho_l = 2.00\%$ ,  $z' = 24.4 \text{ cm}$ ,  $x = 17.25 \text{ cm}$ ,  $V_{Rd,c} = 114.15 \text{ kN}$ ,  $\Theta = 39.81^\circ$ ,  $V_{Rd,max} = 612.01 \text{ kN}$ ,

$AB = 1$  for  $V_{Ed}/V_{Rd,max} = 0.114$ ,  $\Delta F_{s,Ed} = 41.73 \text{ kN}$

reinforcement

$a_{sbv} = 3.71 \text{ cm}^2/\text{m}$

messages for calculation run

shear design: cross section compressed

shear design: longitudinal reinforcement considered

## 2.3. result

resulting reinforcement:  $A_{sa} = 73.74 \text{ cm}^2$

$a_{sbv} = 3.71 \text{ cm}^2/\text{m}$

incl. base reinforcement:

$A_{sa} = 73.74 \text{ cm}^2$

$a_{sbv} = 3.71 \text{ cm}^2/\text{m}$

### 3. fire design

#### material properties

concrete acc. to EC 2, 3.1.7(1): C30/37,  $\varepsilon_{c2} = -2.00\%$ ,  $\varepsilon_{cu2} = -3.50\%$ ,  $f_{cd} = 20.00 \text{ N/mm}^2$

reinf. external acc. to EC 2, 3.2.7(2a): B500A,  $\varepsilon_{ud} = 25.0\%$ ,  $f_{yd} = 434.78 \text{ N/mm}^2$ ,  $f_{td} = 456.52 \text{ N/mm}^2$ ,  $E_s = 200000.0 \text{ N/mm}^2$

#### 3.1. results table

initial reinforcement:  $A_{sa,0} = 13.57 \text{ cm}^2$

| lc | $N_{Ed}$<br>kN | $M_{Ed}$<br>kNm | $A_{sa}$<br>$\text{cm}^2$ | $\Delta A_{sa}$<br>$\text{cm}^2$ | $\mu_{fi}$ | $\mu_{fi,max}$ |
|----|----------------|-----------------|---------------------------|----------------------------------|------------|----------------|
| 1  | -317.69        | 45.16           | 13.57                     | ---                              | 0.000      | 0.490          |
| 2  | -181.37        | 63.09           | 13.57                     | ---                              | 0.000      | 0.490          |
| 3  | -288.89        | 16.34           | 13.57                     | ---                              | 0.000      | 0.490          |
| 4  | -200.57        | 39.27           | 13.57                     | ---                              | 0.000      | 0.490          |
| 5  | -197.69        | 49.79           | 13.57                     | ---                              | 0.000      | 0.490          |
| 6  | -272.57        | 34.36           | 13.57                     | ---                              | 0.000      | 0.490          |

N,M: design calculation values;  $A_{sa}$ : flexural reinforcement;  $\Delta A_{sa}$ : additional reinforcement;  $\mu_{fi}, \mu_{fi,max}$ : existing, maximum utilization

#### 3.2. lc 1 (decisive)

design calculation values:  $N_{Ed} = -317.69 \text{ kN}$ ,  $M_{Ed} = 45.16 \text{ kNm}$

reinforcement

$A_{sa} = 13.57 \text{ cm}^2$

#### fire protection verification for compression members

goal: fire resistance class R 90 ( $\mu_{fi,max} = \mu_{fi} \cdot f^{1-11} = 0.700 \cdot 0.70 = 0.490$ )

utilization:  $\mu_{fi} = 0.000 < \mu_{fi,max} = 0.490$  ok

#### Feuerwiderstandsdauer (EC 2-1-2, 5.3.2(4), Gl. (5.7)):

Kreis:  $\varnothing = 400 \text{ mm}$ ,  $d_1 = 50 \text{ mm}$ ,  $l_{0,fi} = 4.20 \text{ m}$ ,  $A_s = 1357 \text{ mm}^2$ ,  $\mu_{fi} = 0.000$

Voraussetzungen:  $d_1 \geq 25 \text{ mm}$ ,  $l_{0,fi} \leq 6 \text{ m}$ ,  $200 \text{ mm} \leq b' \leq 450 \text{ mm}$ ,  $A_s \leq 0.04 \cdot A_c$ ,  $\mu_{fi} \leq 1$

$A_c = 125664 \text{ mm}^2$ ,  $b' = \varnothing = 400 \text{ mm}$

$\omega = (A_s \cdot f_{yd}) / (A_c \cdot f_{cd}) = 0.276$  with  $f_{yd} = 434.8 \text{ N/mm}^2$ ,  $f_{cd} = 17.00 \text{ N/mm}^2$

$R_{\eta,fi} = 83 \cdot (1 - \mu_{fi} \cdot (1 + \omega)) / ((0.85 / \alpha_{cc}) + \omega) = 82.98$ ,  $\alpha_{cc} = 0.85$

$R_a = 1.6 \cdot (d_1 - 30) = 32.00$ ,  $R_1 = 9.6 \cdot (5 - l_{0,fi}) = 7.68$ ,  $R_b = 0.09 \cdot b' = 36.00$ ,  $R_n = 12$  for  $n > 4$  Stäbe

Feuerwiderstandsdauer  $R = 120 \cdot ((R_{\eta,fi} + R_a + R_1 + R_b + R_n) / 120)^{1.8} = 226 \text{ min}$

