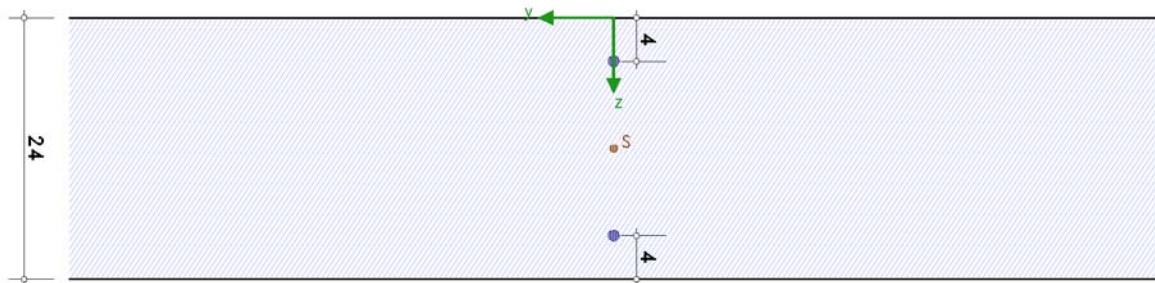


1. input protocol



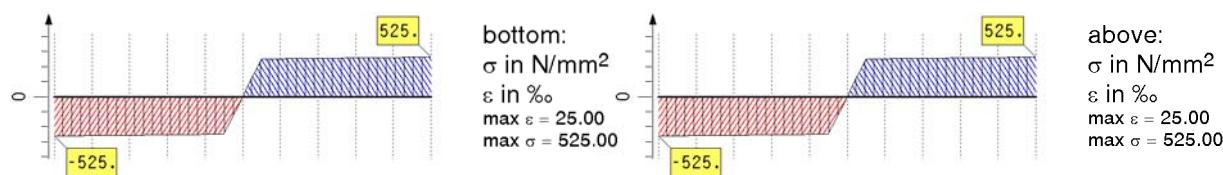
1.1. building material

reinforcing steel bottom B500A, above B500A, concrete C30/37

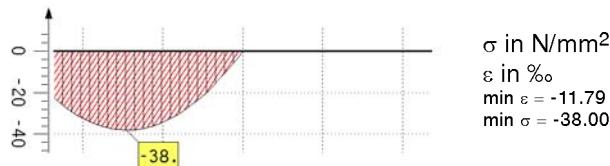
characteristic values for the consideration of creep and shrinkage in concrete (for verifications in SLS):
creep coefficient $\varphi_{eff} = 2.367$, shrinkage $\epsilon_{cs,\infty} = 0.000\%$

characteristic values for the calculation of effective concrete strengths (crack verification): cement CEM 32.5 R (class N),
effective section thickness $h_0 = 24.0$ cm

stress-strain line of reinforcing steel: EC 2-1-1, 3.2.7 (bilinear)



stress-strain line of concrete: EC 2-1-1, 3.1.5 (realistic)



1.2. material safety factors

serviceability: concrete $\gamma_c = 1.00$, reinforcement $\gamma_s = 1.00$

1.3. cross section

plate: $h = 24.0$ cm

axis distances: $d_o = 4.0$ cm, $d_u = 4.0$ cm

base reinforcement: $A_{so0} = \emptyset 10 / 90.0 = 0.87 \text{ cm}^2/\text{m}$, $A_{su0} = \emptyset 10 / 90.0 = 0.87 \text{ cm}^2/\text{m}$
max. reinforcement ratio $\rho_s = 8.00\%$

1.4. durability and concrete cover

above: minimum strength class, concrete cover for $\emptyset_s = 10$ mm

due to reinforcement corrosion XC1 \Rightarrow C16/20, $c_{min} = \emptyset_s = 10$ mm, $\Delta c = 10$ mm, $c_{nom} = c_{min} + \Delta c = 20$ mm

minimum concrete quality C16/20 with $f_{ck} = 16.0 \text{ N/mm}^2 < 30.0 \text{ N/mm}^2$ ok

minimum axial spacing min $d = c_{nom} + \emptyset_s/2 = 25$ mm < clc $d = 40$ mm ok

bottom: minimum strength class, concrete cover for $\emptyset_s = 10$ mm

due to reinforcement corrosion XC2 \Rightarrow C16/20, $c_{min} = 20$ mm, $\Delta c = 15$ mm, $c_{nom} = c_{min} + \Delta c = 35$ mm

due to concrete attack XA1 \Rightarrow C25/30

minimum concrete quality C25/30 with $f_{ck} = 25.0 \text{ N/mm}^2 < 30.0 \text{ N/mm}^2$ ok

minimum axial spacing min $d = c_{nom} + \emptyset_s/2 = 40$ mm \leq clc $d = 40$ mm ok

1.5. design parameters

1.5.1. crack verification

perm. crack width: $w_{o,lim} = 0.30 \text{ mm}$, $w_{u,lim} = 0.30 \text{ mm}$

bar diameter of the crack-distributing reinforcement: $\varnothing_{ro} = 10 \text{ mm}$, $\varnothing_{ru} = 10 \text{ mm}$

1.5.1.1. minimum reinforcement (EC 2, 7.3.2)

calculation acc. to Lohmeyer/Ebeling

time of crack initiation $t_{crit} = 1.3 \cdot t_{max,T} + 24 = 56 \text{ h}$,

$t_{max,T} = 25 \text{ h}$ for normal hardening concrete (CEM 32.5 R) and $h_0 = 24.0 \text{ cm}$

concrete tensile strength during initial cracking $f_{ct,eff} = k_{ct} \cdot f_{ctm} = 1.98 \text{ N/mm}^2$,

coefficient $k_{ct} = k_j \cdot k_{ct}(t) = 0.68$ for normal hardening concrete (CEM 32.5 R) and $t_{crit} = 56 \text{ h}$, $k_{ct}(t) = 0.68$,

$k_j = 1.0$ (spring/autumn)

calculation of the constraint force for in-situ concrete walls

dimensions of the wall $H_w = 3.20 \text{ m}$, $L_w = 6.00 \text{ m}$, $t_w = 24.0 \text{ cm}$

constraint force $N_{ct} = \sigma_{ct,d} \cdot A_{c,eff} = 449.55 \text{ kN/m}$, $A_{c,eff} = 2080.0 \text{ cm}^2/\text{m}$

design value of constraint stress $\sigma_{ct,d} = k_{ct,d} \cdot \sigma_{ct}(t) = 2.16 \text{ N/mm}^2$, $k_{ct,d} = 0.48$ for $L_w/H_w = 1.88$

constraint stress $\sigma_{ct}(t) = \alpha_T(t) \cdot \Delta T_{c,B} \cdot E_c(t) + \varepsilon_{cst} \cdot E_c(t) = 4.49 \text{ N/mm}^2$

shrinkage at time $t = 56 \text{ h}$: $\varepsilon_{cst} = -(\varepsilon_{cas} + \varepsilon_{cds}) = -0.020\%$, where

autogenous shrinkage: $\varepsilon_{cas} = \varepsilon_{cas,0} \cdot \beta_{as} = 0.013\%$, with $\varepsilon_{cas,0} = 2.5 \cdot (f_{ck}-10) = 0.050\%$, $\beta_{as} = 1 - e^{-0.2 \cdot t^{1/2}} = 0.263$

drying shrinkage: $\varepsilon_{cds} = \varepsilon_{cds,0} \cdot \beta_{ds} \cdot k_h = 0.007\%$, with $\varepsilon_{cds,0} = 0.85 \cdot ((220+110 \cdot \alpha_{ds1}) \cdot e^{-\alpha_{ds2} \cdot f_{cm}/10}) \cdot \beta_{RH} = 0.557\%$,

$k_h = 0.81$ for $h_0 = 24.0 \text{ cm}$, $\alpha_{ds1} = 4.0$ and $\alpha_{ds2} = 0.12$ for cement group N,

$\beta_{RH} = 1.55 \cdot (1 - (RH/100)^3) = 1.356$ for $RH = 50\%$, $\beta_{ds} = \Delta t / (\Delta t + 0.04 \cdot (h_0^3)^{1/2}) = 0.015$, $\Delta t = t - t_s = 2.33 \text{ d}$

coefficient of thermal expansion of young concrete $\alpha_T(t) = 12.7 \cdot 10^{-6} \text{ 1/K}$ at time $t = 2.33 \text{ d}$ (56 h)

average cooling of concrete $\Delta T_{c,B} = 12.2 \text{ K}$ for normal hard. concrete (CEM 32.5 R) and $h_0 = 24.0 \text{ cm}$ (spring/autumn)