$\Rightarrow$  fire resistance class R 180

maximale fire resistance class R 180 > R 90 ok

#### 3.3. result

resulting reinforcement:  $A_{sa} = 13.57 \text{ cm}^2$

incl. base reinforcement:  $A_{sa} = 13.57 \text{ cm}^2$

### 4. final result

maximum reinforcement:  $A_{sa} = 73.74 \text{ cm}^2$

$a_{sbV} = 3.71 \text{ cm}^2/\text{m}$

### design resistance ensured

#### 5. selected reinforcement

lateral concrete cover  $c_{vr} = 2.0 \text{ cm}$

bottom:

concrete cover  $c_{va} = 3.0 \text{ cm}$

longitudinal reinforcement from bending and normal force  $24 \times \varnothing 20$

reinforcement ext  $A_{sa} = 75.40 \text{ cm}^2 > \text{req } A_{sa} = 73.74 \text{ cm}^2$  ok

bar distance min  $d_{va} = 4.0 \text{ cm}$

center distance ext  $d_a = 4.8 \text{ cm} < d_a = 5.00 \text{ cm}^2$  ok

above:

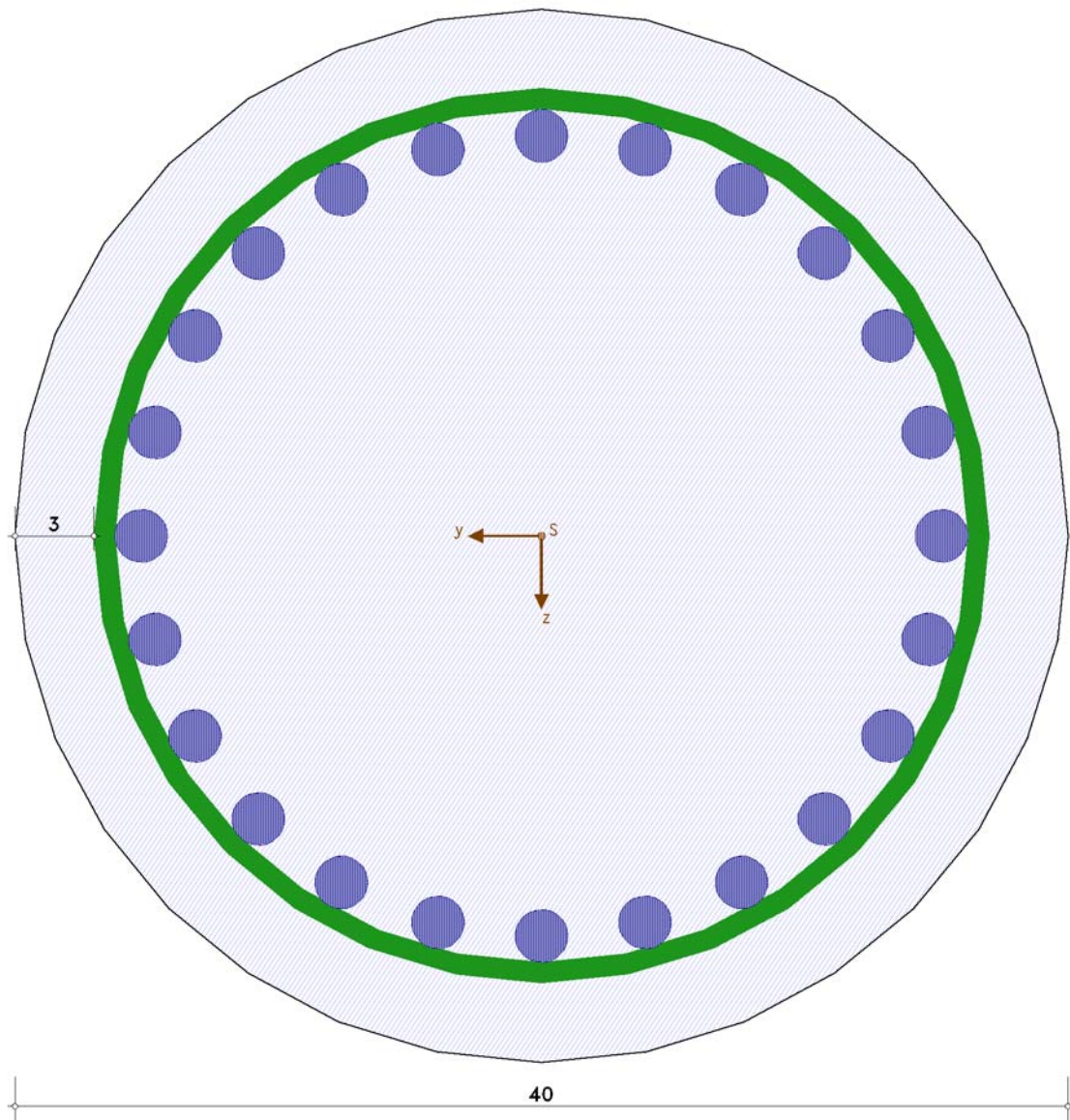
concrete cover  $c_{vi} = 2.0 \text{ cm}$

shear reinforcement:

stirrup reinforcement from shear force  $\varnothing 8 / 25.0 \text{ cm}$ , 2-cut

reinforcement ext  $a_{sbV} = 4.02 \text{ cm}^2/\text{m} > \text{req } a_{sbV} = 3.71 \text{ cm}^2/\text{m}$  ok

graphic:



## 6. regulations

EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

EN 1990/NA, Nationaler Anhang zur EN 1990, Ausgabe Dezember 2010

EN 1992-1-1, Eurocode 2: Bemessung und Konstruktion von Stahlbeton- und Spannbetonbauteilen -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1992-1-1:2004 + AC:2010, Ausgabe Januar 2011

EN 1992-1-1/NA, Nationaler Anhang zur EN 1992-1-1, Ausgabe April 2013