E-modulus of young concrete $E_c(t) = k_{Et} \cdot E_c = 25651.9 \text{ N/mm}^2$, tangent modulus $E_c = 1.05 \cdot E_{cm} = 34478.4 \text{ N/mm}^2$

coefficient $k_{Et} = \alpha_{E,g} \cdot 0.83 = 0.74$ for normal hardening concrete (CEM 32.5 R) and $t_{crit} = 56 \text{ h}$, $\alpha_{E,g} = 0.9$

constraint force $N_{ct} = 449.55 \text{ kN/m}$

constraint force (EC 2): $N_{ct,EC2} = f_{ct,eff} \cdot A_{c,eff} = 411.68 \text{ kN/m}$, $f_{ct,eff} = 1.98 \text{ N/mm}^2$, $A_{c,eff} = 2080.0 \text{ cm}^2/\text{m}$

constraint force $N_{ct} > N_{ct,EC2} \Rightarrow$ crack resistance not existent ($N_{ct}/N_{ct,EC2} = 1.092 > 1$) $\Rightarrow N_{ct} = N_{ct,EC2}$

calculation of minimum reinforcement with $N_{ct,clc} = N_{ct} \cdot A_c / A_{c,eff} = 475.02 \text{ kN/m}$, $A_c = 2400.0 \text{ cm}^2/\text{m}$, $A_{c,eff} = 2080.0 \text{ cm}^2/\text{m}$

coefficient for stress distribution k_c from centric constraint

coefficient for consideration of nonlinearily distributed residual stresses k from self-induced constraint

2. notes

crack verification: perm. crack width (load+constraint) is not verified.

cross section type plate: results refer to 1 m plate width.

3. crack verification

material properties

σ - ϵ line acc. to EC 2, 3.1.5(1): C30/37, $\varepsilon_{c1} = -2.16\%$, $\varepsilon_{cu1} = -3.50\%$, $f_{cm} = 38.00 \text{ N/mm}^2$, $E_{cm} = 32836.6 \text{ N/mm}^2$

σ - ϵ line acc. to EC 2, 3.2.7(2a): B500A, $\varepsilon_u = 25.00\%$, $f_{yk} = 500.0 \text{ N/mm}^2$, $f_{tk} = 525.0 \text{ N/mm}^2$, $E_s = 200000.0 \text{ N/mm}^2$

σ - ϵ line acc. to EC 2, 3.2.7(2a): B500A, $\varepsilon_u = 25.00\%$, $f_{yk} = 500.0 \text{ N/mm}^2$, $f_{tk} = 525.0 \text{ N/mm}^2$, $E_s = 200000.0 \text{ N/mm}^2$

3.1. calculation of minimum reinforcement (EC 2, 7.3.2)

crack stress $\sigma_{cr} = 1.98 \text{ N/mm}^2$, coefficient for non-linear residual stresses $k = 0.80$

reinforcement above

perm. crack width $w_{o,lim} = 0.30 \text{ mm}$

coefficient for stress distribution $k_{co} = 1.00$, tension zone $A_{cto} = 12.00 \text{ dm}^2$, crack zone $A_{c,eff,o} = 10.40 \text{ dm}^2$

stress in reinforcement $\sigma_{sro} = 266.9 \text{ N/mm}^2$

reinforcement (minimum reinforcement) $A_{so,min} = 7.12 \text{ cm}^2$

reinforcement bottom

perm. crack width $w_{u,lim} = 0.30 \text{ mm}$

coefficient for stress distribution $k_{cu} = 1.00$, tension zone $A_{ctu} = 12.00 \text{ dm}^2$, crack zone $A_{c,eff,u} = 10.40 \text{ dm}^2$

stress in reinforcement $\sigma_{sru} = 266.9 \text{ N/mm}^2$

reinforcement (minimum reinforcement) $A_{su,min} = 7.12 \text{ cm}^2$

4. final result

maximum reinforcement: $A_{so} = 7.12 \text{ cm}^2$, $A_{su} = 7.12 \text{ cm}^2$

design resistance ensured

5. regulations

EN 1990, Eurocode 0: Grundlagen der Tragwerksplanung;

Deutsche Fassung EN 1990:2002 + A1:2005 + A1:2005/AC:2010, Ausgabe Dezember 2010

EN 1990/NA, Nationaler Anhang zur EN 1990, Ausgabe Dezember 2010

EN 1992-1-1, Eurocode 2: Bemessung und Konstruktion von Stahlbeton- und Spannbetonbauteilen -

Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau;

Deutsche Fassung EN 1992-1-1:2004 + AC:2010, Ausgabe Januar 2011

